

Lappeenrannan teknillinen yliopisto
Lappeenranta University of Technology

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**TORQUE VIBRATION MODEL OF AXIAL-FLUX SURFACE-
MOUNTED PERMANENT MAGNET SYNCHRONOUS
MACHINE**

*Thesis for the degree of Doctor of Science
(Technology) to be presented with due
permission for public examination and
criticism in the Auditorium 1383 at
Lappeenranta University of Technology,
Lappeenranta, Finland on the 22nd of
August, 2003, at noon.*

Acta Universitatis
Lappeenrantaensis
154

ISBN 951-764-773-5
ISSN 1456-4491

Lappeenrannan teknillinen yliopisto
Digipaino 2003

ABSTRACT

Lappeenranta University of Technology
Acta Universitatis Lappeenrantaesis 154

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Lappeenranta 2003
ISBN 951-764-773-5, ISSN 1456-4991

In order that the radius and thus ununiform structure of the teeth and other electrical and magnetic parts of the machine may be taken into consideration the calculation of an axial flux permanent magnet machine is, conventionally, done by means of 3D FEM-methods. This calculation procedure, however, requires a lot of time and computer recourses. This study proves that also analytical methods can be applied to perform the calculation successfully. The procedure of the analytical calculation can be summarized into following steps: first the magnet is divided into slices, which makes the calculation for each section individually, and then the parts are submitted to calculation of the final results. It is obvious that using this method can save a lot of designing and calculating time.

The calculation program is designed to model the magnetic and electrical circuits of surface mounted axial flux permanent magnet synchronous machines in such a way, that it takes into account possible magnetic saturation of the iron parts. The result of the calculation is the torque of the motor including the vibrations. The motor geometry and the materials and either the torque or pole angle are defined and the motor can be fed with an arbitrary shape and amplitude of three-phase currents. There are no limits for the size and number of the pole pairs nor for many other factors. The calculation steps and the number of different sections of the magnet are selectable, but the calculation time is strongly depending on this. The results are compared to the measurements of real prototypes.

The permanent magnet creates part of the flux in the magnetic circuit. The form and amplitude of the flux density in the air-gap depends on the geometry and material of the magnetic circuit,

on the length of the air-gap and remanence flux density of the magnet. Slotting is taken into account by using the Carter factor in the slot opening area.

The calculation is simple and fast if the shape of the magnet is a square and has no skew in relation to the stator slots. With a more complicated magnet shape the calculation has to be done in several sections. It is clear that according to the increasing number of sections also the result will become more accurate. In a radial flux motor all sections of the magnets create force with a same radius. In the case of an axial flux motor, each radial section creates force with a different radius and the torque is the sum of these.

The magnetic circuit of the motor, consisting of the stator iron, rotor iron, air-gap, magnet and the slot, is modelled with a reluctance net, which considers the saturation of the iron. This means, that several iterations, in which the permeability is updated, has to be done in order to get final results.

The motor torque is calculated using the instantaneous linkage flux and stator currents. Flux linkage is called the part of the flux that is created by the permanent magnets and the stator currents passing through the coils in stator teeth. The angle between this flux and the phase currents define the torque created by the magnetic circuit.

Due to the winding structure of the stator and in order to limit the leakage flux the slot openings of the stator are normally not made of ferromagnetic material even though, in some cases, semimagnetic slot wedges are used. In the slot opening faces the flux enters the iron almost normally (tangentially with respect to the rotor flux) creating tangential forces in the rotor. This phenomenon is called cogging. The flux in the slot opening area on the different sides of the opening and in the different slot openings is not equal and so these forces do not compensate each other. In the calculation it is assumed that the flux entering the left side of the opening is the component left from the geometrical centre of the slot. This torque component together with the torque component calculated using the Lorentz force make the total torque of the motor.

It is easy to assume that when all the magnet edges, where the derivative component of the magnet flux density is at its highest, enter the slot openings at the same time, this will have as a result a considerable cogging torque. To reduce the cogging torque the magnet edges can be

shaped so that they are not parallel to the stator slots, which is the common way to solve the problem. In doing so, the edge may be spread along the whole slot pitch and thus also the high derivative component will be spread to occur equally along the rotation.

Besides forming the magnets they may also be placed somewhat asymmetric on the rotor surface. The asymmetric distribution can be made in many different ways. All the magnets may have a different deflection of the symmetrical centre point or they can be for example shifted in pairs. There are some factors that limit the deflection. The first is that the magnets cannot overlap. The magnet shape and the relative width compared to the pole define the deflection in this case. The other factor is that a shifting of the poles limits the maximum torque of the motor. If the edges of adjacent magnets are very close to each other the leakage flux from one pole to the other increases reducing thus the air-gap magnetization.

The asymmetric model needs some assumptions and simplifications in order to limit the size of the model and calculation time. The reluctance net is made for symmetric distribution. If the magnets are distributed asymmetrically the flux in the different pole pairs will not be exactly the same. Therefore, the assumption that the flux flows from the edges of the model to the next pole pairs, in the calculation model from one edge to the other, is not correct. If it were wished for that this fact should be considered in multi-pole pair machines, this would mean that all the poles, in other words the whole machine, should be modelled in reluctance net. The error resulting from this wrong assumption is, nevertheless, irrelevant.

UDC 621.313.323 : 621.318.2

Keywords: Permanent magnet synchronous machine, Axial-flux, tangential vibration

ACKNOWLEDGEMENTS

I wish thank all the parties who have promoted the progress of this thesis.

First I would like express my great gratitude for my supervisor Professor Juha Pyrhönen for creating the preconditions to carry out this study and for all his support and interest in the work. Also the good advice of the supporting team Markku Niemelä, Janne Nerg and Jussi Salo is considered with gratefulness. Asko Parviainen I wish to thank for the calculation support and the laboratory team Jouni Ryhänen, Harri Loisa and Martti Lindh for the measurement arrangements.

The financial support by IVO-foundation (at present Fortum foundation), Ulla Tuominen foundation, Tekniikan editämissäätiö, National Technology Agency of Finland, Finnish Academy, Metso Paper Oyj and ABB Industry Oy is highly appreciated. Kone Corporation and there especially Tarvo Viita-aho I thank for material and technical support.

I'm much obliged to Professor Tapani Jokinen and Dr. Eero Keskinen for valuable comments and corrections and Julia Vauterin for language review during pre examination.

Most of all I wish express my gratefulness to my family Kirsi, Laura, Henni and Jesse for standing beside me during these rough years. I love you.

Lappeenranta 31th of June 2003

Panu Kurronen

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ABSTRACT

ACKNOWLEDGEMENTS

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ABBREVIATIONS AND VARIABLES

ABBREVIATIONS

2D	Two-dimensional
3D	Three-dimensional
ABB DCS 500	ABB DC-converter tm
AFPMSM	Axial flux permanent magnet synchronous motor
CCW	Counter clockwise
CW	Clockwise
DC	Direct current
DTC	Direct Torque Control
FEM	Finite Element Method
T/I	Torque-Current -ratio
IM	Induction motor
mmf	Magneto motive force
NdFeB	Neodym Iron Boron -alloy
PM1	Permanent magnet shape
PM2	Permanent magnet shape
PM3	Permanent magnet shape
PMSM	Permanent magnet synchronous machine
SOR	Sector of a ring
RMS	Root mean square
SM	Synchronous motors
SmCo	Samarium Cobalt -alloy

VARIABLES

$[N]$	MMF matrix.
$[R]$	Reluctance matrix
B	Flux density

BH_{\max}	Energy product
B_{pm}	Permanent magnet remanence flux density
B_r	Remanence flux density
E	Electric field strength
f	Frequency
f_s	Rated supply frequency
g_l	Positive or negative integer.
g_a	Length variable
H	Field strength
H_c	Coercive force
H_c'	Coercivity
h_{pm}	Magnet thickness
h_{so}	Slot opening height
h_{to}	Tooth height
\hat{i}	Peak current
I	RMS current
i_d	Direct axis current
I_n	Motor rated current
JH_C	Coersivity
k_w	Constant.
L_{sc}	The length of the stator stack
m	Number of phases
n	Number of poles
n_c	Number of coils
NI	Total current of each individual coil
N_s	Number of turns in a slot
p	Number of pole pairs
P_n	Motor rated power
Q	Charge
q	Number of slots per pole and phase

Q_s	Number of slots
r	Radius
R	Reluctance
r_{ag}	Average air-gap radius
r_m	Permanent magnet outer radius (radial flux motor)
r_r	Rotor radius (radial flux motor)
r_s	Stator radius (radial flux motor)
ssg	Constant.
T	Torque
T_0	Average torque
T_{cog}	Cogging torque
T_ν	Torque harmonic of order ν
T_e	Electric torque
U_n	Motor rated voltage
ν	Speed
w	Local winding pitch
w/τ_p	Deviation of the coil span w from the pole pitch τ_p
W'	Co-energy
w_1	Distances from the calculation point to the slot opening edge
w_2	Distances from the calculation point to the slot opening edge
w_{PM}	Tangential width of the magnet or its section
w_{sl}	Slot width
w_{so}	Slot opening width
w_{to}	Tooth width
x	Length variable
Δ_{PM}	Distance
$\Delta\varphi_p$	Ideal phase shift
α	Calculation angle (elect.)
α_d	Angle corresponding to slot pitch
α_1	Angle shift

α_p	Magnet relative length
β	Factor, function of w_{so}/δ
δ_{ag}	Air-gap length
γ_s	Skewing angle of the magnet edge
μ_0	Permeability of vacuum
μ_{pm}	Relative permeability of the permanent magnet
μ_r	Relative permeability of the iron
ν	Order of harmonic
$\hat{\Theta}_\nu$	Magneto motive force
θ	Angular position
τ_p	Pole pitch
τ_s	Slot pitch
τ_ν	The pole pitch of the harmonic
ξ_ν	Winding factor of a harmonic
ψ_s	Flux linkage

1 INTRODUCTION

Speed controlled electrical drives and especially low speed systems may have severe vibration interactions with the driven mechanical system. The problem came into focus in low speed direct drive systems since in these cases the non-idealities of the motor and the power electronic controller are emphasized. At low speeds the mechanical system does not filter undesirable torque vibrations from the driven system. The most difficult torque vibration frequencies are lower than a few hundred hertz. Vibrations in this frequency range may proceed easily in mechanical systems and even in building constructions.

The wide use of electrical positioning, linear motors and controlled rotating machines in the industry has increased the complexity of vibration problems in mechanical systems. The torque ripple created by electric drives causes mechanical resonance in machines. Due to this, the dynamic interaction has to be taken into account when controlling the systems. These kinds of interactions may be found practically in every rotating mechanical system.

The consequences of mechanical vibration in rotating systems may be diverse. Not only mechanical wearing and brake down may be the result, but the transferable vibration or unbearable noise may also cause problems to its surroundings. Also the production quality may suffer from the unstable rotational speed or high level of vibration. Any of these may lead to malfunctions or to an exceeding of the set limits and may thus result in a restriction of use. In the industry these equipments can be part of the chain in a large production line. As a consequence of the costs caused by an interruption of production the demands for reliability increase significantly. To be able to avoid unexpected interruptions anticipatory condition monitoring based on vibration level measurement has been applied more and more commonly.

The problems mentioned above have lead to tightened regulations concerning vibrations and noise levels. These limits are part of the requirements set for the standard of living and, for this reason, must be applied for example to residential buildings. Noise level limits inside apartments caused by equipment inside the building, like air conditioning, elevators, etc., can be set even as low as 30 dBA (Bovärket 2001). This, again, sets high requirements to the industry manufacturing this type of equipment. Silencers or isolation materials can be used to limit the airborne noise, but vibration transferring through the structures may create noise even far from the source.

Excitation that leads to a vibrating system may be created by multiple sources such as non-idealities in speed control loop, frequency converter, motor electrical circuit, magnetic circuit, or it may be transferred from the surroundings. The excitations caused by non-idealities may be damped by material, parameters, manufacturing or design changes. Also active dampers, which are set to resonate at a certain frequency and thus suck the vibration excitation, are sometimes used. To avoid the system interrupting the surroundings or vice versa noise or vibration isolation is required.

Until now most industrial low speed applications have been driven either with DC motors or induction motors with reduction gears. Synchronous machines have mostly been used as generators. Figure 1.1 illustrates the distribution of motor types in Stora-Enso paper mills in Imatra in 1994 (Kaukonen 1994). Since then, the situation has not changed dramatically.

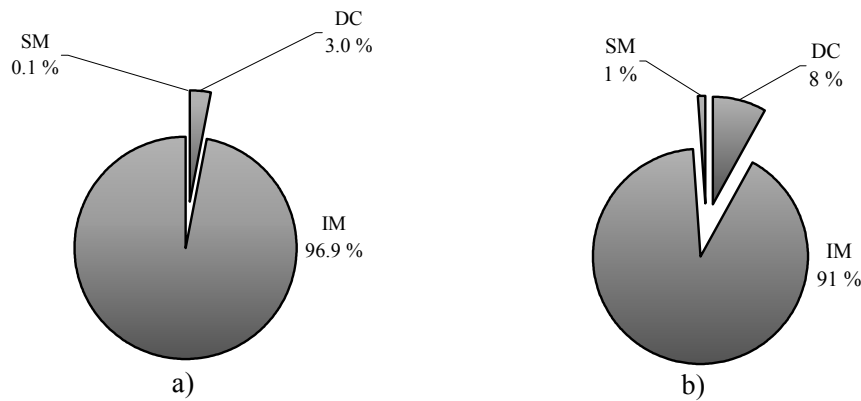


Fig. 1.1. Motor type distribution in Stora-Enso Kaukopää paper mills 1994. a) shows the number of motors and b) the rated cumulative installed power of the motors. IM stands for induction motors, SM for synchronous motors and DC for DC-motors.

It can be seen clearly that, on the average, DC and synchronous motors have, compared to induction motors, a larger rate of use when the rated power is considered, whereas the rate remains much lower when only the number of used motors is considered. Compared to the induction motor having an equal power the DC and synchronous motor are often expensive and, due to the brushes, require a lot of service and typically also external excitation sources. The problem with induction motors is that the slip with a certain torque is about constant. Rotor losses correspond to the relative slip and when the synchronous speed is reduced, the relative slip and thus the losses increase. During the latest decade permanent magnet materials and

frequency control techniques have developed rapidly. This has brought that permanent magnet synchronous machines have been used more widely and in different types of applications. With permanent magnet synchronous machine gearless drives also the low speed area can be covered maintaining high efficiency.

Permanent magnet synchronous machines (PMSMs) are nowadays used in several pilot applications in paper mills. The machine type is also more and more often used in ship propulsion systems and in direct driven windmills. Lift and hoist applications have pioneered this development and successful mature products are already on the market.

New motor types are often developed for a certain application having certain boundary conditions. There exist no design tradition and modern methods, such as the Finite Element Method (FEM), are used to develop these new machine types.

1.1 Existing Calculation Methods

Traditionally, motors have been designed using analytical calculations, trial and error. The analytical calculations, which formerly were done by hand, have been replaced by computer aided analytical calculations in everyday design. Especially the system for induction motor design has matured during the latest one hundred years. During the latest decades the FEM has become a common tool to design and calculate electrical motors. The advantage of the method is that it allows very accurate defining of the motor details and used materials, but also, at the same time, focusing on the design of the most interesting areas or parameters. It also gives a lot of possibilities to calculate different types of parameters such as torque, forces, electrical parameters, material saturation level in different parts etc. Many commercial FEM-programs are able to communicate with different types of calculation systems, like electrical circuit simulators. This offers a lot of new possibilities to take into account different factors of different systems and their mutual effect. Many programs also allow both steady state and transient calculations.

Two-dimensional (2D) solvers have been available for about 20 years. Along the years the development of the software as well as hardware has been enormous. In many cases the problems were much too large or complex to be solved. Three-dimensional calculation has become more popular, but the 2D FEM is still more commonly used. In some cases, 3D-calculation doesn't give any extra advantage since the calculation time or resources are normally always limited. Also modelling is generally a lot easier with 2D. However, the

electrical motor has typical factors, which require 3D calculation to achieve accurate results. These 3D-problems result from the rotor skewing, the motor end-effects in short machines or the axial flux structure, which causes a changing of the factors along the radius. In permanent magnet machines the magnet edges are often skewed in relation to the stator slots in order to reduce the high cogging effect. This means that PMSMs, practically, almost always require 3D calculation. Normally, it is not necessary to calculate and model the whole motor, but it is enough to calculate only one sector of the machine because of its symmetry. When the flux paths can be assumed to be on a plane, as in a radial flux motor with neglected coil end effects, calculation can be made two-dimensionally in axial sections.

FEM includes large matrixes to be solved, and it is easy to understand, that large systems or complex structures need a high amount of elements. The denser part of small elements can be set in critical areas, like air-gap, to be examined, and a sparser element net in less meaningful areas of the magnetic circuit. Transient or steady state rotating motor calculations still need a lot of time for modelling and calculating. The process to model and calculate one single case in one operational point may take days or even weeks. Often, this is a far too slow process, especially, if the design obtained after the first cycle is not satisfying, but requires one or more iterations in the process. This explains why there still exists a real need for a tool that makes modelling faster, even though the results obtained would be to some extent less accurate.

Vibration problems in electrically driven mechanical systems are the sum of different factors. It is not enough to model just the motor, drive or actuator. The mutual effects of different components have a great impact on the final result. Until now, there exist various solution methods and software to be applied to the respective mechanical systems and to the respective drives and motors. It would be a huge if not an impossible task to combine the commercial mechanics simulator, electrical motor FEM and circuit simulator with the system feedback. Even if that could be done, the solution environment would grow so large and slow, that the result would be a solver that cannot be applied for example to the R&D development process where typically a number of iteration loops is needed.

1.2 Mechanical System Vibrations

Mechanical vibration is the sum of all sinusoidal movements of the system components. The movements are not necessarily homogenous inside each of the components, but may also cause internal forces. In its simplest form it may consist of only one frequency and amplitude, but in multiplex systems it may include an infinite number of frequencies and amplitudes. In addition

to this, the vibrations may appear in different degrees of freedom. They may be components in 3D-coordinates or they can be radial or torsional (tangential). (Newland, 1989)

Each mechanical system has its own natural frequencies. This means that the shape and materials give the system its properties to dampen excitations with different frequencies. These properties in different degrees of freedom normally differ from each other. The more complex the system is the higher is the number of natural frequencies. For example high-speed drives are normally tried to be kept subcritical. In practice, this means that the rotational speed is kept under the first bending mode of the rotating system. When this speed is exceeded, the rotor starts to bend causing vibrations and great stress to the bearings. In addition to the shape and material, the amplitude is in such a case also dependent of the rotational balance of the system and thus high-speed systems are normally carefully balanced.

Figure 1.2 shows the bending mode frequency response of a cylindrical rotor and of the same rotor with identical masses (large inertia) fixed on both ends of the shaft. It can be noticed that increasing the mass of the system reduces the natural frequencies of the system and adds new components to the spectrum. When excitation occurs at these critical frequencies the vibration is highly amplified. It is not necessary to run at critical frequency, but the excitation may be for example a supply frequency multiple (harmonic order).

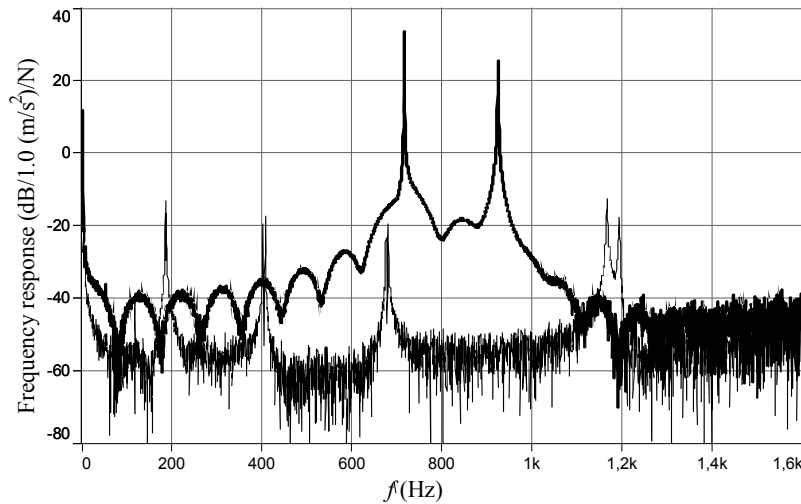


Fig. 1.2. Typical frequency response of a cylindrical rotor (higher peaks) and the same rotor with impellers at both ends of the shaft (Measured by the author in a medium speed machine application).

When there is only one frequency and direction it is usually easy to find a way to dampen the vibration or even totally get rid of it. In complex systems, damping the vibrations usually requires a number of different technologies and is a compromise that leads to an acceptable result. Typical ways of avoiding vibration problems are: decreasing the excitation, using a resonator to suck the critical excitation, changing the mechanical structure to keep the natural frequencies above the excitations or limiting the operation of the application to uncritical rotational speeds.

Frequency converters often have the feature due to which so-called predefined forbidden frequencies are avoided. This property is typically used, when in normal operation or during acceleration the natural frequencies have to be passed fast. In practice, this means that these frequencies with a certain tolerance are passed quickly and continuous operation is kept either above or below this area.

The increased computer capacity and sophisticated programs have enabled the development of good tools to calculate the natural frequencies of a component or even of a complicated mechanical system. For the existing systems these can be found by means of the modal analysis. The modal analysis is normally commenced by giving a mechanical impulse to the system using an impulse hammer. After this, the frequency response of the mechanical system is measured. Also the mode type can be found with this system.

1.3 Permanent Magnet Synchronous Motor

Traditionally, separately excited synchronous machines (SM) have been used as generators and high power motors, often with higher voltages. Even though the SM has an efficiency that can easily be higher than that of the induction or DC-motor and has an adjustable power factor, it is seldom used in other than large industrial or traction applications. Compared to the induction motor it is more difficult to use for example in applications that require a frequently starting of the motor. As the denomination indicates, the rotor rotation has to be synchronized to the voltage supply in both the velocity and phase angle in order to achieve a successful start up. In practice, this calls for the use of vector controlled inverters. When using an induction motor the start up may be done by directly switching the machine on the network. Also scalar inverters or soft starters may be used. Also the SM structure with wound rotor and slip rings make them more expensive to manufacture.

Since high-energy permanent magnets were discovered and frequency converters with synchronous motor applications entered the market, the use of synchronous motors has rapidly increased. Especially in low speed applications, which traditionally have been driven with induction motors and reduction gears, the gearless PMSM drive is now often an alternative for replacement. Induction motors are not used without gears in low speed applications since in direct drives the relatively high per unit slip increases the rotor losses remarkably.

1.3.1 Development and Features of Permanent Magnet Material

The development of permanent magnet material has been fast during the latest decades. First, the materials were based on Cobalt -, Tungsten - and Chromium – iron alloys. – Aluminium – Nickel - Cobalt alloys were discovered in the 1930s, but the developing of Samarium – Cobalt in the 1960s and finally Neodymium – Iron – Boron based magnets in the late seventies made it possible to benefit the permanent magnet materials in electrical motors. Figure 1.3 shows the development of the energy content of different permanent magnet materials. The slope in the curve is rather radical up to the year 1983. Since then, the energy density did not rise dramatically nor any new types of material were published, but a lot of interest has been focused on the material properties of Neo-magnets , like corrosion resistance and temperature tolerance.

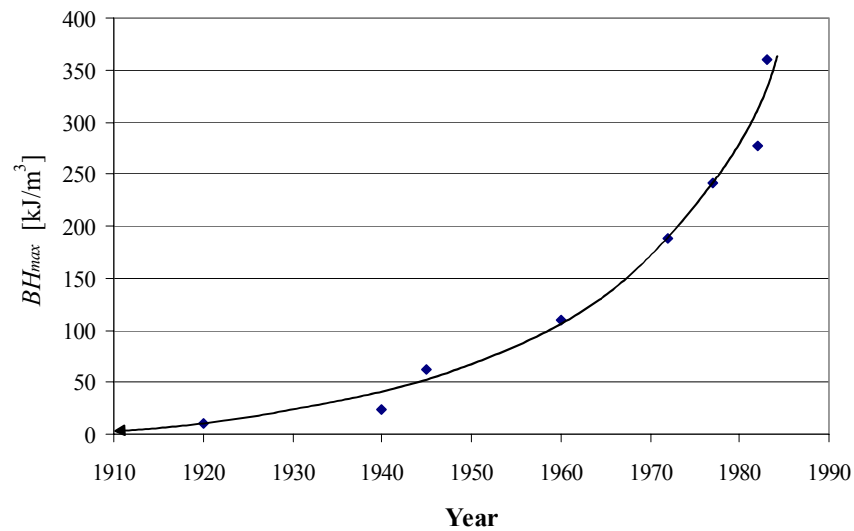


Fig. 1.3. Development of the permanent magnet materials (Pyrhönen 1991).

Especially the good properties - a large remanence and coercivity - of SmCo and NdFeB magnets have made it possible to introduce the application of these materials to industrial motors. The coercive forces of both of these materials are large enough to tolerate a large demagnetising armature reaction. This property makes the utilization of these materials possible in motor and generator drives where negative d-axis currents are allowed. The traditional $i_d = 0$ control method is no more needed and new, much more effective control methods like DTC (Direct Torque Control) have been introduced for application to PMSM drives (Luukko 2000). Compared to motors driven with $i_d = 0$ control, the DTC control method offers the possibility even to reduce the motor size. Figure 1.4 illustrates a typical NdFeB -type of permanent magnet temperature dependent BH-curves. When the external opposite field strength becomes larger than the so-called knee in the relevant curve, irreversible changes occur in the magnetisation. This phenomenon is called demagnetisation.

However, there are some properties related to the use of permanent magnet materials, which have slowed down the final break through. The patents concerning the materials and the material prices have kept the cost of the magnets quite high. Also the manufacturing process is quite complicated.

The first generation of NdFeB-magnets was susceptible to corrosion and had thus to be protected carefully against humidity. Now, the materials have improved remarkably, but still this weakness should be taken carefully into consideration. The phenomenon called white corrosion emerges, when the magnetic material is exposed to hydrogen. When corrosion occurs, the material turns to white powder and loses its properties. For this reason, practically all magnetic materials are either coated or phosphated.

Typically, the temperature limitation for permanent magnets is below 120 degrees Celsius due to the temperature dependent demagnetisation curves of the magnets. In the latest years, with the use of special alloys this limit could be raised for some magnets to about 180 °C.

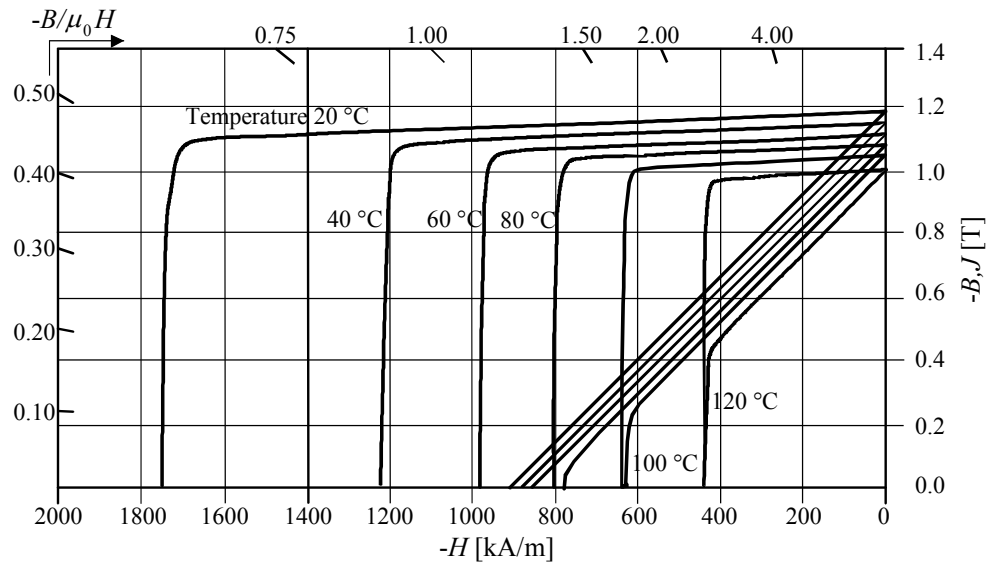


Fig. 1.4. Temperature dependent demagnetisation curves of a NeFeB – magnet type (Neorem, 2003).

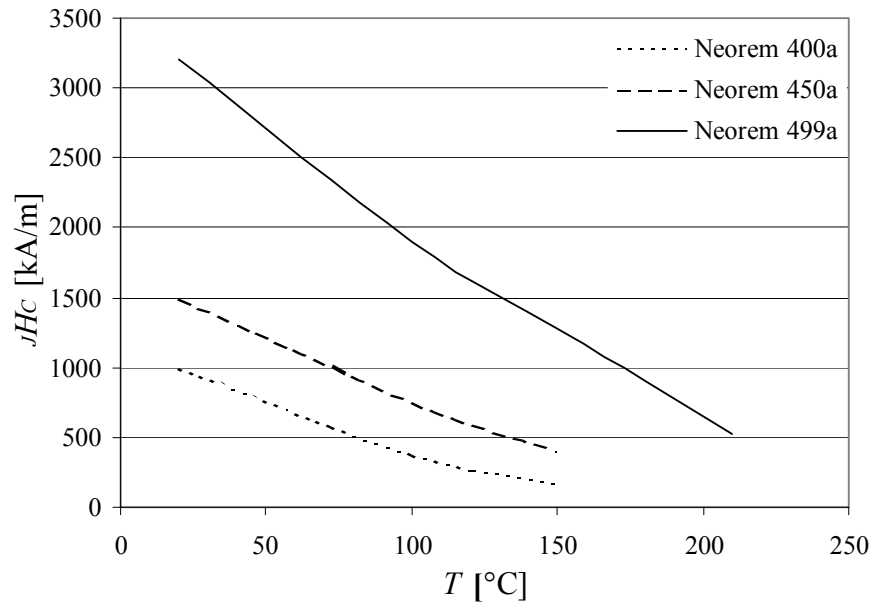


Fig. 1.5. Temperature dependence of the coercivity with different NdFeB PM materials (Neorem 2003).

While raising the temperature tolerance, part of the magnetic properties will be lost. For example, Neorem 400a has an energy product (BH_{\max}) of about 310 kJ/m^3 and a remanence flux density of 1.28 T at 20 °C, while the lot more temperature resistant Neorem 499a has respective values of 190 °C and 1.00 T.

1.3.2 Permanent Magnet Synchronous Motor (PMSM) types

In some references, especially from the United States, permanent magnet synchronous machines are called brushless DC motors, due to the fact that they do not have a rotating ampere-conductor distribution, which requires a sinusoidal drive, even though the stator is fed with sinusoidal phase currents (Gieras 1999).

Rotating field permanent magnet motors can be divided into categories in many different ways. The type to be used depends on the requirements of the application. If it is required space or shape or linear movement it may be decided for the axial flux or linear motor. In the exterior-rotor motor (drum motor) the rotor can be used in a conveyer to drive the belt and no external equipment is required for this purpose.

Table 1 presents four different ways of categorizing the permanent magnet motors. This division is only one example and the arguments for the selection may be different. The arguments are also typically overlapping and one special type may belong to different groups. One example for this is maybe the most common type: the surface mounted radial flux interior rotor slotted stator motor, which has an argument that may belong to each of the groups.

Table 1.1. Different permanent magnet motor categories.

Magnet mounting	Motor type	Rotor type	Stator type
Interior magnet	Radial flux	Interior-rotor	Slotted stator
Surface mounted	Axial flux	Exterior-rotor	Slotless stator
Inside rotor iron	Linear motor	Disc-rotor	
Pole shoe	Transversal flux		

Radial Flux Machine

The most typical or traditional electrical motor type is radial. In this type a cylindrical rotor rotates inside a stator tube (interior-rotor motors) or, in some cases, a tube rotor rotates around a stator (exterior-rotor motors). The motor properties, such as air-gap flux density distribution, effective amount of permanent magnet material, cogging torque are, among other factors, dependent on the magnet mounting, shape and volume. Also the manufacturing costs for the different types may differ significantly. Figure 1.6 shows some possibilities for magnet mounting.

In the interior-rotor motor, when the magnets are fixed on the rotor surface (Fig. 1.6, a and b) there is a high stress, especially in high-speed solutions, concentrated on the joint between the magnet and the rotor. Typically in such cases, the joint is assured with a special band made of light, high stress tolerable material, such as carbon fiber. When the magnets are inside the iron (Fig. 1.6, d...g) no similar solution is required. Figure 1.7 illustrates the basic principle of interior- and exterior-rotors.

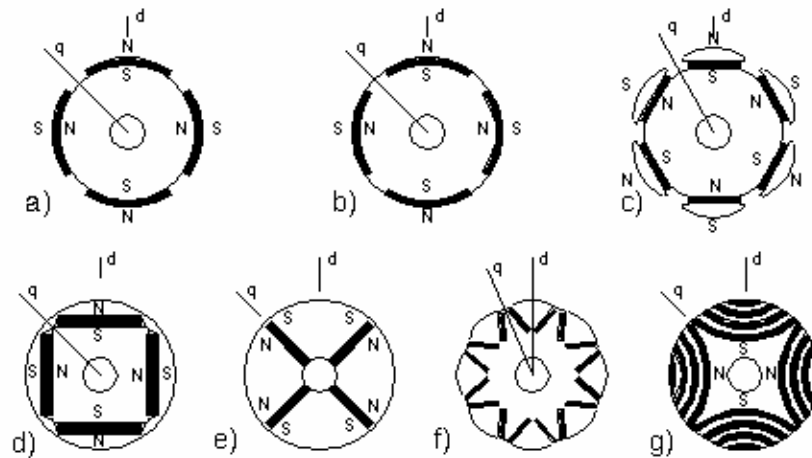


Fig. 1.6. Different magnet mounting possibilities in radial flux machines. a) surface mounted, b) interior mounted, c) pole shoe, d)...g) different magnet mounting types inside the rotor iron. (Heikkilä 2002)

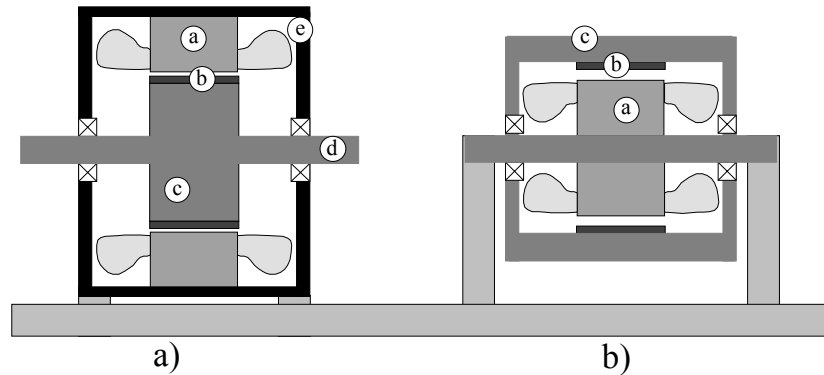


Fig. 1.7. a) Interior-rotor and b) exterior-rotor permanent magnet motor. In the exterior-rotor motor the rotor outer surface can be used for example for a belt drive or inner pole for a fan. (a) is the stator, (b) the permanent magnet, (c) the rotor iron, (d) the shaft and (e) the motor frame.

Axial Flux Machines

In some cases the axial length is limited. The axial flux machine offers in these cases the solution. Especially in slow multi-pole machines the stator and rotor yokes can be made rather thin and the coil end over hang is radial, so the limitation of the axial space can be set very low. A good example of such an application is the machine-room-less elevator, MonoSpace™, invented by KONE Corporation. The hoisting machine is situated on the top of the hoist way and fixed to the guide rail (Fig. 1.8). Typically the space required by the hoist way is kept as small as possible to limit the construction. This again means the space for the motor between the guide rail and the wall is small. The basic construction of an axial flux motor is shown in Fig. 1.9. As with the exterior-rotor motor in the case of an axial flux motor the rotor can be used directly, without special shaft, for this type of application.

Even though the axial flux PM-motor is mainly designed for low speed applications, there are also some examples of its use in high-speed applications. Sahin (2002) introduces a motor, which is designed for 16000 rpm and 30 kW applications. Even though the radius of the magnets would be small, the high stress is directed on the magnets and thus enough attention should be focused on the mechanical issues and on the fixing of the magnets.

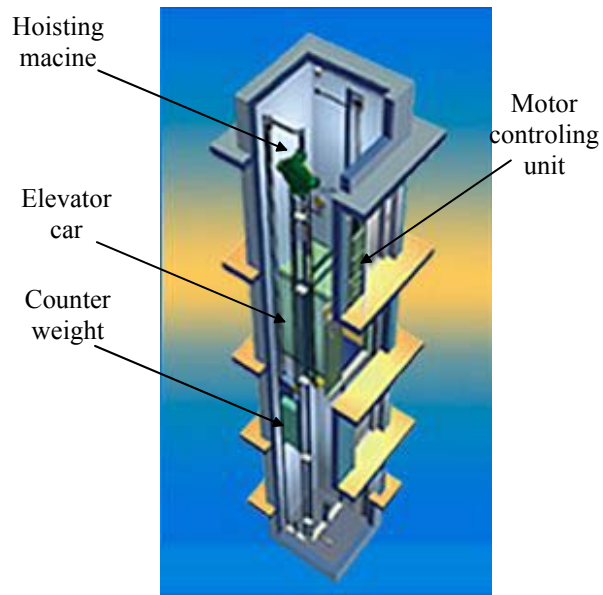


Fig. 1.8. KONE Elevators MonoSpace™ elevator concept based on the axial flux PMSM. (Kone 2003)

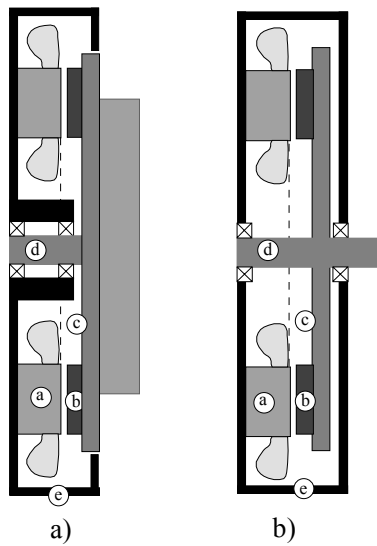


Fig. 1.9. Two axial flux motor constructions. a) is the stator, b) the permanent magnet, c) the rotor iron, d) the shaft and e) the motor frame. In version a) the rotor works also as a regulating unit, but IP-classification is limited due to sealing. In version b) sealing is easier, but the load machinery is separate.

In certain applications the axial flux motor requires less material than the radial motor does for the same operation. In their study Sitapati and Krishnan (2001), compared one radial and four axial field topologies. Their conclusion was that the axial flux motor has a higher power density compared to radial flux motor. Zhang et al. (1996) came to the same conclusion concerning the torque density, when the reference considered is the amount of active material.

Transversal Flux Machines

The transversal flux motor is actually one application of the axial flux motor. This is a solution in which the torque can be doubled without doubling the axial space by using the rotor core for both stators. Of course, the magnet thickness or volume has to be doubled, as it is shown in figure 1.10 a. According to the name, the flux goes through the rotor and thus there is no iron needed between the magnets (fig. 1.10 b). In such a case, the rotor does not have to be ferromagnetic at all. This structure type sets some requirements for the permanent magnet mounting, because the magnets cannot be bounded from their back surface. Figure 1.11 shows the flux path differences between axial flux and transversal flux motors.

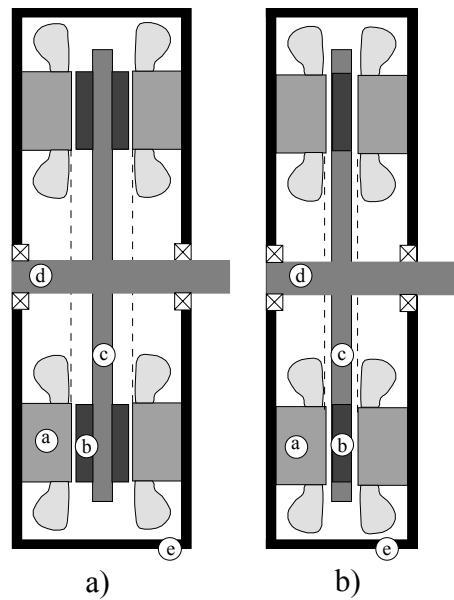


Fig. 1.10. Two different constructions of a transversal flux machine. a) with magnets on both sides of the rotor iron and b) with flux passes through the magnet and no rotor iron is needed.

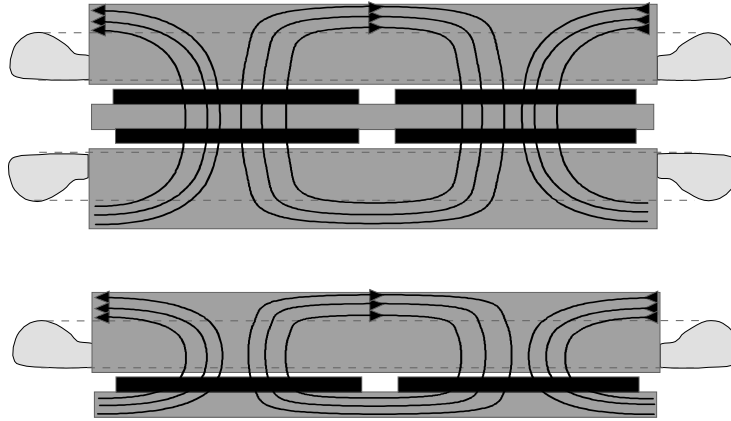


Fig. 1.11. Flux path in (four-pole) transversal flux and axial flux motors

Permanent Magnet Linear Machines

Linear motors are typically capable of performing a 1-dimensional movement. By combining several motors, the degree of movement freedom can be increased. For example, in stamping machines or in laser cutting machines the object has to be moved on a plane two-dimensionally. Other possible applications for linear motors are for example conveyers and elevators (Gieras 1999 and Hakala 1995).

Often, the applications require accuracy of movement. Both the speed and the exact place must be known. By using an encoder with a high number of pulses or a resolver it can be achieved an accuracy of even 5 μm .

In rotating motors all the active material in the flux path is always in use. Considering the linear motor, only part of the active material is being used and the other parts are not under operation. It can easily be noticed, that the longer the required movement is, the more material is needed. For this reason, the movement is typically rather short.

One problem with linear motors is, that the inactive part is open to the surroundings. For example, in the metal industry a lot of ferromagnetic dust may hover in the air. The field (leakage paths) of the permanent magnets collects this dust easily. Due to the magnetic forces

the dust cannot easily be removed. Figure 1.12 shows two possible constructions of linear motors. The leakage paths between the magnets are shown in the lower construction.

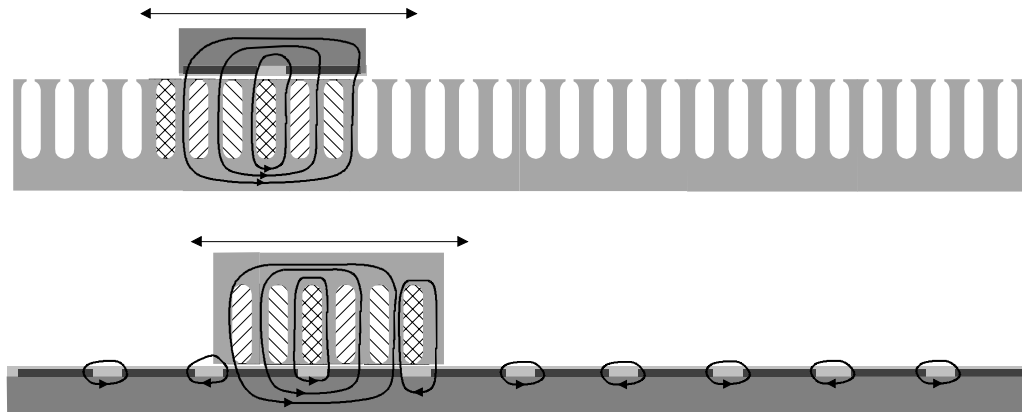


Fig. 1.12. Magnetic circuit and flux paths of the slotted iron core linear permanent magnet motor. In the upper picture the moving part is passive (permanent magnets) and in the lower picture active (phase coils). The controlled coils are marked hatched.

1.4 Frequency Converter

In addition to the motor and mechanics, also the power supply, typically a frequency converter, is a source of vibration. In many cases, the ideal supply for the motor would be a phase symmetrical sinusoidal current source, even though some times certain harmonic components may be used to compensate the properties of the motor. The increased switching frequency, faster power components and different controlling techniques have brought the frequency converters closer to the ideal current source.

Modern frequency converters use a switching frequency up to 20 kHz. In this way, the ripple amplitudes are limited low. Also the inductance of the electric circuit has a great effect on the amplitude. These frequencies are typically so high that they are not able to create any remarkable tangential vibration, but typically causes high frequency magnetostriction in lamination and thus noise.

Instead, non-homogeneous components and measurement errors may cause offset or gain differences between the phases. Current measurement offset error causes a fundamental

harmonic component and current measurement gain error causes a second order harmonic component to the torque (Chung 1998, Laurila 2002).

1.5 Outline of the Thesis

The behaviour of PM-motors has been studied widely during the latest years. Different methods of reducing the torque ripple have been developed and studied in many sources. Also calculation methods to estimate the torque and cogging have been an interesting field of study. Most of the studies are carried out with the finite element method, which gives reliable results when modelling is done carefully, but requires a lot of work and calculation recourses. Analytic methods are mainly used to calculate a certain factor in the motor model.

The critical frequencies in a mechanical system are difficult to predict. Traditionally, a prototype is built by means of which practical results can be obtained. However, to avoid the need to build expensive prototypes a project was founded to model the torque vibrations of a mechanical application including the frequency converter, motor, actuator and the control system. This study is part of that project.

The work has two objectives. 1) to create an analytical, reluctance network based and accurate enough calculation method to evaluate the instantaneous electro-magnetic torque of PMSMs with rotor surface mounted magnets. The calculation model must be applicable to the larger mechanics simulation system mentioned above 2) to minimize the output torque ripple of the prototype machine developed during the study.

Zhu et al. (1993 & 2000) have been widely referred in the area of permanent magnet motor modeling and the cogging phenomenon. They developed analytic approach to flux density created by the permanent magnets in the air-gap. Their approach is also one of the bases in this study and is one the main requirements in order to handle the torque component analytically. They also studied widely the effect of different design factors on the torque quality.

Due to the traditional structure of electric motors most of the articles handle radial flux (cylindrical) motors. Most of the effects are about equal when compared with axial flux (AF) motors, but there are also some differences. One these is the magnetization direction in radial magnets (Jahns 1996). The other difference is that in radial motor the torque is created with constant radius, when in AF motors it varies. The force created in the stator outer radius creates

higher torque than same force in the inner radius. This factor was not found in any of the used references.

Li & Slemon (1988) were among the first to study the effects of NdFeB –magnet to torque vibration in synchronous machines. As with many others their study was base on the 2-dimensional approach, which limits the possibilities in magnet, slot and teeth widths. They found optimum width for square magnet and slot/tooth width. Calculation was made with linear stator (linear motor model). While the calculation programs developed Ishikawa & Slemon (1993) continued on this basis but with cylindrical model, which also took the rotor curvature in to account. The results they got where slightly different compared with the linear model.

However, a simple, but reliable enough tool to evaluate the effect of different factors on the torque ripple was not found in the references. One limiting factor for this may be the demand of three dimensional calculations due to the structure of the motor. It is aimed at developing a calculation environment with analytical equations to solve radial and axial flux PMSMs with rotor surface mounted permanent magnets simply and fast, but still sufficiently accurately. The modelling of the motor and its different factors should be simple, but still the achieved results must be useful and reliable. The model is to be fed with the currents, required mechanical torque and speed and the output of the calculation is the torque created by the motor. If the latter differs from the torque of the actuator, the difference either accelerates or decelerates the system. Also the possibility to connect the model with other factors (power source, control circuit and mechanics) that have a great impact to the torque and vibration would make this type of model most interesting.

This difference (excitation) is generated by the non-idealities of the electric and magnetic systems. How the mechanical system will react to this depends on the frequency of the excitation and frequency response of the mechanical system.

The second chapter introduces the equations to create a calculation model for the surface mounted rotating permanent magnet motor. This model may be applied to both the radial and axial flux motor. The main interest is, however, focused in the latter, since the results may thus be compared and verified with the results achieved with the testing prototype.

The third chapter discusses different factors that affect the vibration created by the motor. These are factors that are related to material properties, geometry and asymmetry. In a brief review it is also focused on the frequency converter non-idealities.

In the fourth chapter, the analytic calculations are compared with the FEM-calculations and measured results. A conclusion of the research is given in the last chapter.

1.6 Scientific Contribution of The Work

The scientific contribution of the work can be summarized as follows:

1. Analytic equations and methods are introduced for the fast and reliable torque calculation of a surface mounted axial flux permanent magnet machine and the possibility is discussed to integrate the method as part of the total electro-mechanic system calculation.
2. A close, theoretical study is done of the effects of different factors on the torque quality.
3. A large number of measurements are performed to verify the calculation method.

Typically, the calculating of an axial flux permanent magnet machine is performed applying a 3D FEM-method, by means of which it is possible to take into account the radius and non-uniform structure of the teeth and the other electrical and magnetic parts of the machine. The calculation requires a lot of time and computer recourses. This study will prove that calculating can also be done with analytical methods progressing the following way: first, the magnet is divided into slices and the calculation is performed for each section separately, then, the parts are submitted for final results. This method offers the advantage that a lot of time in design and calculation can be saved.

The calculation method is used to study the effect of the different factors of the permanent magnet and of the other parts of the magnetic circuit on the torque quality. It is proven with different methods that combining in a suitable way the magnet shaping, magnetic circuit asymmetry and magnetic circuit dimensioning it is possible to reduce the torque ripple to fulfil the requirements of almost any electric motor application.

The measurements are carried out with a number of different permanent magnet shapes and distributions as well as with some modifications made in the stator. Also the effect of supply non-linearities is measured. These measurements are verified with different calculation methods and thus support the reliability of this method.

2 TORQUE CALCULATION MODEL

This chapter introduces the analytical equations that create the basics of the calculation model for rotating permanent magnet motors having the permanent magnet material attached on the rotor surface. The model takes into account the stator magneto motive force harmonics, the air-gap permeance harmonics and the rotor permanent magnet shapes. With some slight modifications the model can be applied to both radial and axial flux motors. However, the main interest is focused on the latter.

2.1 General

The Finite Element Method has become a common tool to design and calculate electrical motors in steady state and in transients. Even though progress in the development of computer technology and calculation programs has been rapid and computers have become faster and capable of treating a large amount of data, the accurate modelling of the motors remains still a time consuming process, especially if a three-dimensional solution is required. The increasing demand on the motor performance calls for more reliable results, more accurate models and shorter time steps in dynamic simulation. In radial flux motors two-dimensional (2D) modelling is often accurate enough, especially if the motor is long and the end effects in the motor may be ignored. As an example, in the case of slot skewing or special magnet shapes modelling must be done in axial slices in order that the geometry should be taken into consideration. Three-dimensional (3D) modelling has thus been increasingly approved, though the fact that - as it can be assumed - with the accurate 3D model calculation and modelling require really a lot of time. In axial flux machines many parameters change as a function of the rotor radius. Inherently, a pure 3D modelling or 2D modelling using several slices is required if accurate torque quality studies should be performed. The results given in chapter 4.2 confirm this statement. In some occasions the average torque of an axial flux machine may, however, be calculated using the simplified 2D model.

With an analytical model of the motor the calculation results obtained may be less accurate than those obtained with FEM, but in many cases the required results can be reached in a fractional time. Especially used as a normal design tool the analytical calculation program is very attractive. In the project of the this research the motor calculation has to be part of a whole electromechanical drive model and compatible with the calculation of the other parts. In such a case FEM cannot be applied and thus an analytical model is needed.

The calculation model is based on the magneto motive forces (mmf) created by the magnets, the stator winding and the reluctance network of the magnetic circuit. Calculation gives as a result the torque of the motor as a function of time including the torque vibrations. The motor geometry, the materials and either the torque or load angle are defined and the motor can be fed with an arbitrary shape and amplitude of three phase currents. The motor size, geometry, number of pole pairs or any other factors are not limited. The calculation steps and the number of sectors of circles (slices) of the magnet are selectable, but they do have a great impact on the calculation time. Figure 2.1 introduces a calculation model for a sinusoidal magnet shape.

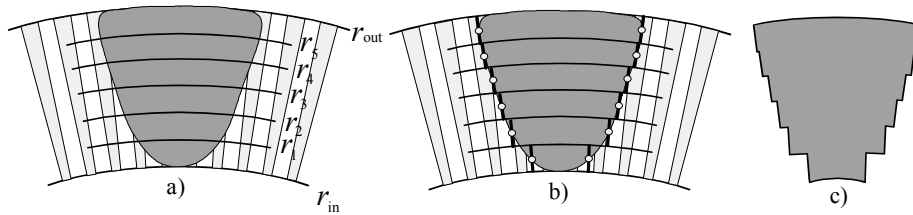


Fig. 2.1. Calculation model for a magnet with sinusoidal contour, when it is divided in six radial parts. a) is the original permanent magnet form, b) represents the slices and c) the calculation model.

The result obtained when a small number of slices is set (Fig 2.1. c) differs quite a lot from the results obtained with the original shape (fig 2.1. a). The harmonic torque calculation results with a coarse division and an arbitrary magnet shape generally do not meet the requirements (chapter 4.2). In the calculation model each slice has a tangential width, which is defined by the edge points of radius $(r_i + r_{i+1})/2$. It is easy to understand that a coarse division of the magnets may produce unexpected torque behaviour since each of the sectors of the circles has edges parallel to the stator slots.

2.2 Air-Gap Flux Created by the Permanent Magnets

A permanent magnet creates a magnetic flux in the magnetic circuit. The form and the amplitude of the flux density in the air-gap depend on the geometry and the materials of the magnetic circuit, the length of the air-gap and the magneto-motive force of the magnet. The temperature of the magnet has some effect on its mmf, but it is not considered in the calculation. If the demagnetisation curve of the used magnetic material is linear the mmf of the magnet may be defined using either the coercive force H_c of the magnet or the remanence flux density B_r of the magnet. Otherwise, the apparent coercivity H_c' of the magnet should be used.

Zhu (1993) introduced an equation to calculate the flux density created by the linear magnets on a slotless stator surface:

$$B_{pm}(\theta_2) = \sum_{n=1,3,5,\dots}^{\infty} \frac{4}{\pi} H_c \sin\left(\frac{n\pi\alpha_p}{2}\right) \frac{p}{(np)^2 - 1} \left\{ \frac{(np-1) + 2\left(\frac{R_r}{R_m}\right)^{np+1} - (np+1) + 2\left(\frac{R_r}{R_m}\right)^{2np}}{\frac{\mu_r + 1}{\mu_r} \left[1 - \left(\frac{R_r}{R_s}\right)^{2np}\right] - \frac{\mu_r - 1}{\mu_r} \left[\left(\frac{R_m}{R_s}\right)^{2np} - \left(\frac{R_m}{R_s}\right)^{2np}\right]} \right\} \left[\left(\frac{r}{R_s}\right)^{np-1} \left(\frac{R_m}{R_s}\right)^{np+1} + \left(\frac{R_m}{r}\right)^{np+1} \right] \cos(np\theta_2) \quad (2.1)$$

H_c is the coersivity of the permanent magnet, R_x is the radius of the rotor (r), stator (s) or magnet (m), μ_r the permeability of the magnet, α_p the relative width of the magnet versus the pole pitch, p the number of pole pairs and θ_2 the angular position. When applying this equation to the axial flux motor the parameters R_m , R_s and R_r must be calculated using the average radius of the stator or the average radius of a slice, air-gap length (δ_{ag}) and magnet height (h_{pm}).

Chung and Gweon (2002) developed a method for the permanent magnet linear motor to calculate the air-gap flux density created by the permanent magnets. The method is based on the same Fourier series equation as Zhu's method, but treats the air-gap a bit differently

$$B_{pm} = \sum_{n=1,3,5,\dots}^{\infty} \frac{\frac{8B_r}{n\pi} \sin\left(\frac{n\pi\alpha_p}{2}\right)}{\left(e^{\frac{-2n\pi\delta}{\tau_p}} + 1 \right) + \frac{\mu_m \left(-e^{\frac{-2n\pi\delta}{\tau_p}} + 1 \right) \left(e^{\frac{2n\pi h_{pm}}{\tau_p}} + 1 \right)}{\mu_0 \left(e^{\frac{2n\pi h_{pm}}{\tau_p}} - 1 \right)}} e^{\frac{-n\pi\delta}{\tau_s}} \cos\left(\frac{n\pi x}{\tau_p}\right), \quad (2.2)$$

where B_r is the permanent magnet remanence flux density and τ_p the pole pitch. Both equations (2.1 and 2.2) give the flux density distribution on a smooth stator surface. The stator slotting effect is usually taken into account by using the Carter factor. Chung and Gweon (2001) apply the following equation, which seems to give good results compared to the results given by FEM for the test motor

$$k_c = \left[1 - \frac{w_{so}}{\tau_s} + \frac{4g'}{\pi\tau_s} \ln \left(1 + \frac{\pi w_{so}}{4g'} \right) \right], \quad (2.3)$$

where τ_s is the slot pitch, w_{so} the width of the slot opening and g' the total air-gap length.

However, in this case, it is not sufficient to use only the Cater factor; the permeance function of the air gap region is required. Several sources discuss different methods to calculate the permeance function k_Λ . Heller and Hamata (1977) present different equations, depending on the air-gap length, slot and slot opening parameters. The following equation introduced by Weber (1928) is one of the most appropriate equations referred to by Heller and Hamata. The air-gap flux density along a slot pitch is modified by the permeance function

$$B(\alpha) = k_\Lambda B_{\max} = \left(1 - 2\beta \sin^{2n} \frac{\pi}{\alpha_d} \alpha \right) B_{\max}, \quad (2.4)$$

where

$$n = \frac{\tau_s - w_{so}}{w_{so}}. \quad (2.5)$$

β is a function of w_{so}/δ and α_d is the angle corresponding to slot pitch. The depth of the drop in the flux density under the slot opening depends on the distance to the stator surface, where the distribution is calculated.

Figure 2.2 shows an example of the flux density created by the magnets in the air-gap. Because the amount of flux is considered to be constant, the maximum flux densities are a bit higher with slotted stator than the flux densities without slotting, ie. the average of the positive and negative part of the waves in both curves are equal.

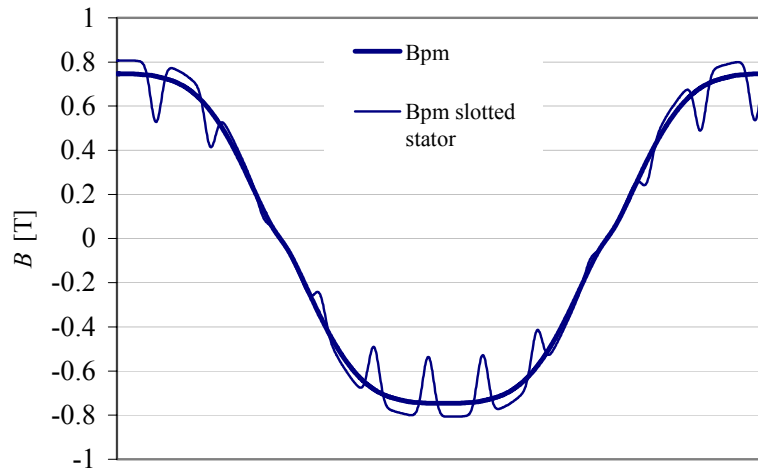


Fig. 2.2. Air-gap flux density along one pole pair area created by the permanent magnet, with and without slotting

To compare the applicability of eqns. 2.1 and 2.2 an example was calculated applying both methods (Fig 2.4) and compared to the 3D FEM calculation of the same model (Fig 2.3).

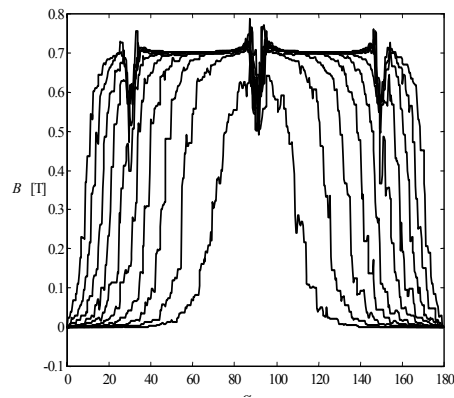


Fig. 2.3. Air-gap flux density in an axial flux motor created by a magnet with sinusoidal contour. FEM-calculation.

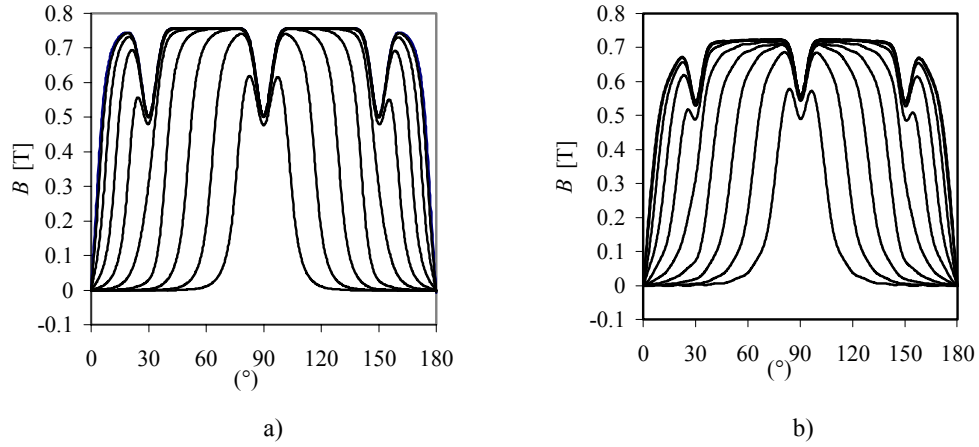


Fig. 2.4. Air-gap flux density in an axial flux motor created by a magnet with sinusoidal contour calculated with a) the linear motor model (Chung 2002) and b) the radial motor model (Zhu 1993).

The results calculated with eqns. 2.1 and 2.2 are closely corresponding to each other, but Chung's version is a little bit simpler and fits better for the axial motor, due to the parameters used. Compared to the FEM calculation Chung's calculation model also seems to give closer results, especially near the edge areas of the magnets (widest curves at about 10° and 170°).

In both equations the number of harmonics to be used is an important parameter. A comparison of figures 2.5 and 2.4 a) illustrates the difference in the results obtained with 10 and 100 harmonics. The effect of missing Fourier's components is indicated as waves in figure 2.5. Increasing the number from 100 does not significantly influence the results anymore.

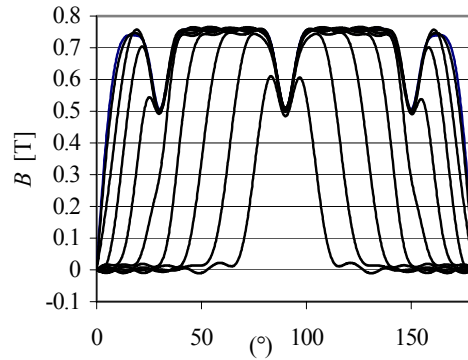


Fig. 2.5. Air-gap flux density in the axial flux motor created by a sinusoidal magnet calculated with the linear motor model (10 harmonic components).

The calculation is simple and fast if the shape of the magnet is a square and has no skew related to the stator slots. When the shape of the magnets is more complicated the calculation has to be done in several slices. The bigger the amount of slices the more accurate is the result. A coarse division of the sector into slices may cause unexpected torque vibrations since the width of an individual slice may appear to be seriously disadvantageous with reference to the pole pitch or slot pitch.

2.3 Magnetic Circuit

The magnetic circuit of the motor, consisting of the stator iron, rotor iron, air-gap, magnet and slot, is modelled in the model developed with a reluctance network, which takes the saturation of the iron into account. This means that several iteration circles, in which the permeability in individual regions is updated, should be performed in order to get reliable results. Figure 2.6 shows the network of the area of six slots.

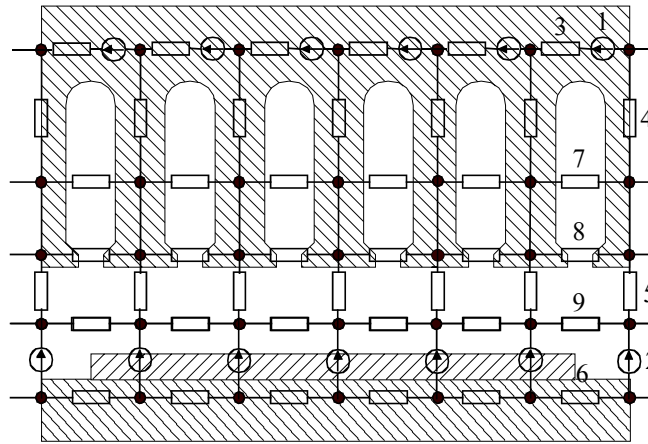


Fig. 2.6. The reluctance network of one pole area. The components in the figure are: 1 mmf of the winding in the slot, 2 mmf of the rotor (magnet), the reluctance of the 3. stator yoke, 4. stator tooth, 5. air-gap, 6. rotor yoke, 7. stator slot, 8. stator slot opening and 9. tangential leakage reluctance in the air-gap

The reluctance network is, in this case, the simplest possible to model the magnetic circuit. Adding the nodes and reluctance components increases the reluctance matrix rapidly and the benefits obtained by this seem to be insignificant considering the increasing calculation time. Compared to FEM (chapter 4.2.1) even with a huge increase of calculation time the method is competitive. It should be kept in mind that one of the objectives aimed at was for the procedure

to be part of system calculation. In such a case, it is not appropriate to enlarge the matrix sizes and increase the calculation time. Also the results given in chapter four prove this simple network to be accurate. The calculation procedure itself does not limit the network size.

In case of an integer slot winding the total calculation model is made for one pole pair of the machine, and this one pole pair module is connected from both ends to each other to take the flux passing edge of the model in to consideration. This means that the model analyses the machine calculating just one pole pair. However, this is not enough in the case of a fractional slot winding or in cases in which non-uniformity in the magnet positions or magnet sizes is included. In these cases several pole pairs must be calculated. The total torque is reached by multiplying the torque of the calculated area with the number of similar areas.

The main route of the flux goes along the stator yoke, the teeth, the air-gap and the rotor yoke. The BH -curve of the magnetic material is defined, and the values of the reluctances are calculated depending on the saturation of the magnetic circuit components. The permeability of air is constant, and the air-gap reluctance as well as the leakage reluctances are thus kept constant.

According to the calculations made with this procedure, the tangential leakage reluctance has a very small effect on the calculation results, but it adds one calculation circuit in each tooth area. When calculating asymmetric cases as e.g. an additional slot in the stator (described closer in chapter 3), a model of the whole motor including all pole pairs is needed. If in such asymmetric cases this component is neglected the size of the matrixes and calculation time will be considerably reduced. The flux ϕ in each circuit is solved by

$$[\phi] = [R]^{-1} [NI], \quad (2.6)$$

where $[R]$ is the reluctance matrix and $[NI]$ is mmf matrix.

Reluctance networks have been successfully used also with other types of electrical motors. Perho (2002) presented a method to calculate induction motors with the reluctance model. However, Perho defines the circuit using an amount of elements that is much larger compared to the model introduced in this work. Figure 2.7 shows the reluctance model of one slot and tooth area as it is described Perho's work.

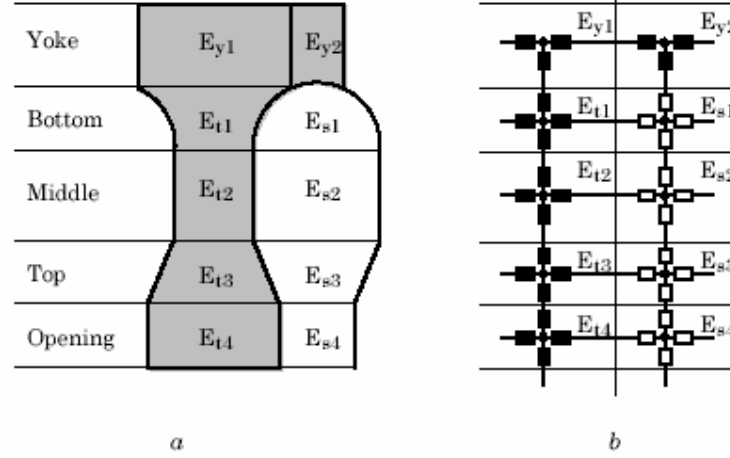


Fig. 2.7. The reluctance network described by Perho (2002) of one tooth and slot area.

To describe one slot pitch in the stator 47 reluctance components and 8 circuits are needed, when in the simpler model (Fig. 2.6) only five components and two circuits are used. In Perho's model the air-gap is modelled using a higher number of components compared to the model presented in this work. This brings a better accuracy, but also a lot more calculation resources. In practice, increasing the amount of reluctance network components improves the calculation accuracy gradually and, finally, using either FEM or reluctance networks give results and a computational time that are in the same range.

Roissee and Brochet (1996) described a coupled permeance network for the magnetic path, which is close to the reluctance net shown in figure 2.6. Their approach is based on the mmf's created by the linear current density and the magnets. The permeance components are calculated with 2D FEM, which makes the procedure more complex. Also parameter variance, like iron path permeability, in different loading conditions is not considered. Their results are compared to measured results, nevertheless, promising, which supports the usage of a reluctance net.

2.4 Torque Calculation

There are different possibilities of calculating the torque created by the motor, based on the currents and flux. This chapter discusses one applicable method, which is based on the Lorentz force

$$d\vec{F} = dQ(\vec{E} + \vec{v} \times \vec{B}), \quad (2.7)$$

In practice, the sum of the tangential components created by the electric field strength (\vec{E}) is zero and, thus, does not create any torque. This is due to the fact that the electrical field around the slot is equal to the opposite directions thus compensating each other. Here, only the last component in bracket part of equation 2.7 is considered.

$$d\vec{F} = dQ(\vec{v} \times \vec{B}) = dI(d\vec{l} \times \vec{B}) \quad (2.8)$$

The Maxwell stress tensor is also often used in the torque calculation. In practice, the Maxwell stress tensor may be calculated only by using FEM. The normal and tangential components of the air gap flux density must be accurately known. Even though an accurate element network in the air-gap region of the FEM calculation is used applying the Maxwell stress method may produce an error in calculation of the torque. For this reason this method is often replaced by other methods even when using FEM. Belmans (1990) suggests that the rotor loss calculation based torque calculation should be used for induction machines instead of the Maxwell stress method. For the PMSM, however, the rotor loss method is not applicable. In this study considering an air gap flux density solution that is not at all accurate enough, the Maxwell stress method cannot be applied. However, the Lorentz force based methods seem to give satisfactory results.

2.4.1 Flux Linkage

The linear current density is somewhat imaginary and thus, considering the harmonic components, depends on the presentation. In case no harmonic calculation is needed, the instantaneous linkage flux may be used, which would be a more substantive approach. The part of the flux that is created by the permanent magnets and the stator currents and passes through the coils in the stator teeth is called the flux linkage. When using the space vector approach the angle between the flux linkage and the stator current vector defines the torque created by the magnetic circuit. In a three-phase machine the torque is (Kovacs, Racz 1954)

$$T_e = \frac{3}{2} p \psi_s \times i_s. \quad (2.9)$$

The stator flux linkage vector and the current vector are defined using the phase values as

$$\psi_s(t) = \frac{2}{3} \left(\Psi_a(t)e^{j0} + \Psi_b(t)e^{j\frac{2\pi}{3}} + \Psi_c(t)e^{j\frac{4\pi}{3}} \right), \quad (2.10)$$

$$i_s(t) = \frac{2}{3} \left(i_a(t)e^{j0} + i_b(t)e^{j\frac{2\pi}{3}} + i_c(t)e^{j\frac{4\pi}{3}} \right). \quad (2.11)$$

The torque vector in Eqn. 2.9 may contain time harmonic components created by the current harmonics. However, in this case the vector presentation is not applicable since it does not take the machine non-idealities into account. Instead, in order that the motor space harmonics can be taken into account in the torque production the instantaneous component values must be used and thus the torque may be expressed as:

$$T_e(t) = \sum_{n=1}^{n_c} p \varphi_n(t) N i_n(t), \quad (2.12)$$

where $N i_n$ is the total current of each individual coil, φ_n is the peak value of flux linkage and n_c is the number of coils. This expression will be used in the machine modelling done in this work hereafter.

In the reluctance net model the flux in each part of the magnetic circuit is known. This means that also the flux linkage in each of the teeth as well as the current in each of the coils is known in every time step. Now, when numerically calculating the product, it is not necessary to know the angles between the components, but instead the branch fluxes and the currents in the coils around them are used. Figure 2.8 shows part of the stator in a three-phase motor, the phase coils of one phase and the flux in the teeth. For example, in one of the coils fluxes 2...6 create the flux linkage.

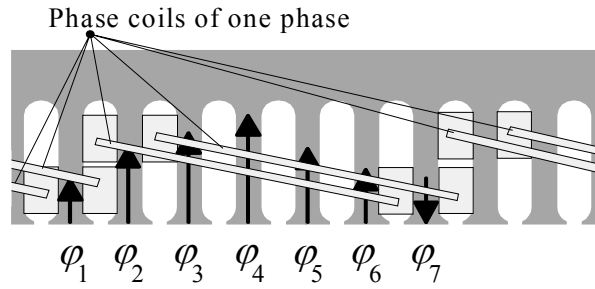


Fig. 2.8. The flux linkage and phase coils of one phase in $5/6$ coil span $q = 2$ stator. The fluxes 2...6 pass through one of the coils and fluxes 3...7 through another.

This enables the development of another, Lorentz force based calculation method to calculate the torque. In practice, part of the flux goes through the coil window, producing the linkage only with part of the turns in the coil. In case the accuracy is high or coil window is narrow the slot area should be divided in several reluctance components. The more components are used, the closer the solution achieved corresponds the finite element method and more calculation resources and time are needed.

2.5 Cogging Torque

Due to the winding structure of the stator and in order to limit the leakage flux the slot openings of the stator are normally not made of ferromagnetic material, even though in some cases semi-magnetic slot wedges are used. Because of the permeability difference in the slot opening the flux enters the iron creating normally (depending on the shape of the opening and the saturation of the teeth) tangential forces in the rotor (Fig 2.9). The fluctuation in the permeance is called cogging. Typically, the slot opening is the most dominating factor in the fluctuation. The latter, however, may be affected also by other factors like iron path saturation.

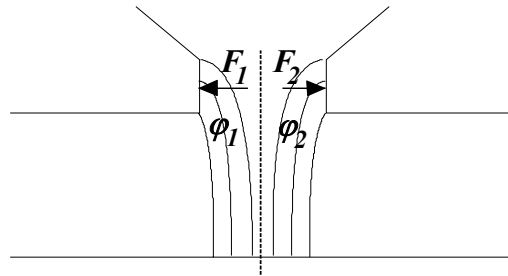


Fig. 2.9. The air-gap flux components under the slot opening that create the cogging torque.

The flux in the slot opening area on different sides of the opening and in different slot openings is typically not equal and thus these forces do not compensate each other. In the calculation it is assumed that the flux entering the left side of the opening is the component left from the geometrical centre of the slot according to figure 2.9. The calculated total instantaneous torque of the motor is the sum of the flux linkage and permeance fluctuation components.

Proca et al. (1999) presented a similar approach to the radial flux motor based on the force caused by the flux entering the slot opening sides. Their equation is rather complex compared to the method presented above

$$T_{\text{cog}}(\theta) = \frac{\pi L_{\text{sc}} R_s}{2\mu_0 N} \sum \left[B_{\text{PM}}^2 \left(\frac{2\pi}{N} m + \theta \right) (R_M + g_a) \text{ssg} \right], \quad (2.13)$$

where $g_a = 0$ and $\text{ssg} = 0$ outside the slot opening, $g_a = w_1 + \delta_{\text{ag}}$ and $\text{ssg} = 1$ on the left side of the slot opening and $g_a = w_2 + \delta_{\text{ag}}$ and $\text{ssg} = 1$ on the right side of the slot opening. w_1 and w_2 are distances from the calculation point to the slot opening edge. The result based on this equation and Zhu's (1993) B_{PM} -model (eqn. 2.1) are close to FEM-calculations.

The general method to calculate the torque ripple is based on the rate of change with the angular position θ of the co-energy W' in the air-gap (Li 1988)

$$T = \frac{dW'}{d\theta}, \quad (2.14)$$

where

$$dW' = \int \frac{B_\theta^2}{2\mu_0} dV. \quad (2.15)$$

This method requires an accurate modelling of the air-gap and, in practice, a dividing of the air-gap in to finite elements. When a precise model is used this method unquestionably gives more accurate results than the analytical calculation. However, for example in the case of an axial flux motor it should be decided for the 3D method.

2.6 Radial Flux and Axial Flux Motor Calculation

In a radial type motor all sections of the magnets have the same peripheral velocity with respect to the stator windings and create force with the same radius. If the magnet has a constant tangential width and thickness, the flux densities created by each section of the magnet can be combined and the torque can be calculated using only one flux density curve. However, if the magnets are skewed compared to the stator slots, the same air-gap flux density curve may be used, but each section has a different phase angle compared to the stator field and calculation must be carried out in several sections. If the slightest changes in the torque quality should be studied the amount of slices appears to be a crucial factor since this defines the quality of the calculation. The amount of circle ring sector slices needed should be found iteratively. The amount of slices is set large enough when further increasing of the number of slices does not improve anymore the result.

For the axial flux motor the torque calculation should be done in sections independent of the magnet shape or skewing, because each radial section creates a force with different radius and the torque is the sum of the sections. In axial and linear motors normally at least one side of the permanent magnets is plane and magnetization throughout the magnet is parallel. In radial motors magnetization may be also radial. This affects the air-gap flux density created by the magnets. The type of magnetization can be used to affect the motor properties. Parallel magnetization directs the flux towards the centre, making the flux density more sinusoidal, whereas radial magnetization keeps the flux density more constant (trapezoidal) (Jahns 1996, Sebastian 1996).

2.7 Calculation Procedure

Calculation starts with the definition of the motor geometry, the material properties and calculation parameters. A selected number of radial slices defines the magnet. Each slice is described with a pair of numbers. The first number indicates the relative width of the slice compared to the width of the pole and the second indicates the distance from the centre of the slice to the middle of the pole. This representation enables to define any shape of the magnet in a simple but effective way. The only limitations that must be taken into consideration are that the magnets should be of equal thickness (height) and that their relative length should not be greater than unity. The stator and rotor iron materials are described with their specific BH -curves. These curves are set up in separate files, and their number is not limited. The calculation parameters required are given in table 2.1. The winding is defined with the turns N_s , the number

of slots per phase per pole q and the winding type when $q = 2$ ($w/\tau_p = 1$ or $w/\tau_p = 5/6$). The algorithm does not limit additional variations of the winding type. These variations may be applied using additional parts in the program.

Table 2.1 The calculation parameters

The name of the parameter	Symbol	Unit
The number of slots	Q	
The number of turns in one slot	N_s	
Slots per pole per phase	q	
Local winding pitch	w	m
Nr of pole pairs	p	
Local pole pitch	τ_p	m
Average air-gap radius	r_{ag}	mm
Air-gap length	δ_{ag}	mm
Magnet thickness	h_{pm}	mm
Stator core length	L_{sc}	mm
Slot opening width	w_{so}	mm
Slot opening height	h_{so}	mm
Slot width	w_{sl}	mm
Tooth height	h_{to}	mm
Permanent magnet remanence flux density	B_{pm}	T
Permanent magnet relative permeability	μ_{pm}	

The calculation algorithm is presented in Appendix A. The program is developed to calculate cases having a constant speed and current, but the same equations and the same algorithm may be applied also to dynamic cases such as acceleration or a torque step. In the basic calculation a constant sinusoidal three-phase current RMS value and a load angle are given. The rotor rotates with constant speed together with the stator field. The program offers the option to use constant shaft torque and inertia, when the speed is not constant. In the program a constant current is given as a boundary condition, but with the developed algorithm the current shape can be

arbitrary, asymmetric or the motor may be fed alternatively with a voltage source. In the latter case only the addition of a motor equivalent circuit is required.

The program is developed using the graphical programming language called LabView™. The user interface of the program is illustrated in figure 2.10.

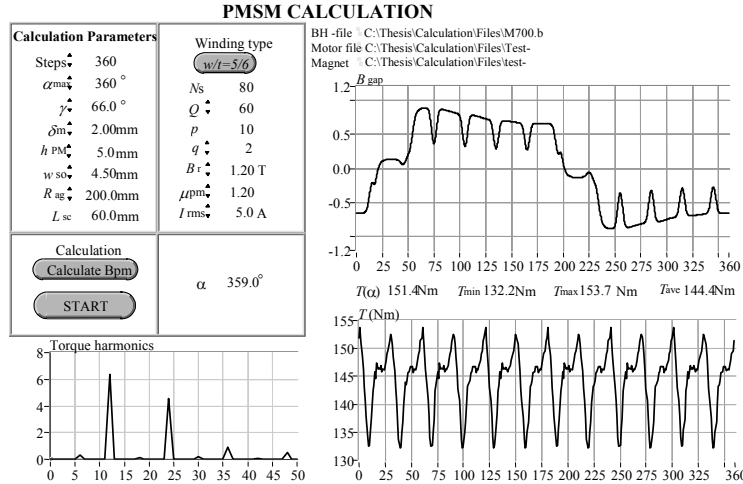


Fig. 2.10. Main view of the calculation program. The calculation parameters are defined in the upper left table. The calculation results T (Nm) and the torque harmonics are represented in the two figures below. The upper right figure represents the air gap flux density in a pole pair area during the calculation.

Also a Matlab™ version of the calculation is made, which enables a combined simulation with the mechanics and the frequency converter. Calculation gives as a result the torque of the motor with defined calculation steps and torque harmonics. For the harmonic calculation the wave length of the fundamental is assumed to be the whole calculation period.

The calculation algorithm also enables the magnets to be set asymmetric. This is done by varying the permanent magnet flux density wave position angularly with the asymmetry rate in each calculation step, as many times as there are magnets or groups of magnets in different positions. This procedure reduces the calculation time since it is unnecessary to calculate the whole magnetic circuit in multi pole machines. The affect and the nature of the asymmetry are discussed in chapter 3.

Additionally, and as a distinctive characteristic, the algorithm provides the possibility of calculating fractional slot windings, e.g. using additional slots or abnormal slot pitches in the

stator. This is also explained in chapter 3. Here, the stator field is asymmetric between the poles, which means that, instead of one pole pair, the whole motor must be modelled and calculated.

2.8 Conclusions

An analytical model for the axial flux permanent magnet motor was developed. The model divides the calculation of an axial flux machine in several radial circles and may thus be used to accurately calculate the torque ripple behaviour of axial-flux permanent magnet synchronous machines. Comparison of the results with the results given by FEM proves that analytical methods may be applied to calculate the air-gap flux density created by the permanent magnets. In the numerical calculation the Lorentz Force based flux linkage method is proven to be the most suitable method since it gives fast reliable results. The calculation allows easy parameter definition and also consideration of certain non-linearities and asymmetries.

3 Torque Vibration

The torque vibration of an electric machine is the sum of different excitations created by multiple sources. Besides the machine itself also the power source may generate a torque ripple. The current shape, especially in frequency converter drives, often differs to some degree from the sinusoidal, which inevitably creates a torque ripple in machines developed for sinusoidal supply. Another source of excitation may be the mechanics. These, however, also amplify (and dampen) the frequencies differently. This chapter studies the influence of different machine components on the torque quality. The forming and the placement of the permanent magnets, the magnetic circuit dimensions, the winding arrangements and different types of asymmetry are discussed.

Vibration excitations are caused by the power supply, the structure of the electrical circuit (winding arrangements and physical asymmetry of the assembly), the mechanical structure of the magnetic circuit, possible eccentricity and etc. In principle, in an electric machine electro-magnetic torque pulsations are generated by two different effects: 1) Stator and rotor mmf harmonic interactions and 2) reluctance discontinuities in the whole magnetic circuit.

The stator harmonic mmfs reach a practical minimum when the number of slots per phase and pole q is as large as feasible and when $w/\tau_p = 5/6$ short pitch windings are used (Vogt 1983). However, in a multi-pole machine there is often no space to increase the value of q and thus the designer has to apply slot numbers per pole and phase near to 1 and 2. In some recent articles fractional slot windings with $q = 0.25$, $q = 0.4$ and $q = 0.5$ are reported (Koch 2002). When above-mentioned values for the fractional slot winding are applied the torque producing tangential electro-magnetic stress reaches very high values, as high as e.g. 58 kN/m^2 .

In a PMSM the thickness variation of the magnets along the pole pitch or the contour shape of uniform thickness permanent magnets may be selected purely sinusoidal which, in principle, eliminates all torque vibrations generated by the stator and rotor mmfs (Pyrhönen, 1999). Using a smooth rotor steel core surface guarantees that no harmonic reluctance torques can possibly be generated in interaction between the stator harmonics and rotor reluctance variations.

Although the sinusoidal form of the permanent magnets produces also a low cogging, there is, however, no guarantee that it will give the minimum cogging torque. Different measures are needed for the cogging torque than for the stator generated harmonic torques. The intersection

point of the permanent magnet edge curve and the stator slot opening should move at a constant speed and when a magnet has totally passed the slot opening the edge of another magnet should take over in order that the process could continue smoothly.

Even though the amplitude of each component would stay constant, the result in the torque vibration depends on the frequency response of the mechanical structure. Typically, the structure may include one or more of the following components: the motor (especially rotor), shaft, clutches, gearbox and the regulating unit. The more complex is the structure, the bigger number of rated eigen-frequencies can be found, and the more likely vibration problems may occur. It has to be noticed, that in the case of a gearbox, also the frequency of the excitations is changed according to the gear ratio.

3.1 Calculation Parameters

There are several different factors that influence the torque vibration of an electric motor. To optimise the motor structure, many of these factors should be analysed in calculations based on the analytical equations introduced in chapter two. The example calculations in this chapter are performed with an axial flux motor having the basic parameters given in table 3.1. These parameters are kept constant and the changes made concern the winding, permanent magnet material properties and geometrical details. Also the effects of different asymmetry parameters are considered. Some of these factors are dealt with in the test motor measurements and in corresponding calculations and they are discussed in chapter four,. Unless otherwise stated the calculations are carried out with a permanent magnet form, which has radial edges that are parallel to the slots (fig. 3.1). This shape is most responsive to cogging and thus the effects of the changes are easier to determine.

Table 3.1. Motor rated parameters and magnet properties for calculations.

Motor parameter	
Motor rated power (P_n)	8.0 kW
Motor rated voltage (U_n)	400 V
Motor rated current (I_n)	17 A
Rated supply frequency (f_s)	18 Hz
Number of slots (Q_s)	120
Number of pole pairs (p)	10
Permanent magnets:	
- Material	NdFeB
- Remanence flux density	1.15 T
- Relative permeability	1.2
Stator dimensions:	
- Outer diameter	600 mm
- Inner diameter	450 mm

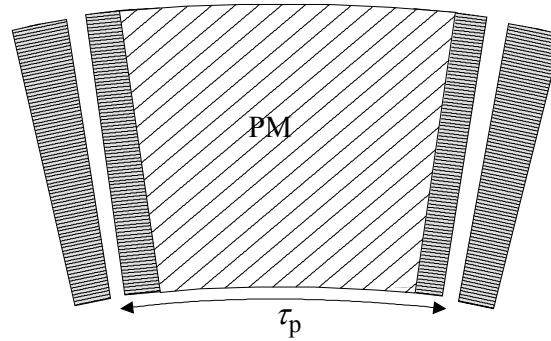


Fig. 3.1. Permanent magnet with edges parallel with the stator slots. This magnet shape is used in the calculations, unless otherwise stated, and is called Sector of a ring, SOR.

3.2 Stator

Depending on their origin, the torque harmonics of an electric motor are divided in two groups: permeance harmonics and winding harmonics. Both of these can be affected by means of the stator design. The stator basically consists of two main components: the magnetic path (typically iron) and the winding. The basic structure of a radial slotted axial flux motor in the area of one pole is shown in Figure 3.2

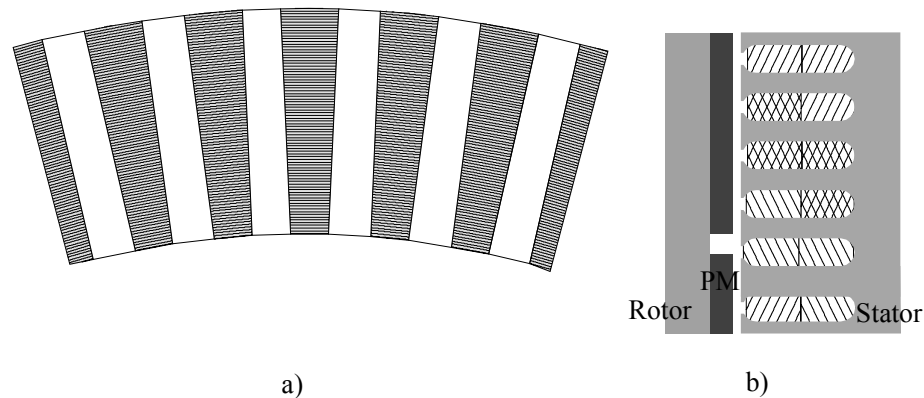


Fig. 3.2. a) Part of the stator of an axial flux motor, b) cross-section of one pole area of the calculation model ($q = 2$, $m = 3$, $w/\tau_p = 5/6$). The different shadings indicate the different phases.

With regard to from the torque harmonic the critical parameters of the stator are:

- Slotting
- Number of slots (Q_s)
- Slot opening width (w_{so})
- Slot opening and tooth shape
- Winding
- Slots per pole and phase (q)
- Type (w/τ_p)
- Phase symmetry (resistance and inductance)
- Magnetic circuit dimensioning (saturation)

In the next chapters, variations of the above-mentioned factors are tested in order to determine the possible effects.

3.2.1 Slotting and slot opening

Typically, electric motor stators are made of slotted laminated steel. The conductors are placed in isolated slots, which, generally, are either magnetically open or semi closed (fig. 3.3 a and b). In figure 3.3 c) the slot opening is closed with a semi-magnetic wedge.

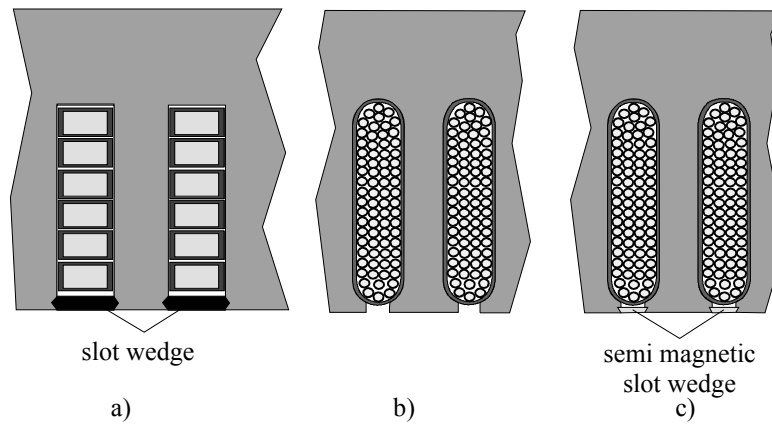


Fig. 3.3. Different slotted stator structures. a) Magnetically open slots closed with either non-magnetic or semi-magnetic slot wedges to keep the conductors in the slots, b) Semi-closed slot openings and c) semi-closed slot openings with semi-magnetic slot wedges.

The effect of the stator slotting on the rotor surface flux density distribution may be described using a permeance function. The harmonic content of this function is varying according to the slot opening dimensions. The flux density distribution under a slot opening may be predicted by Weber's equation (2.4)

Some methods enable reducing of the amount of harmonics in the permeance function. Fig. 3.4 illustrates the plots of flux lines in the vicinities of two different types of semi-closed slot openings. The figures show that there exist, in fact, methods of eliminating the effects of the permeance variations caused by the slot openings (Pyrhönen, Kurrnen 1993).

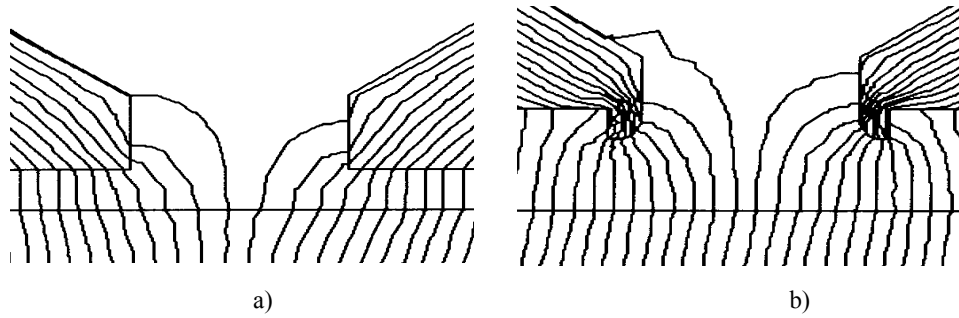


Fig. 3.4. Flux plot in the vicinity of a) the traditional and b) modified stator slot area. The flux density on the rotor surface using modified slot opening seems to be very smooth, compared to the flux density of the traditional stator slot area.

Fig. 3.4 a) illustrates clearly that in an ordinary semi-closed stator slot (the magnetic flux density on the rotor surface under the stator slot opening is smaller than under the teeth. Figure 3.4 b) shows a special type of slot opening to guide the flux in the slot opening area (Pyrhönen, Kurronen 1993). This modified type is, however, usually not utilized because it is considerably more difficult to manufacture than the ordinary slot opening. For this reason, the slot opening producing permeance harmonics should be considered satisfying. The flux density distribution under the slot opening may be determined by using the Weber equation (2.4). The resulting stator slot opening form and the corresponding rotor surface flux density distributions are shown in Fig. 3.5.

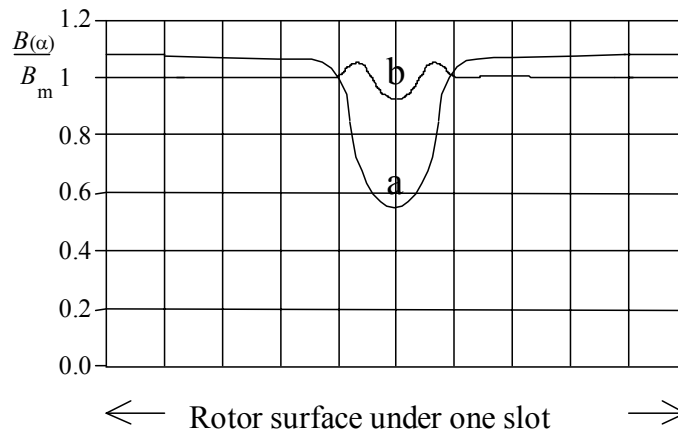


Fig. 3.5. Flux density variation on the rotor surface under one slot pitch, when no current runs in the slot. a) normal semi-closed slot opening (Fig. 3.4 a), b) modified slot opening (Fig. 3.4 b).

It may also be used some semi-magnetic material to close the stator slot openings, which is an alternative method to smooth the permeance function and thus reduce the harmful effects of the permeance harmonics (fig. 3.3 c). The flux density variation is given in Fig. 3.6.

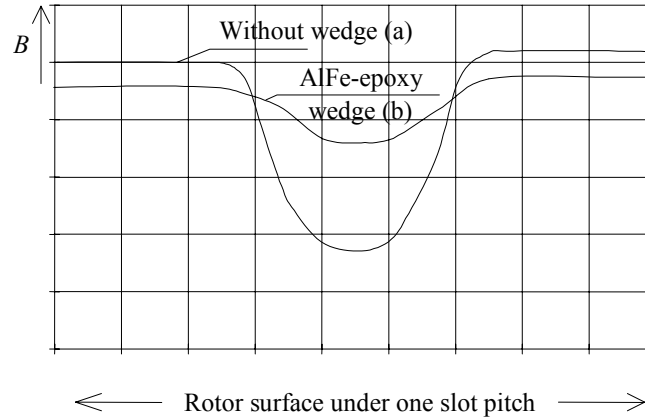


Fig. 3.6. Flux density variation on the rotor surface under one slot pitch, when a small current runs in the slot. a) normal semi-closed stator slot opening , b) slot opening equipped with a semi-magnetic slot wedge with a relative permeability of $\mu_r = 10$ In the figure the same flux is maintained and that is why the flux density under the teeth is higher in the case where no wedges are used.

Both the modified slot opening shape and semi-closed slot opening have a considerable effect on the drop-depth of the flux density on the rotor surface. The modified slot opening shown in Fig. 3.4 b has been successfully tested in solid-rotor induction motors for the reducing of harmonic losses on the rotor surface.

The ultimate way to avoid slot ripple frequency is the total removing of the slots. In applications of this type the conductors are mounted with some fixative in the air-gap on the stator yoke surface (fig. 3.7 a) or the stator iron is totally removed (fig. 3.7 b).

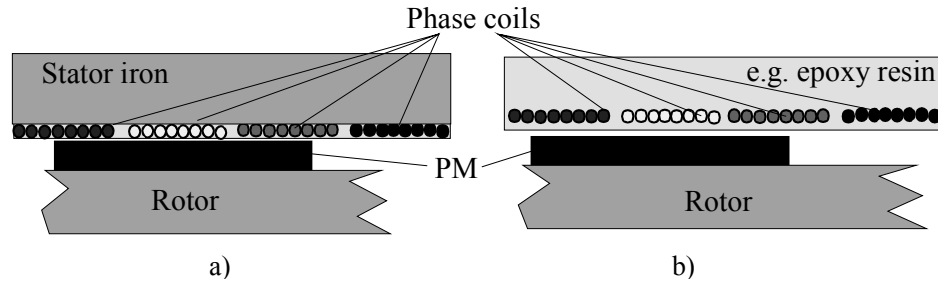


Fig. 3.7. Slot-less stator structures. a) Conductors mounted on stator iron and b) ironless stator.

The disadvantage of slot-less applications appears to be the growth of the physical air-gap, which again causes an increasing of the magnetising reactance. When the windings are fixed on the stator surface, it should be considered that the space for the conductors is rather limited due to the air-gap length (iron to iron). Also special attention should be paid to the fixing and isolating of the coils, which must be done reliably. Nevertheless, compared to the slotted solution the slot-less application offers, in theory, almost unlimited possibilities to form the stator mmf shape. Unfortunately, another effect of the slot-less structure is that, due to the long air-gap length, the air-gap flux density is significantly reduced from the normal values of normal and low-speed machines. Therefore, the slot-less solution may be used only in very high high-speed machines, which normally have very low air gap flux density levels.

With high supply frequencies the stator iron losses due to eddy currents may grow considerably. In such a case, the ironless stator may be an interesting solution, but some of the motor properties are nevertheless lost due to high leakage flux and reluctances in the stator.

In addition to the slot opening shape also the slot opening width is an important factor influencing the flux density drop under the slot opening and has thus a significant effect on cogging. The reference motor was calculated with different slot opening widths and the results are given in figure 3.8.

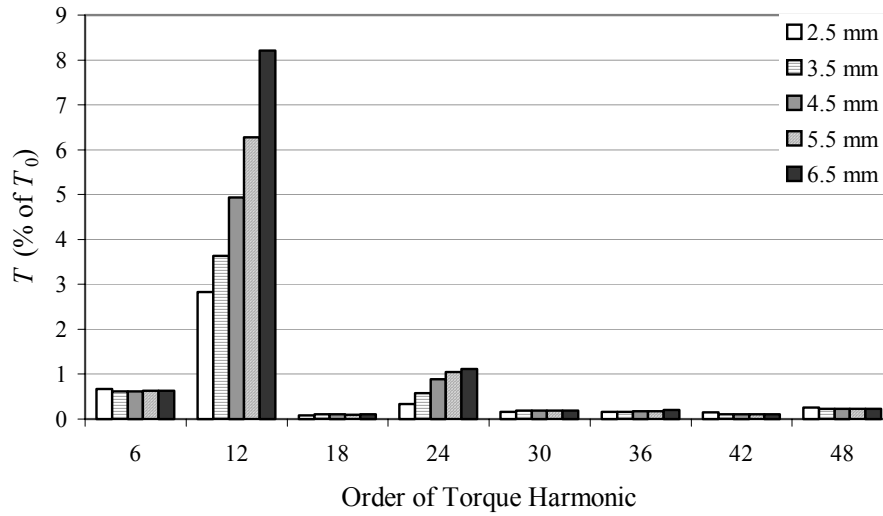


Fig. 3.8. The effect of the slot opening width on the torque harmonic amplitudes. The different slot opening widths used in the calculations are given in the figure. The wider the slot opening is the larger the cogging torque will be.

As figure 3.8 shows, the slot opening width has a remarkable effect on the slot ripple frequency torque component amplitude (12th harmonic with $q = 2$) and its multiples. In practice, the slot opening is made as narrow as possible with respect to the manufacturing of the winding. The physical limitation is set by the conductor diameter. The narrower the opening is the more difficult it is to insert the punch of conductors (side of the coil) in to the slot. Quite often, it is recommended that the opening measure should be at least twice the biggest conductor diameter. With automatic or semiautomatic winding machines this limitation is even tighter.

The effect of slot opening width may also be predictable by means of the air-gap permeance function. The permeance fluctuation was calculated along one pole pitch using the equation given by Weber (2.4) and was then divided into harmonic components (Fig 3.9)

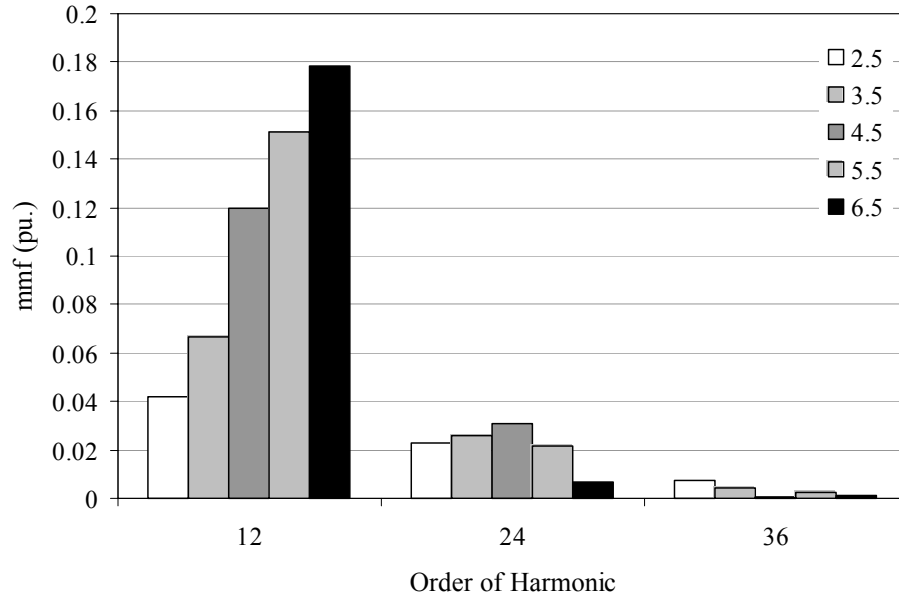


Fig. 3.9. Harmonic content of the mmf with different slot opening length. The physical air-gap is 2 mm and slot pitch 13.7 mm

Figure 3.8 also includes winding harmonic components (sixth and its multiples) of the torque, but when compared to figure 3.9, the uniformity of the 12th harmonic is obvious.

3.2.2 Winding harmonics

Since the windings of an AC-machine are usually placed in the stator slots and cannot thus be spread smoothly over the stator inner surface as a result, in addition to permeance harmonics, also winding harmonics are produced (Pyrhönen 1993). The ordinals of the winding harmonics ν in an m -phase winding are

$$\nu = 2g_1m + 1, \quad (3.1)$$

where g_1 is any positive or negative integer. The angular velocity of the harmonic ν with respect to the stator is

$$\omega_{\nu s} = \frac{\omega_s}{\nu}, \quad (3.2)$$

The harmonics induce voltages in the stator that have the same angular velocity as the fundamental wave. The number of pole-pairs of the harmonic is

$$p_v = \nu p . \quad (3.3)$$

The pole pitch τ_{vp} of the harmonic compared to the pole pitch τ_p of the fundamental is

$$\tau_{vp} = \frac{\tau_p}{\nu} , \quad (3.4)$$

The amplitudes of the magneto motive forces $\hat{\Theta}_\nu$ compared with the amplitude of the fundamental $\hat{\Theta}_1$ can be found with the winding factors ξ_ν

$$\hat{\Theta}_\nu = \hat{\Theta}_1 \frac{\xi_\nu}{\xi_1 \nu} , \quad (3.5)$$

where

$$\xi_\nu = \frac{2 \sin(\nu \frac{w}{\tau_p} \frac{\pi}{2}) \sin \frac{\nu \pi}{2m}}{\frac{Q_s}{mp} \sin \frac{\nu \pi p}{Q_s}} \quad (3.6)$$

The ratio w/τ_p describes the deviation of the coil span w from the pole pitch τ_p . The principle of two three-phase windings - a single layer winding for which $w/\tau_{pp} = 1$ and a two layer winding for which $w/\tau_p = 5/6$. in a $q = 2$ stator is illustrated in figures 3.10 and 3.11.

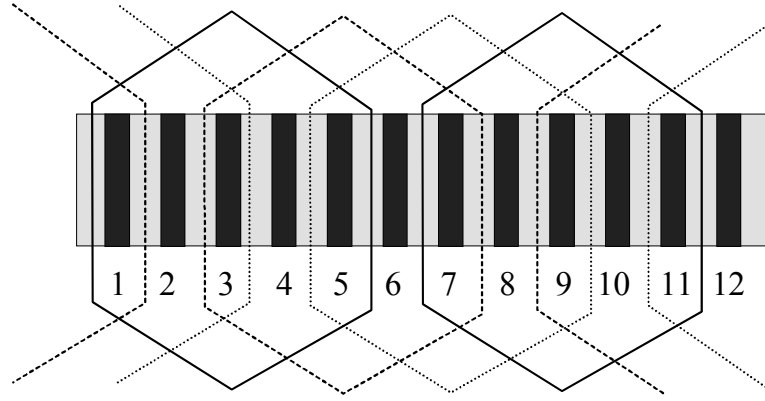


Fig. 3.10. The ordinary three-phase one layer winding ($w/\tau_p = 1, q = 2$), along one pole pitch.

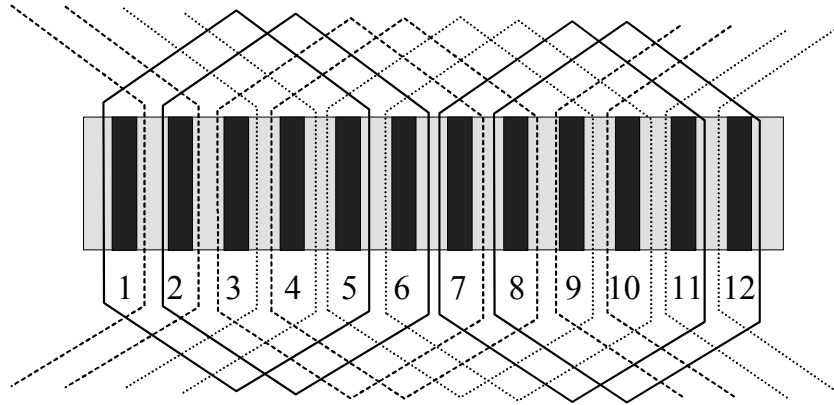


Fig. 3.11. Two layer short pitch winding ($w/\tau_p = 5/6, q = 2$), along one pole pitch.

Even though the winding in figure 3.11 seems more complicated due to the number of coils, in practice it is not. Quite often, the winding type illustrated in figure 3.10 is composed of two layers. This enables diamond winding, which makes the winding ends easier to assemble. This means that the number of coils in both of the cases become the same. When $q = 1$ all the winding factors have the same value $\xi_v = 1$. When a winding with $q = 1$ is applied, a very special rotor design is needed to avoid harmonic torques generated by the stator magneto motive force. The best torque quality is, in this case, achieved with sinusoidal formed permanent magnets. Figure 3.12 gives the most interesting odd harmonic winding factors of the windings described in figures 3.10 and 3.11.

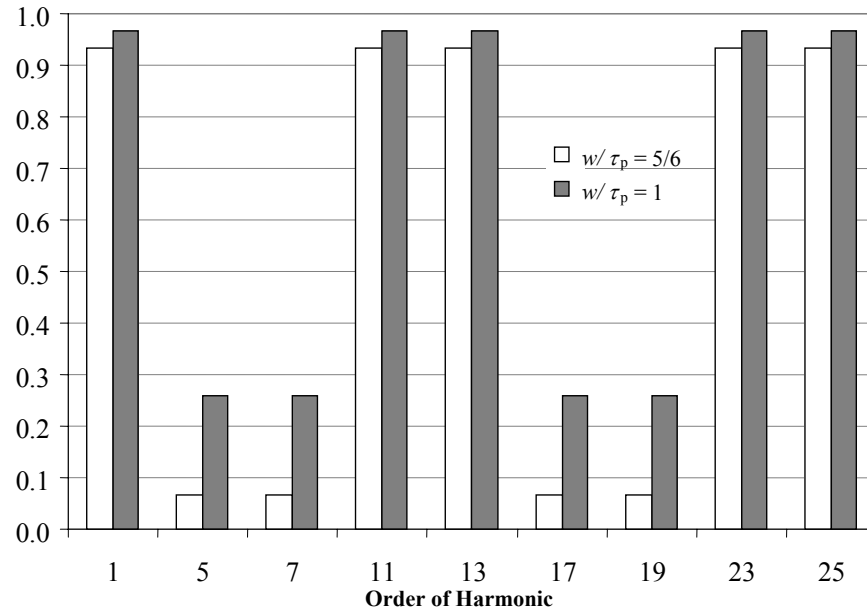


Fig. 3.12. Winding factors of two different windings ($Q = 120, p = 10$)

The fundamental component of the short pitch winding is a bit lower and some of the average torque is lost. But also with a lot lower fifth and seventh harmonic, considerably less sixth harmonic will be produced in the torque. This can also be noticed in the torque calculations.

Three different types of winding arrangements were calculated by means of the reference motor. All windings were applied to the same stator frame, the number of pole pairs in the $q = 1$ version being twice that of the two others. The average torque is kept constant between the versions. To find out the impact of the winding and permeance harmonics the calculation was carried out two times for each coil structure (Figs. 3.13 and 3.14). In the second calculation the permeance fluctuation component caused by the slot openings was submitted from the results.

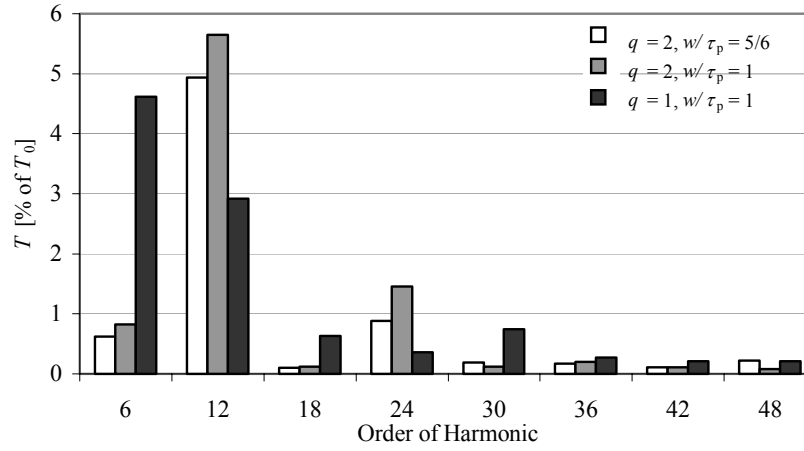


Fig. 3.13. Total harmonic torques created by three different winding arrangements. The magnet width in the calculations is $\alpha = 0.89$.

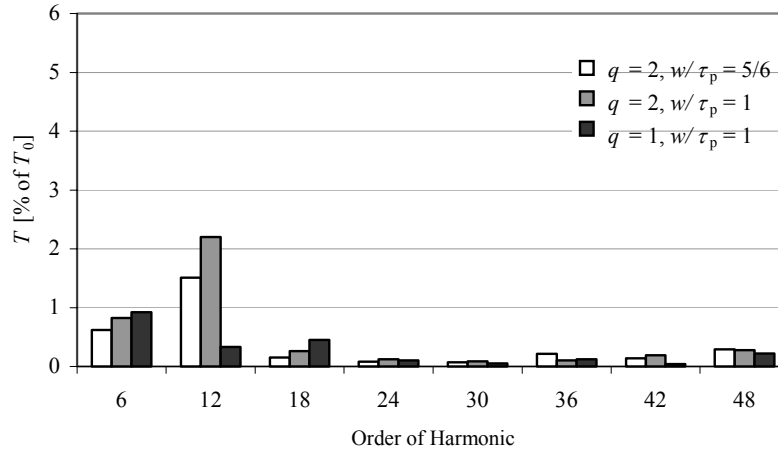


Fig. 3.14. Harmonic torque without slotting permeance component created by three different winding arrangements. The magnet width in the calculations is $\alpha = 0.89$

As figures 3.13 (total harmonic content) and 3.14 (harmonic content without cogging) show, the winding harmonic content is not as significant as the permeance harmonic content. The winding harmonics can be reduced with a fractional slot winding and thus attention should rather be focused on the magnet form and other possible ways (air-gap, magnet positioning asymmetry...) to reduce the effects of the permeance harmonics.

It may be noticed, that the short pitch winding is somewhat better in cases where $q = 2$, with the winding harmonic produced torque ripple (6th) as well as with the mmf harmonic due to slotting (12th). When $q = 1$, the mmf harmonic due to slotting and the first winding harmonic generated torque ripple are at the same frequency (6th) and latter is significantly higher than in the cases when $q = 2$. The harmonic content of mmf with different winding arrangements is illustrated in figure 3.15.

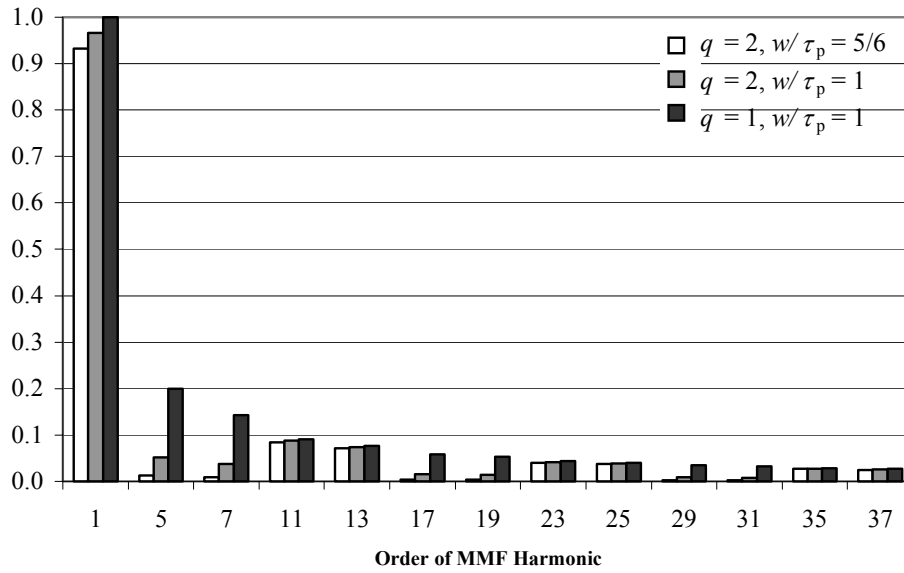


Fig. 3.15. Harmonic pu mmf components created with different winding arrangements. The magnet width in the calculations is $\alpha_p = 0.8$.

The effect of the winding harmonic produced torques (the sixth torque harmonic and its multiples) can also be estimated using winding factors of different winding arrangements. Rotating of the winding harmonics may happen, depending on the harmonic order, clockwise (CW) as well as counter clockwise (CCW) so that when the fundamental frequency wave rotates CW, $(6n - 1)$ rotates CCW and $(6n + 1)$ CW, when n is a positive integer. This means that both $(6n - 1)$ and $(6n + 1)$ create with fundamental frequency a component with the harmonic order $6n$. When comparing the sixth torque harmonic in figure 3.13 and the fifth and the seventh mmf-harmonic amplitudes in figure 3.15 (winding harmonic divided with harmonic

order), the affinity can easily be noticed, even though the sixth harmonic in figure 3.13 contains also the permeance-harmonic-created cogging torque component.

3.3 Air-gap

Varying the air gap length may be the simplest way to affect the torque harmonic amplitudes. A calculation with air-gaps between 0.1 ... 6 mm was made. The results obtained for the torque harmonics and for the average torque with constant current RMS value (Fig. 3.16) are interesting.

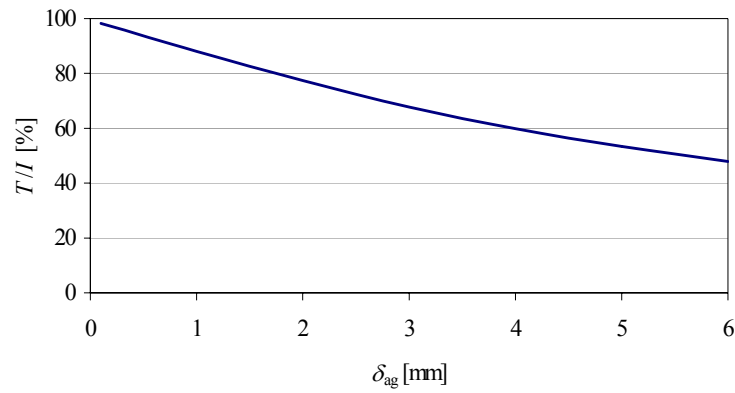


Fig. 3.16. The effect of the air-gap length on the maximum average torque created with constant current. The reference value (100 %) is theoretical closed air-gap ($\delta_{ag} = 0$)

Figure 3.17 represents the reference motor behaviour calculated with three different air-gap lengths.

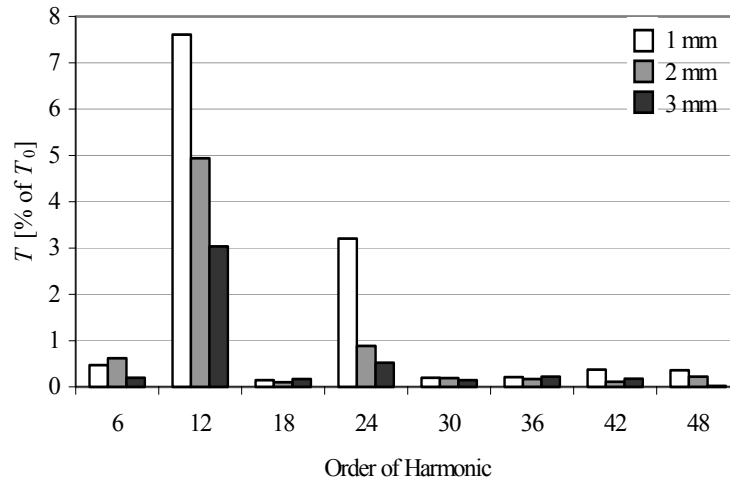


Fig. 3.17. The effect of three different air-gap lengths on the harmonic torques at constant average torque T_0 .

The closer the magnets are placed to the stator the larger grows the air-gap flux density and the magnetizing inductance increasing the torque–current–ratio, but also the deeper becomes the groove in the air-gap flux density distribution under the slot opening increasing the cogging phenomenon. The optimum air-gap length should be adjusted depending on the application, e.g. compromising between maximum torque, losses (T/I -ratio) and cogging.

3.4 The Rotor

The torque of the motor is created by the flux in the air-gap and thus the harmonic content of the air-gap flux density is of critical importance. Along the stator the rotor structure has a great influence on this flux density shape. With a laminated rotor and punching technique there are numerous possibilities of permanent magnet mounting in radial flux machines, as it is shown in figure 1.6. It is more difficult to arrange the manufacturing of the rotor lamination in axial flux motors. Hence, the permanent magnets are normally fixed on the rotor surface and the main difference in the torque quality should be achieved by shaping the magnets.

3.4.1 Permanent Magnets

Permanent magnets have several properties that affect the flux distribution in the air-gap such as:

- The shape of the magnet

- The magnetisation direction
- The cross-sectional shape (pole shoe form)
- The height of the magnet
- The width of the magnet
- Magnet properties (remanence flux density, permeability, coercive force)
- The distance between the poles (leakage flux)
- Positioning on the surface

The magnetisation direction is relevant mainly in radial flux machines, having a round air-gap shape. The effect of parallel or radial magnetisation on the air-gap flux density created by the magnets is remarkable (Sebastian 1996). In parallel magnetisation the flux lines on the magnet surface are parallel independent of the surface shape, when in radial magnetisation they have the direction of the radius. In axial flux machines parallel magnetisation is normally used.

Optimal width of the magnet

Another value of critical importance is the magnet width compared to pole width or slot pitch (figure 3.18).

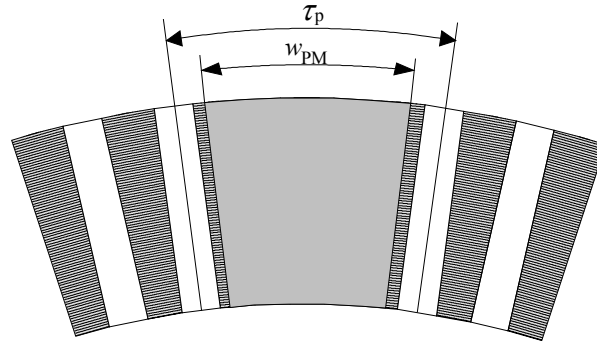


Fig. 3.18. Permanent magnet with parallel edges (SOR) compared to the slot opening.

Li (1988) and Ishikawa (1993) have studied this topic in radial PM motors using FEM. They used radial magnetised magnets for their calculations. The authors introduce formulations, where the optimal magnet width should be selected according to the following equations:

$$w_{PM} = (n + k_w) \tau_s . \quad (3.7)$$

n is an integer and k_w is a constant. The magnet relative width compared to pole width is

$$\alpha_p = \frac{w_{PM}}{\tau_p} . \quad (3.8)$$

In their respective study, Li suggests for k_w the value 0.14 and Ishikawa 0.17. Table 3.2 gives the optimal relative magnet widths for the reference motor. The values are calculated applying respectively Li's and Ishikawa's formulation.

Table 3.2. Optimal permanent magnet relative widths calculated applying respectively Li's and Ishikawa's formulation.

N	α_p (Li)	α_p (Ishikawa)
1	0.190	0.195
2	0.357	0.362
3	0.523	0.528
4	0.690	0.695
5	0.857	0.862

Figure 3.19 illustrates the calculation results obtained with analytical equations and with magnet relative widths between 0.5...1. The magnet shape used in calculations corresponds to that shown in figure 3.18.

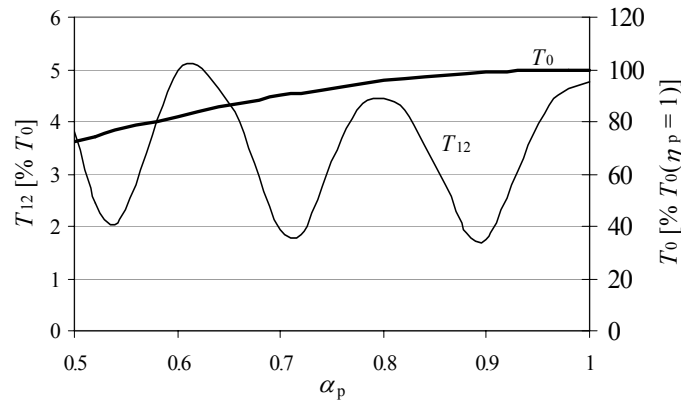


Fig. 3.19. The effect of the magnet relative width on the average torque and 12th harmonic component (T_{12}) at constant pole angle. The slot opening is 4.5 mm. The permanent magnet width has a significant effect on the cogging torque. The best result with respect to the average torque and cogging is achieved with $\alpha_p = 0.89$. A local optimum producing a lower average torque is at $\alpha_p = 0.72$.

When comparing the values given in table 3.2 with the results described in figure 3.19, which represents the effect of magnet relative width in the reference motor calculated with the method above-mentioned, it should be noticed that they are very closely corresponding. Any of the articles referred to mentions the shape of the slot opening or any other dimensions, but it may be concluded from the figures that the slots are open (wide slot opening). However, the articles do not examine the effect of the slot opening on the optimal width of the permanent magnet. In figure 3.20 the effect of the slot width on the optimal magnet width is described.

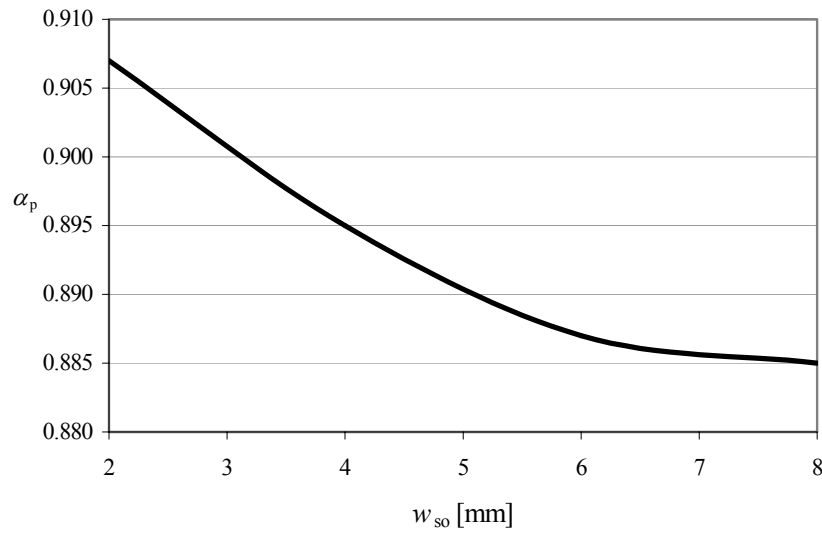


Fig. 3.20. The effect of the slot opening width (w_{so}) on the optimal magnet relative width (α_p) with rated average torque. The local optimum producing the maximum average torque is selected

Figure 3.20 shows that varying the opening width causes a slight difference, which partly explains the slight differences in the results. Also the type of the motor (radial vs. axial) and, probably, magnetisation may affect to a certain degree the results, but in general the results seem to be very similar.

The optimal relative magnet length can also be determined relatively accurately from the harmonic content in the smooth (slot-less) air-gap flux density curves created by the magnet (figure 3.21). Even though this calculation does not take into account the loading conditions, slot opening size, etc., the results are interesting.

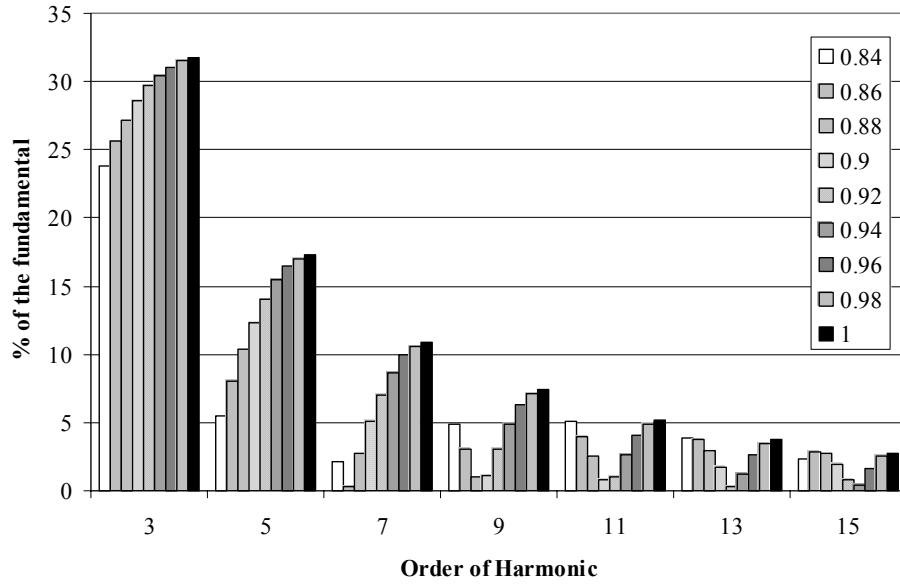


Fig. 3.21. Harmonic content of mmf (no load) calculated from the air-gap flux density created by the magnet. The relative width of SOR-type magnet is varied between 0.84...1.00.

12th harmonic component in the torque is produced by the 11th and 13th harmonic components in mmf. In the range of $\alpha_p = 0.84 \dots 1.00$ the minimum of these components is reached at about 0.90, similarly as for the torque calculation. When giving it a closer examination, it can be found that the same sinusoidal component, as it was seen in figure 3.19 (12th harmonic), appears in the bar presentation of each harmonic. This can be most clearly observed with the 15th harmonic. This means that the local minima of the harmonics are found also with other widths, as it was also seen in figure 3.19. Nevertheless, in practice, the 12th harmonic appears to be the most interesting component of the torque in this respect and its calculated area is thus the most relevant.

Different Permanent Magnet Designs

As it was earlier stated, the magnets of sinusoidal shape and uniform thickness (figure 3.19), in theory, eliminate all torque vibrations generated by the stator and rotor mmfs. The use of sinusoidal magnets in AFPMS-motors brings the problem that the magnets of one pole pair should be of equal shape and orientation (as in Figs. 3.22 and 3.23) in order to keep the symmetry between the poles. The magnets should be separated from each other with a certain distance (Δ_{PM}) in order that the fixing of the magnets in the manufacturing process would

become easier and the leakage flux between could be minimized. Last two factors limit the effective area of the magnet leading in the somewhat reduced maximum torque and increased T/I ratio. Theoretically, the 3rd harmonic in the magnet contour function should not increase the level of torque vibration, but it increases the effective area compared to pure fundamental (Figs. 3.22 and 3.23).

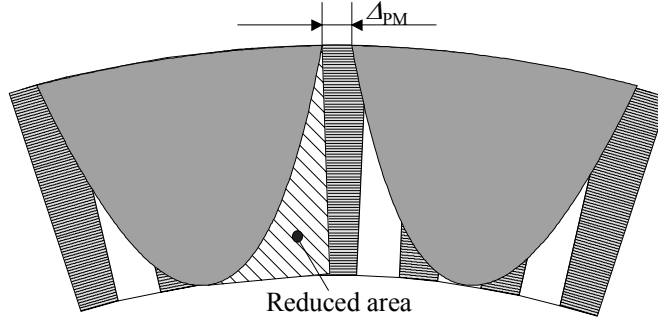


Fig. 3.22. PM with sinusoidal (only fundamental) contour shape and equal uniform thickness ($q = 1$). The figure demonstrates the reduced magnet area giving thus a reduced volume compared to the sector of a ring (SOR) shape.

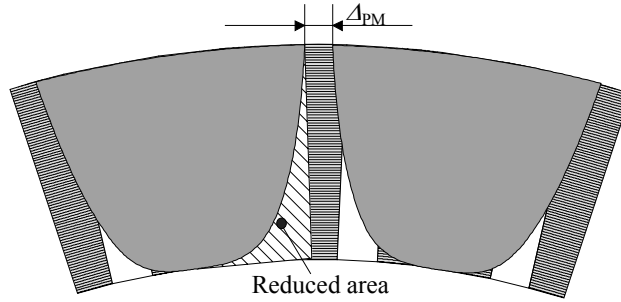


Fig. 3.23. PM with sinusoidal (fundamental and small amplitude of the 3rd harmonic added) contour shape and equal uniform thickness ($q = 1$).

The torque created by the PM with sinusoidal contour were calculated and compared with the in figure 3.18 illustrated shape (SOR) of the magnet in $q = 2$, $w/\tau_p = 5/6$ stator $\xi_1 = 0.933$, $\xi_5 = 0.067$ and $\xi_7 = 0.067$. The magnet and calculation details are given in table 3.3.

Table 3.3. Calculation parameters and magnet properties for calculations. The names of the magnet shapes refer to figures 3.18 (SOR), 3.22 (Sin(1)) and 3.23 (Sin(1+3)). Sin(1+3) contains third harmonic 10 % of the fundamental component.

Motor parameter	SOR	Sin (1)	Sin (1+3)
Calculation torque T_0	~ 690 Nm		
Motor current (I)	17 A		
Slot opening width w_{so}	4.5 mm		
Air-gap length δ_{ag}	2 mm		
Magnet thickness (h_{PM})	5.0 mm	5.5 mm	5.5 mm
Magnet relative width (α_p)	0.8		
Magnet relative width in stator outer diameter (α_p)	0.8	0.96	0.96
Total volume (cm^3)	8.25	7.20	8.11
Permanent magnets			
- Material	NdFeB		
- Remanence flux density	1.15 T		
- Relative permeability	1.2		

The thickness of the sinusoidal contour magnets was increased by 0.5 mm to partly compensate the reduced surface area. The results of the calculation are given in figure 3.24.

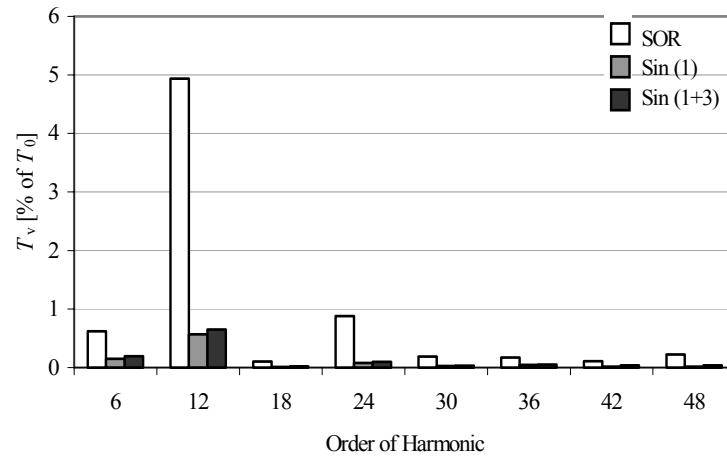


Fig. 3.24. Harmonic content of the electro-magnetic torque with different magnet shapes and rated average torque. Calculation parameters are given in table 3.3.

The sector of the circle-shape of the magnet, used in the comparison, does not have the optimal relative width (comp. fig. 3.17) creating a large cogging (5 %), but also with the optimal width ($\alpha_p = 0.89$ or 0.72), the 12th harmonic has an amplitude of almost 2 % of T_0 . The sinusoidal contour shape seems to be effective with all multiples of the 6th order. The torque quality produced using the sinusoidal contour magnets meets almost all the requirements made of it. However, the cogging torque, which is in the range of 0.7 %, is not good enough for purposes demanding an utmost smoothness of the torque.

Since the cogging must be further reduced and a considerable share of the effective magnet surface area is lost with the sinusoidal contour shape alternative shapes will be studied. Modifying of the permanent magnet edges is probably the most generally used method to reduce cogging (De la Ree 1989, Jahns 1996, Huang 2001). The permanent magnet is formed so that the edge is not parallel with the slot opening but during rotation goes smoothly over it. For the radial flux machine the simplest form is a rhomb. For the axial flux motor the corresponding shape is shown in figure 3.25.

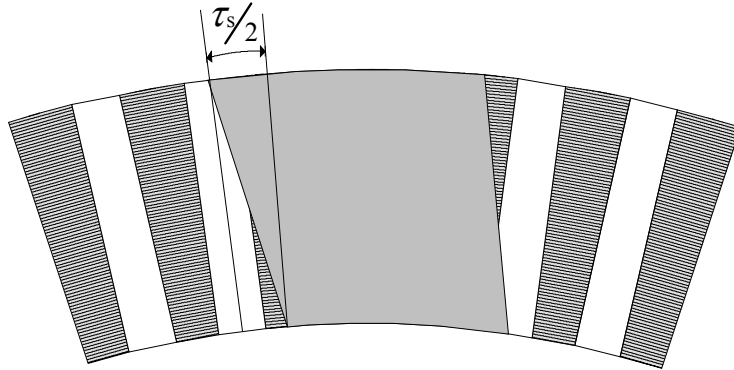


Fig. 3.25. Permanent magnet form with edges skewed by half a slot pitch (30 electrical degrees in $q = 1$). The mmf Fourier analysis of this form is as follows, $\Theta_1 = 1$, $\Theta_3 = 0.245$, $\Theta_5 = 0.075$, $\Theta_7 = 0.014$, $\Theta_9 = 0.003$, $\Theta_{11} = 0.001$, $\Theta_{13} = 0.003$

The calculation results shown in figure 3.19 indicate that the first (closest to the pole width) optimal width for the magnet is about $\alpha_p = 0.89$. The magnet of this width was skewed from 0 to 85 electrical degrees. The results of the calculation are shown in figure 3.26.

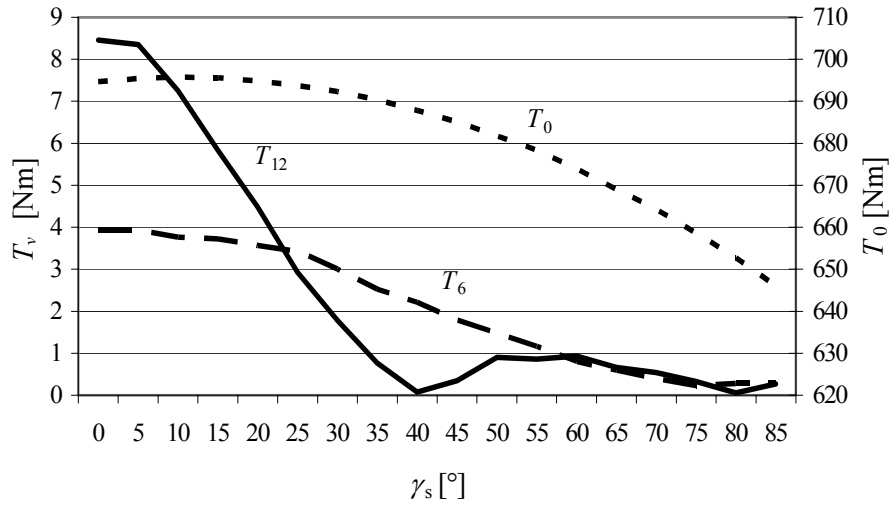


Fig. 3.26. The effect of the skewing angle (electrical) on the 6th and the 12th harmonic torque and the average torque ($q = 2$ and $\alpha_p = 0.89$). γ_s defines the edge skew (one pole pitch is 180°).

The calculation shows (Fig. 3.26) that the first minimum for the slot ripple frequency (12th with $q = 2$) is at 40° and the next at 80°. The winding harmonic (T_6) reaches its first minimum at about 80°. The pole angle was kept constant during the calculation. It can be noticed that the average torque (T_0) reduces when the skewing increases. At 40° the average-torque is reduced only by about 1%, but the 12th harmonic is almost vanished and the 6th harmonic torque is reduced by about 50%.

The mmf harmonics created by magnets in similar cases having a certain shape give interesting results for comparison with the torque harmonics. The skew area between 25°...70° (el.) gives harmonics shown in figure 3.27.

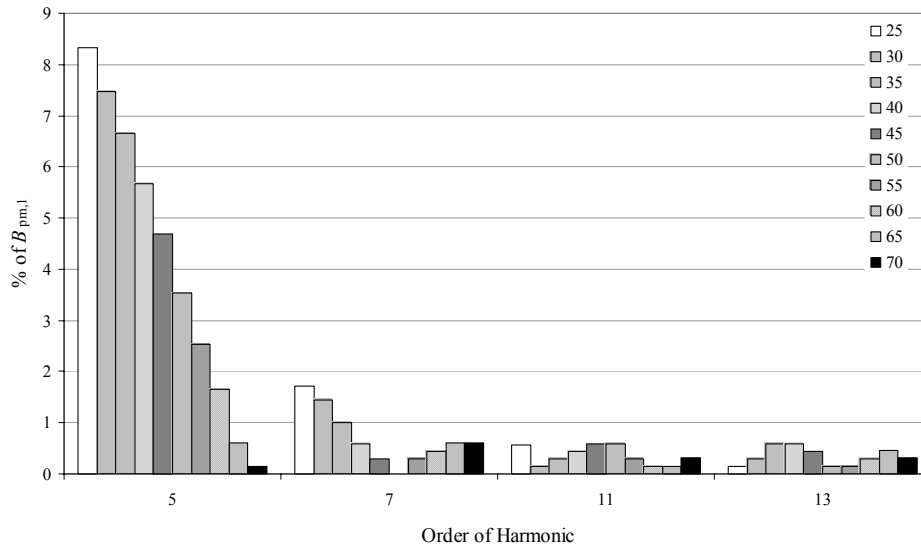


Fig. 3.27. The effect of the skewing angle (electrical) on the permeance harmonics, calculated in no load condition and for the slot-less stator. The skew angle is varied between 25°...70°.

The mmf harmonic orders five and seven together with the fundamental create 6th harmonic and the mmf harmonic orders 11 and 13 create the 12th harmonic in the torque. The fifth harmonic in mmf (which is more dominant compared to the seventh) behaves similarly as the sixth in the torque. It remains unclear if the mmf 11th and 13th are equal with the 12th torque harmonic. This may be explained by the fact that mmf is calculated in no load condition and for the slot-less stator, in which case the permeance harmonics due to slotting are not considered. As an interesting result may be observed the reduction of the fundamental component of the air-gap flux density due to magnet edge skewing (Fig 3.28).

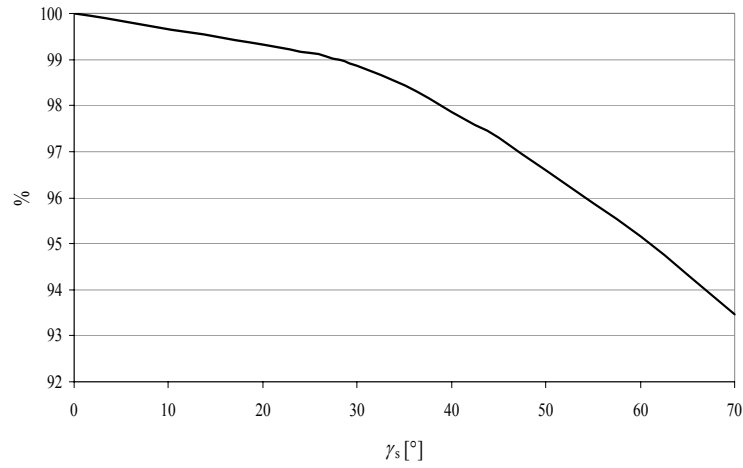


Fig. 3.28. The reduction of the fundamental air-gap flux density due to skew angle. The reference value is that of the non-skewed magnet.

The reduction of the fundamental component of air-gap flux density created by the permanent magnet corresponds well the average torque given in with figure 3.26. This means that the adverse effect of skewing appears to be the decreasing of the T/I -ratio. In figure 3.29 the 40° skewed magnet torque production is compared with the sinusoidal shapes and a comparison of the corresponding no load (slot-less stator) mmf harmonic between the same magnet versions is presented in figure 3.30.

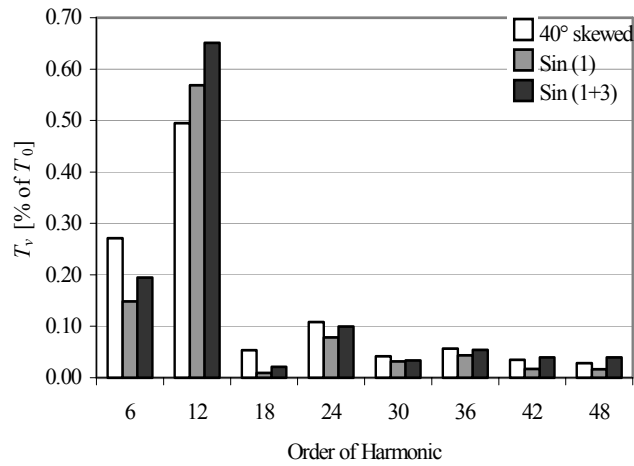


Fig. 3.29. Torque harmonics in rated load condition. 40° skewed ($\alpha_p = 0.89$) magnet compared with sinusoidal contour magnets. $q = 2$.

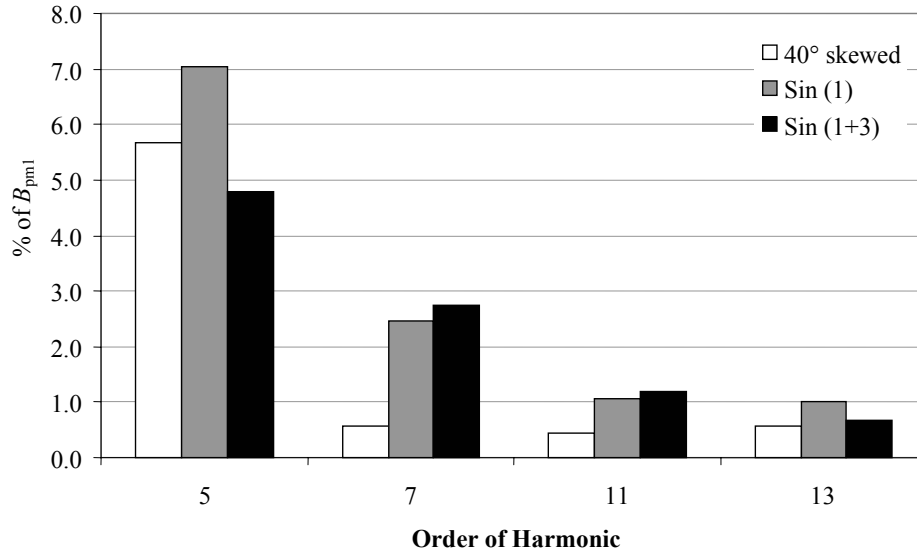


Fig. 3.30. Permeance harmonics of slot-less stator in no load condition with 40° skewed ($\alpha_p = 0.89$) magnet compared with sinusoidal contour magnets. $q = 2$.

Skewing seems to be a very effective way of reducing both permeance and winding harmonics. But, as above-discussed, parallel (edges parallel together) skewing reduces the average torque/magnet volume. Opposite skewing in the side edges (according to figure 3.31) may be an alternative to avoid this problem.

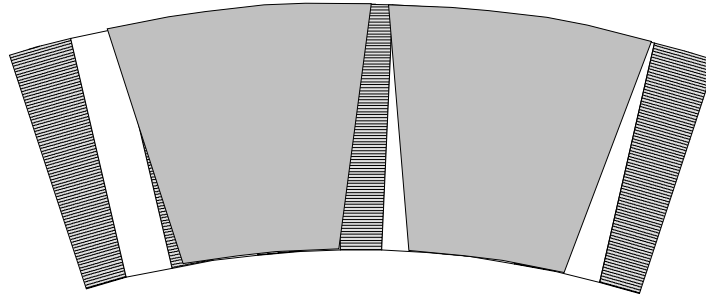


Fig. 3.31. AFPM with opposite skewing in the opposite edges. This shape keeps its same magnetic centre in the magnet with the whole stator radius, which parallel skewing does not.

Because cogging is a result of time varied (rotating field) permeance change under the slot opening, it might be optimal to have the edge pass the slot with equal speed along the radius

(v_{rad}). If the edge is straight, the speed changes along the radius and thus the edge could be curved. A magnet of this shape is shown in figure 3.32.

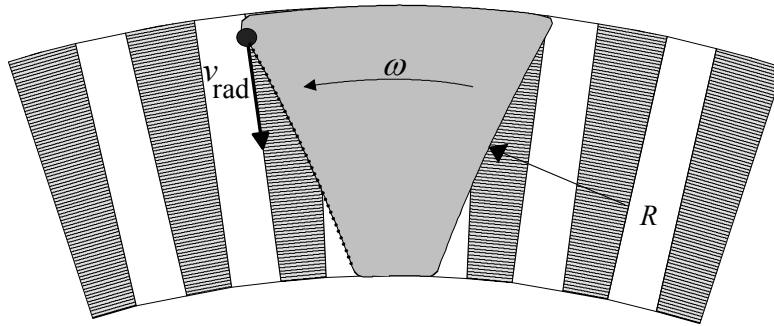


Fig. 3.32. Magnet with skewed and curved edges to keep the radial edge speed (v_{rad}) constant.

The calculation results given in Fig. 3.33 indicate that the above-mentioned assumption is incorrect. The difference, however, is insignificant.

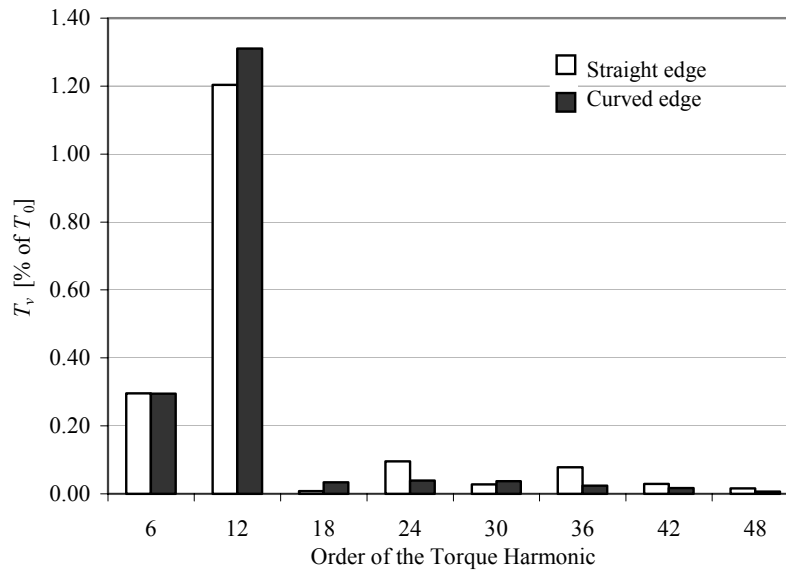


Fig. 3.33. Torque harmonic contents using magnets with curved and straight edges and with rated load.

Unequal Magnet Thickness

The calculation program assumes that the magnets are of uniform thickness. This means that the no-load air-gap flux density is also uniform on the magnet surfaces. The air-gap flux linkage time function can, in these cases, be formed only by selecting the suitable magnet contour. It is, however, possible to affect the air-gap flux density by forming the cross-section form of the magnet in varying the thickness of the magnets to be suitable. Still, shaping of the permanent magnet is limited by the manufacturing process. Sharp corners, as figure 3.29 a) illustrates, are not recommended for use neither in the magnet manufacturing process nor in the fixing. In the compression process the height of the magnet should be approximately uniform. Thin edges easily get cracks, which might break the whole magnet because of the powerful internal forces. Also during the process of mounting the forces between the magnet and the rotor iron are strong as a result of which the magnet may get easily broken. As to the air-gap flux density spatial shape the magnet shown in figure 3.34 a) would be right, but in practice the result should correspond to the figure shown in fig. 3.34 b). Even so, both alternatives lose some of the effective volume compared to a rectangular cross-section, which thus reduces the T/I -ratio (maximum torque/current unit) or increases the length of the air-gap.

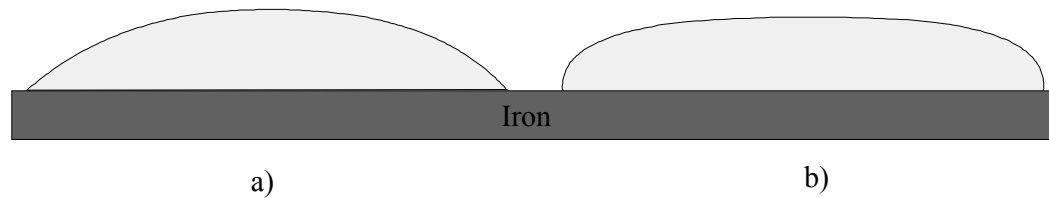


Fig. 3.34. Two different cross-sectional areas of permanent magnets to form the air-gap flux density closer to a sinusoidal form. In practice, version a) is not valid due to its sharp edges and thus b) suits better for practical applications.

Because of the size of the magnetic pole the construction of large machines allows also a number of magnets having a same polarity. This enables the designer to use variably thick pieces in different parts of the pole and thus to modify the air-gap flux density closer to the sinusoidal flux density. Nipp (1996) has studied this type of arrangement for surface inset magnets in a radial flux motor. His results indicate that with this type of magnet combination lower harmonic amplitudes may be achieved as when only magnets of uniform thickness are applied. In a smooth surface mounted, axial motor, some of the magnet effective volume would

be loosed. Magnets having a same polarity reject each other, which makes mounting difficult. This is always the case when one pole is made of multiple pieces.

Results from magnet shaping

There are numerous different ways to modify the permanent magnet pole. The optimum shape and size depend on the application used and for this reason it is impossible to define the absolutely perfect, multipurpose shape. In general, the magnet should be formed either by skewing (with equal thickness) or applying, e.g. according to Fig. 3.34, cross-section shape modification. With such a formulation the cogging can almost be totally eliminated without loosing much of the average torque performance.

3.5 Magnetic Circuit and Saturation

The critical parameters for the designing of an electrical motor are the flux path dimensioning and the geometry in general. However, some of the motor applications set limitations because of which it is necessary to make compromises concerning the dimensions of the motor or the amount of materials in the motor. This means that it should be sought for a balance between copper and iron losses, saturation, current density etc. As a consequence, not only the losses are affected, but also the torque vibration and the rated torque of the motor. If the cross-section area of the flux path is too small, the relative share of leakage flux increases. This usually deforms the air-gap flux density from the ideal sinusoidal shape, increasing thus the harmonic content in the torque. Also poor material properties may cause saturation, which also increases the harmonic content of the torque.

To find out and analyse the effect of saturation the teeth (figures 3.35 and 3.36) and stator yoke (figure 3.37) cross section areas were varied. The other parameters of the stator were kept constant. As the diameters and the slot numbers were first kept constants also the slot pitch (τ_s) stays constant. This means that in varying the tooth width (w_{to}) also the slot width (w_{sl}) will change correspondingly,

$$w_{sl} = \tau_s - w_{to} , \quad (3.9)$$

As a result, the reluctance network parameters of that part change and this in turn affects the leakage flux.

In practice, decreasing the slot width also limits the amount of copper in the slot due to which also other motor parameters become different. Figure 3.35 shows that with the slot width of 10 mm the iron in some of the teeth becomes highly saturated causing an increase in almost all the orders of the harmonic torques. High saturation causes also a considerable reduction in the average torque T_0 (fig. 3.36).

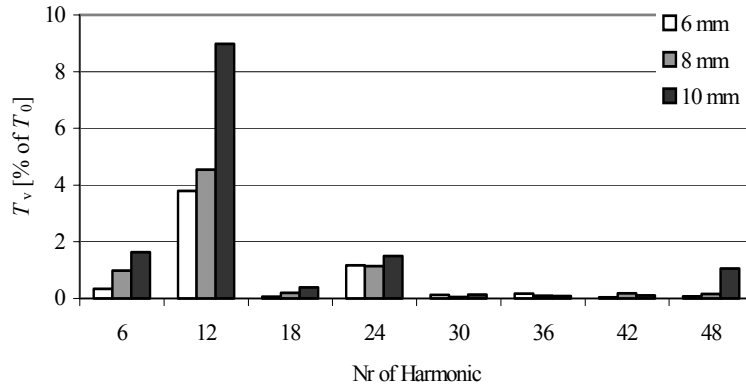


Fig. 3.35. Relative harmonic torques when the slot width is varied between 6 and 10 mm. The slot opening is kept constant (4.5 mm).

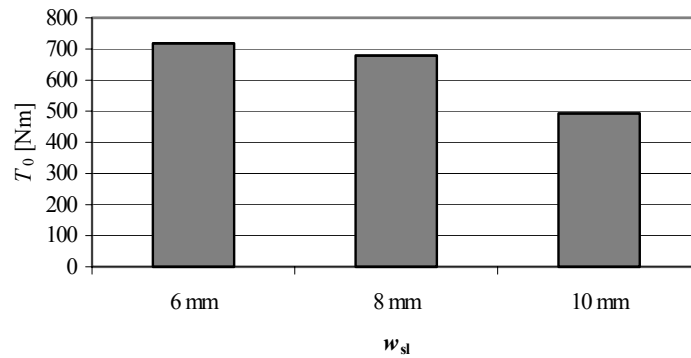


Fig. 3.36. The effect of saturation on the average torque of the motor. The slot width was varied between 6 and 10 mm to vary the tooth cross-section area.

Saturation can also take place in the stator or rotor yoke. In an ideal situation the flux density is sinusoidal distributed along the yoke. If the iron path is too tight the top of the curves flatten which creates harmonic components in the flux density. In practice, this means that the leakage flux in the slots, the slot openings and the air-gap increases. In figure 3.37, the motor is

calculated in rated load condition by adding and removing 50 % of the stator yoke cross section area.

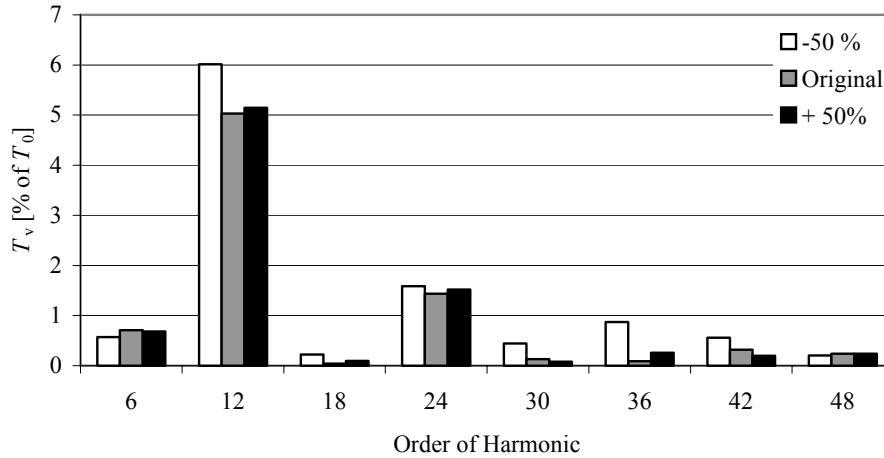


Fig. 3.37. The effect of the yoke saturation on the torque harmonics. The motor is calculated using constant current and pole angle. The cross section is reduced and increased by 50 % from the original value.

The results show that the dimensions in the original version were close to optimal. Increasing the area does not reduce the harmonic components and does not increase the created torque. While reducing the cross section area by 50 % the slot ripple frequency starts to increase and the rated torque (torque with same current and pole angle) will be reduced by about 14 %.

The effect of saturation is quite commonly ignored in studies treating the cogging effect. However, the figures above indicate that in dimensioning the magnetic circuit it may be created an additional source of cogging and therefore this process should be paid careful attention. It is impossible to give any exact recommendation to specify the iron path saturation. This value depends on the used material and application (e.g. over load capacity). Practical experience shows that it is an appropriate method to create an approximately equal peak flux density in the teeth and yokes and to keep this below 2 Teslas.

3.6 Asymmetric magnetic circuits

The basic idea of creating asymmetry in the magnetic circuit is to prevent all magnets of entering the slot area simultaneously. This topic has been widely studied during the latest years

(Studer 1997, Zhu 2000 and Bianchi 2000). In symmetric permanent magnet distribution all poles amplify the harmonic frequencies in the same phase angle. In ideal asymmetry the same excitation exists in each pole as it does in the symmetric distribution, but because the phase angles are different in the slot frequencies the poles compensate each other. The slot frequency (cogging) is defined as

$$f_{sf} = \frac{Q}{p} f_s = 2qmf_s, \quad (3.10)$$

where q is the number of slots per pole and phase, m is the number of phases and f_s is the supply frequency.

Asymmetry has also its disadvantages. Depending on the type and degree of asymmetry low order harmonics such as first or second or even sub-harmonics, which in symmetric cases with no offset or gain error do not exist, may appear.

This may be due to the fact that the phase angle between the coils or of the fundamental wave of the linear current distribution is unequal, or the leakage fluxes in different poles differ from each other. The asymmetric magnetic circuit also causes asymmetry in the reluctance network due to different cross section areas or permeability of the corresponding parts of the magnetic circuit. This means that the electro-motive forces in different poles are in a different angle, as a result of which asymmetry occurs in the magnetic circuits between the poles, which affects the saturation of the circuit and the multiphase electric circuit. In series connected circuits this effect is more controllable due to equal current in each of the phase coils. Also the EMF is the sum of individual coils. When there are several branches, asymmetry caused by the unequal current distribution may change the balance between these branches causing thus saturation and flux differences in the magnetic circuit.

In case of symmetric magnetic circuit every pole may be put to work in the optimum point to maximize the T/I -ratio or just the torque. When the torque versus pole angle is sinusoidal and not linear, the T/I -ratio is, compared to a symmetric circuit, always somewhat smaller. The extreme case is when the asymmetry is increased equally to 180 electric degrees. In this case the sum torque is always zero, even though individual poles create torque.

To decrease the cogging torque the asymmetry needed is from zero to one slot pitch. The bigger the slot number per pole and phase q is set, the smaller the angle of one slot pitch is obtained and also the smaller the required relative asymmetry will be compared to the pole width.

The more complex the asymmetry appears to be, the more difficult the model for calculation will be. In practice, asymmetry brings that the whole machine has to be calculated instead of just one pole pair. In many cases FEM offers the easiest way of calculating.

The following chapters studies different possibilities of creating asymmetry in the magnetic circuit.

3.6.1 Asymmetric Magnet Distribution

It may be consequently assumed that when all the magnet edges, where the derivative component of the magnet flux density is at its highest, enter the slot openings at the same time high cogging torque is created. The cogging torque is usually reduced by forming the magnet edges so that these are not parallel to the stator slots. The shape of the air-gap flux linkage becomes thus closer to sinusoidal. But also in this case, all the non-linearities meet the slots simultaneously and this causes cogging.

In addition to the option of forming the geometry of the magnets, it is also possible to place them somewhat asymmetric on the rotor surface (fig. 3.38). An asymmetric distribution can be created in many different ways. All the magnets can be put in different deflection from the symmetrical centre point or they can be for example shifted in pairs. However, some factors limiting deflection should be considered. Firstly, the magnets cannot overlap. Deflection is, in this case, defined by the magnet shape and the relative width compared to the pole. The other reason is that shifting the poles limits the maximum torque of the motor. If the edges of adjacent magnets are very close to each other the leakage flux from one pole to the other increases due to which the air-gap magnetization decreases.

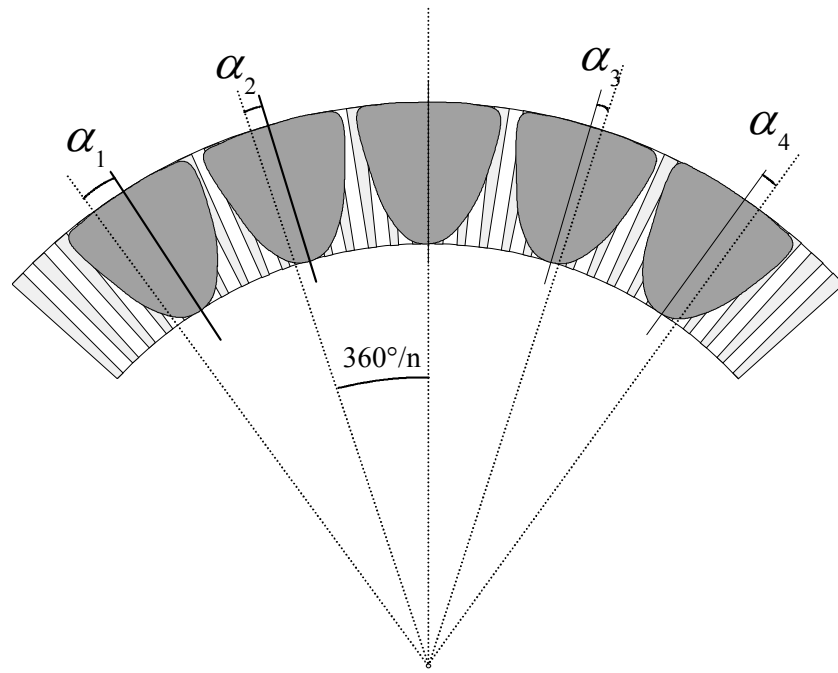


Fig. 3.38. Asymmetric magnet distribution in one quarter of the rotor. The magnet in the middle is kept in its original position. The other magnets are shifted by angles $\alpha_1 \dots \alpha_4$ from the symmetric position. In the symmetric distribution the distance between the magnet centres is $360^\circ/n$, where n is the number of poles.

Some assumptions and simplifications are needed in order to limit the size of the asymmetric model and the calculation time. In the calculation the reluctance network components in every pole pair are assumed to be equal, which corresponds to the symmetric distribution. If the magnets are distributed asymmetrically the flux in different pole pairs is not exactly the same. In such a case, it is incorrect to assume that the flux in the tangential edges of the model (between the parallel pole pairs) would be exactly the same. If the same should be considered for a multi-pole-pair machine, this would mean that all of the poles, in other words the whole machine, should be modelled in the reluctance network. However, the error made with this assumption remains insignificant, when the level of used asymmetry level is kept not too high ($> \tau_s$).

There are some factors that limit the application of asymmetry. The maximum asymmetry is ultimately limited by overlapping, but in practice some distance ($> \delta_{ag}$) should be left between

the permanent magnets to limit the leakage flux between them. This is the most important limitation when relatively wide ($\alpha_p > 0.95$) permanent magnets are used. The effect of magnet asymmetry is analyzed in figures 3.39 and 3.40.

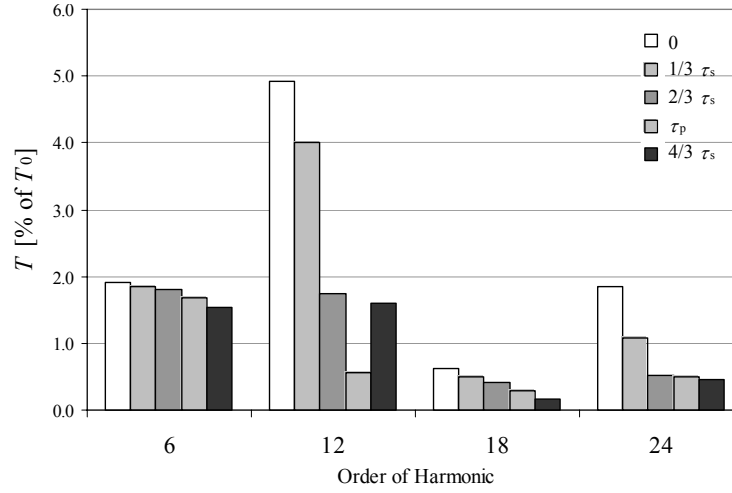


Fig. 3.39. The effect of an asymmetric magnet position on the torque harmonics. The maximum deviation is varied between 0 ... $4/3 \tau_s$. The calculation was made using equal asymmetry and SOR-magnets ($\alpha_p = 0.8$).

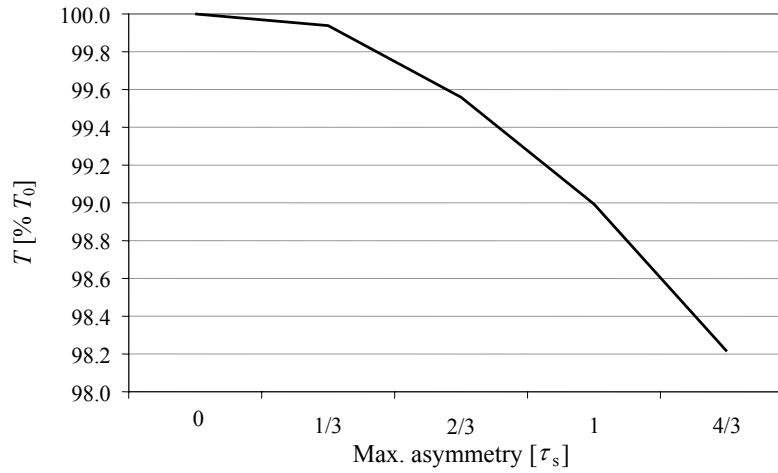


Fig. 3.40. The effect of an asymmetric magnet position on the average torque with constant current and constant average pole angle. The maximum deviation is varied between 0 ... $4/3 \tau_s$. The calculation was made using equal asymmetry and SOR-magnets ($\alpha_p = 0.8$).

As it is shown, asymmetry reduces some of the air-gap mmf fundamental in the same way as skewing does. The optimal level for asymmetry is one slot pitch. The 12th harmonic in the torque is reduced by about 90 % of that of the symmetric case of comparison and the average torque using the same calculation values is reduced only by 1 %.

3.6.2 Additional slot or slots

In machines with an integer q and a symmetric magnet distribution every magnet is passing a stator slot opening in exactly the same phase. This causes easily some cogging torque and noise in the machine, even then when the most sophisticated design for the form of the permanent magnets has been applied. The reason for this is that the number of slots divided by the number of magnets is an integer. Besides applying of asymmetric magnet distribution, asymmetry can also be created by means of the slots. With an increased number of slots ($Q \neq n p$) the cogging occurs in different phase in different poles. In the case of an odd Q all the magnets pass the slots in different phase angles and with an even Q at least two of the magnets are in the same relative angle.

Using an additional, empty slot or several empty slots asymmetry is achieved also between the poles and the stator phases and this causes low order harmonics in the torque. One additional slot makes an ideal phase shift ($\Delta\varphi_p$) between the poles, spreading the shift equally along one tooth pitch

$$\Delta\varphi_p = \frac{\tau_s}{2p} . \quad (3.11)$$

The more there are slots ($Q = m p q$), the smaller is the effect of one additional slot on the total pole asymmetry, but instead the cogging torque reduction remains at the same level as with small value of q . The method may thus be recommended for motors having a high number of pole pairs. From the production point of view it is easy to accomplish an additional slot. The measurements and the calculation results obtained with an additional slot are discussed in chapter 4.

In transversal flux motors this kind of an asymmetry has to be taken carefully in to consideration while the two different stators should preferably be exactly in 180°(el.) phase shift. The additional slot should cause the asymmetry difference in the opposite way in the two stators.

3.6.3 Eccentricity

Eccentricity is one of the factors that create unwished harmonic torques in the motors. This subject has been studied by e.g. Kim 1998, Wang 1999 and Paljan 2000. Eccentricity appears to be a problem in radial motors, more precisely in cases where the rotor alignment in the manufacturing process did not succeed or the rotor stiffness is not sufficient. However, eccentricity is more an unpredictable error of manufacturing, not a designing criterion, and is therefore not treated in detail in this research. Furthermore, it would require a different way of handling the air-gap reluctances and flux density created by the magnets to study eccentricity using the calculation method presented in chapter 2.

3.7 Conclusions

It is shown that in forming the magnet and using asymmetry either in the stator or magnet distribution it is possible to effectively reduce the cogging torque without dramatically affecting the torque average value. The winding arrangements and number of slots per pole and phase are a means of reducing the winding harmonics. Since the magnetic circuit depends on different factors as e.g. application, its requirements, manufacturing capabilities and other elements like the cost target of the machine, it is impossible to recommend any exact design for it. However, it may be stated that, generally, forming the magnet and using suitable asymmetry should be recommendable in most of the cases.

4 MODEL VERIFICATION – EXPERIMENTAL RESULTS

According to the calculations discussed in chapters 2 and 3 there exist many possibilities to affect the torque ripple of a permanent magnet synchronous motor. The results are based on theoretical studies and it is the objective of this chapter to show that the calculated and measured values correspond well to each other. It is also shown that based on the principles obtained with the calculation model introduced in this work it is possible to produce a really low torque ripple machine.

4.1 Reference Motor Versions

The motors manufactured to perform verification are axial flux motors with $Q_s = 120$, $q = 2$, $w/\tau_p = 5/6$ and $p = 10$, which is a motor configuration that produces a fairly low amount of stator harmonic magneto-motive force components. The elimination of the cogging torque is thus emphasized when the designing is made for the purpose of achieving a smooth torque. The calculation program enables the use of rotor PM of almost arbitrary shapes. Only the magnet width is restricted to be less than or equal with the pole pitch ($\alpha_p \leq 1$). Based on the calculations results three different magnet shapes were selected for practical verification of the results. The selected magnets shapes are illustrated in figure 4.1. The magnet shape shown in Fig. 4.1 a is optimised to achieve the lowest possible cogging. With the sinusoidal magnet shape (Fig. 4.1 b) no stator winding harmonics based torque components are produced since this shape produces a flux linkage containing only the first and the third harmonic. The magnet contour shape shown in Fig. 4.1 c is close to that of a sinusoidal magnet which has a negative third amplitude. The stator slot passing velocity of the magnet edges is almost constant and thus the cogging will remain low. In this study the magnets will be further called respectively: a) PM1_x, b) PM2 and c) PM3_x, where the subscript x indicates the asymmetry level of the magnet positioning as follows:

- x = 0 symmetric distribution
- x = 1 max. deviation from the symmetry $\pm 7^\circ$ (electrical)
- x = 2 max. deviation from the symmetry $\pm 14^\circ$ (el.)

The magnets of the PM1 and PM3 type were mounted symmetrically as well as asymmetrically.

In asymmetric versions the asymmetry is equal in all quarters of the rotor. In practice, this means that the magnets have corresponding positions and are placed in four groups with a distance of 90° (mech.) between them.

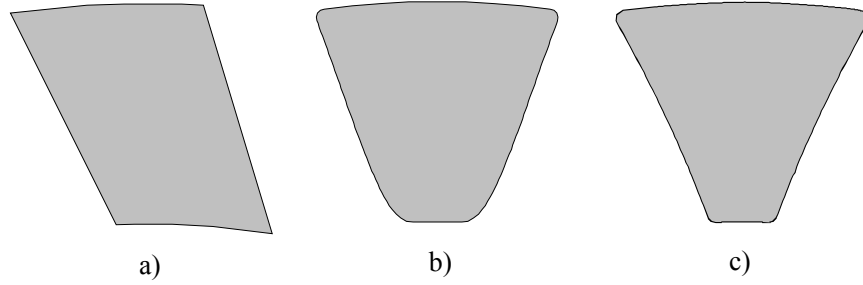


Fig. 4.1. Three different magnet shapes were compared in the calculation. a) 60° (el.) skewed edges (PM1), b) sinusoidal shape (1st and 3rd harmonic) (PM2) and c) skewed and curved edges (PM3). The relative width (α_p) of PM1 is 0.75. The relative width of the outer diameter of PM2 is 0.96, having 10% 3rd harmonic content of the fundamental. The outer diameter α_p of PM3 is 0.96 and inner 0.29.

To further minimise the effects of cogging another one additional slot ($Q_s = 121$) was added to the fractional slot stator winding version. With such a stator it should be possible to effectively eliminate cogging since the magnet edges of different magnets pass the stator slots in different phases. This stator was tested with PM1₂, PM2 and PM3₀.

4.2 Reference Motor Calculations

The model accuracy appears to be an important factor in the calculations as the calculation time and the calculation results are concerned. The actual magnet form and the magnet form resulting from the radial division (fig. 2.1) may produce a different torque harmonic content if the radial division is rough. A comparison was made using 30° (el) skewed magnets having numbers of radial calculation sections set between 3 ... 61. The calculation results clearly show the effect of the division on the torque quality (Fig. 4.2).

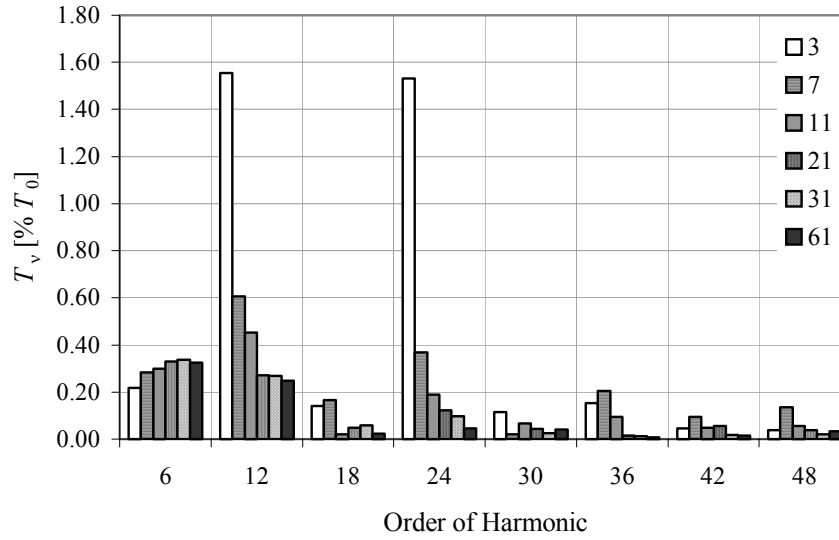


Fig. 4.2. Torque harmonic contents when using 30 °(el.) skewed magnets divided in different numbers of calculation sections. The results show clearly that the model should have at least 20 sections in order to obtain reliable results if the shape differs from the one shown in figure 2.1.

As it can be noticed, a complex magnet shape (differs from figure 3.18) requires at least 20 radial calculation sections to reach an acceptable level in the torque calculation. This is shown by the fact that the calculation results remain quite stable with the calculation numbers 21, 31 and 61. Increasing the number of sections beyond this does not make any more a big difference. The results given later in this study are calculated using at least 25 sections. If 2D FEM should be used the calculation would correspond to the calculation of one average permanent magnet section. In order to get satisfactory results the magnets should be divided, according to the results of Fig. 4.2, into at least 20 slices and the 2D calculation should be repeated for every slice. Referring to chapter 2, the statement that 2D FEM is not applicable to PMSM harmonic torque calculation is hereby confirmed.

The number of the iteration loops in the saturation calculation is the other factor that affects the result accuracy and the calculation time. A reference calculation was made with the SOR-shape (fig 3.18), $\alpha_p = 0.8$ magnet and with five different numbers of iterations (Fig. 4.3).

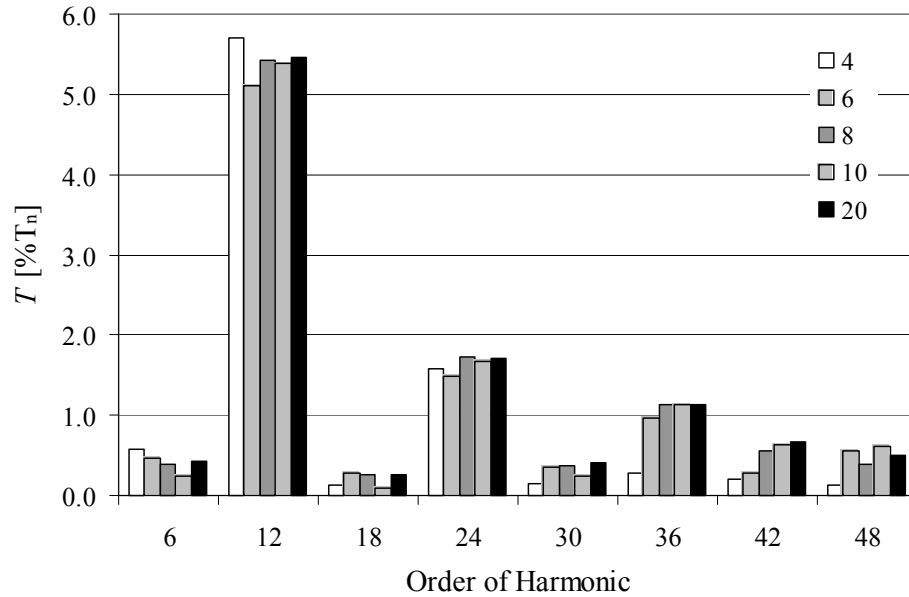


Fig. 4.3. The torque harmonics created by a rotor with SOR-shaped magnets using five different numbers of iteration loops in the iron saturation calculation.

The results obtained with four loops already approximate the result obtained with 20 loops, but according to the calculation at least eight loops are recommended. With a low torque ripple level ($\sim 1\%$ of average torque) even a half percent unit change in a harmonic makes a big difference in the comparison. Even when 20 loops are used the calculation time remains really low compared to the calculation time needed by 3D FEM (see chapter 4.2.1).

4.2.1 Comparison between FEM and Analytical Calculation

A SOR-type magnet, described in figure 3.18, was calculated comparably in no load condition using 3D FEM (Flux3D™) and using the analytical equations given in Appendix I. The comparing results are given in figure 4.4. Because the model turned out to be too large, the element network in the FEM-calculation was made somewhat sparse.

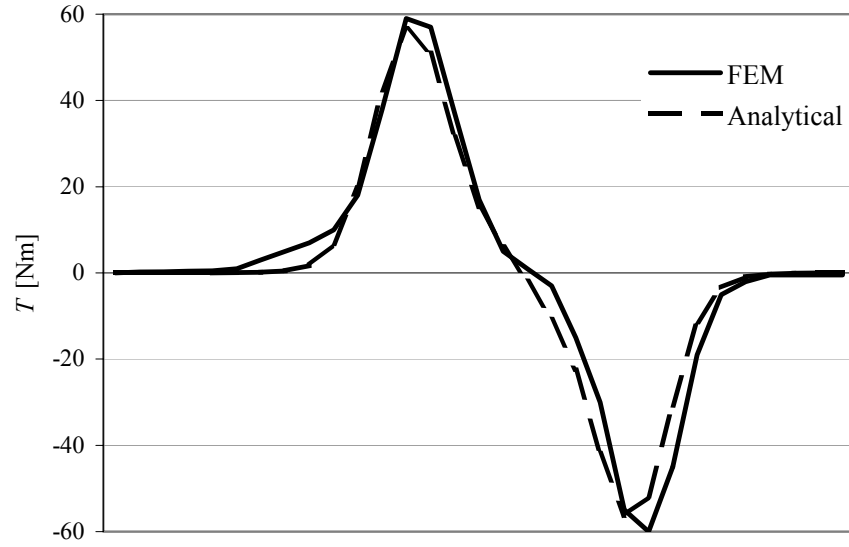


Fig. 4.4. Calculated cogging torque along one slot pitch created by the SOR-magnets (see fig. 3.18 in an axial flux machine).

The calculation over the length of two slot pitches contains only 30 time steps. This can be observed from the results (Fig. 4.4) as a stepwise movement. With respect to the shape and amplitude the results seem to be close to each other. Bianchi (2000) performed the 2D-calculation for rectangular PMs in a radial flux motor and obtained results that are similar with those given in the curves of fig. 4.4.

A corresponding comparison of both calculations methods was done in chapter 2.2 discussing the calculating of the air-gap flux density distribution created by the PM2-magnet type. The results obtained are presented in chapter 3.5.2 (optimal width of the permanent magnet)

Zhu and Howe (2000) made a calculation for a radial flux PM motor ($Q_s = 36$, $p = 3$, $w_{so} = 3.8$ mm, $\delta_{ag} = 1.3$ mm, $h_{PM} = 9.1$ mm, $L_{sc} = 95$ mm), varying the relative magnet width α_p between 0.5 ... 1.0 (fig. 4.5). In their presentation they used both FEM and the analytical calculation. Some of the results were also verified with an actual motor. The same calculation process was repeated applying the analytical model introduced in this study (fig 4.6).

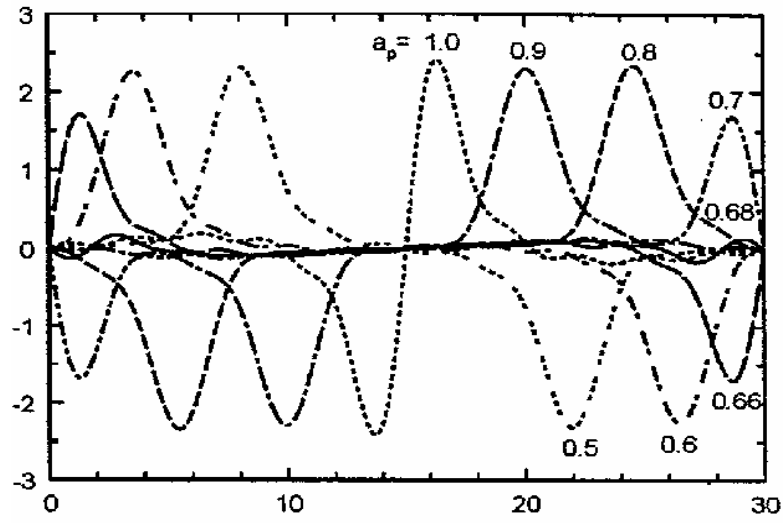


Fig. 4.5. Cogging torque calculations along one slot pitch by Zhu and Howe (2000) when varying the relative magnet width α_p between 0.5 ... 1.0 in the reference motor.

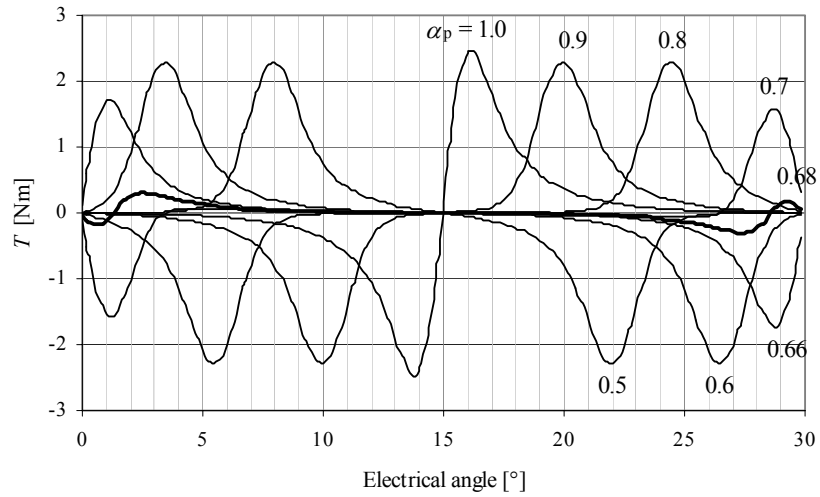


Fig. 4.6. Cogging torque calculations along one slot pitch made for Zhu's motor using the analytical model introduced in chapter 2. Relative magnet width, α_p is varied between 0.5 ... 1.0.

The results presented in figures 4.5 and 4.6 are very well corresponding. The results given 3D FEM and those obtained with the analytical equations could be compared once more in using PM3₀ -magnets. The 3D FEM calculation model is illustrated in figure 4.7. Both the

calculations were made using constant angular velocity. Figure 4.8 shows the torque behaviour along one pole pitch and figure 4.9 the frequency contents (spectrum) of the torque. The calculating was done using the reference motor measurements with the following parameters:

Table 4.1. Calculation parameters

Parameter	Value
Q	120
P	10
NI_{RMS}	680 A / slot
w/τ_p	1
w_{so}	4.5 mm
δ_{ag}	2.5 mm
h_{PM}	5.5 mm
B_r	1.1 T
μ_{PM}	1.1
Stator Material	M700-100A

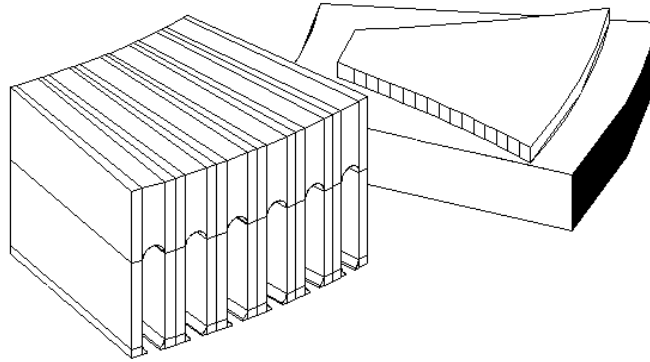


Fig. 4.7. Finite element model of the AFPMSM used in the reference calculations. Due to symmetry the model is made for one pole length (six slots in $m = 3$ and $q = 2$ motor).

The finite element calculation was done using a time step corresponding to 122 points per one pole pair length. In order to have equal conditions for both calculation processes the analytic calculation was done correspondingly. This means that the number of calculation steps is not a multiple of $2mq$ (number of slots per pole pair) and it can be seen as small content of several

different harmonic orders in figure 4.9 and also as small changes between the pulses in figure 4.8.

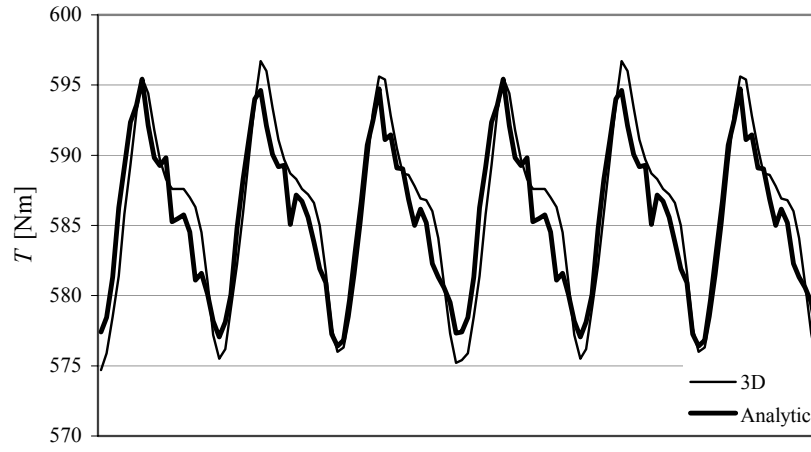


Fig. 4.8. The calculated torque for the reference motor with PM2₀ along one pole pair length. The thin line is calculated with 3D FEM and the bold line with the analytical equations.

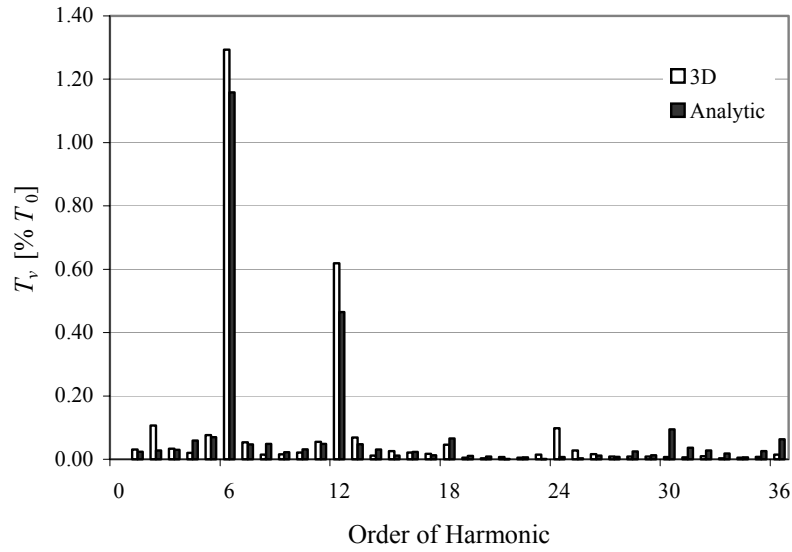


Fig. 4.9. Harmonic contents of the torque curves (Fig 4.8) calculated with 3D FEM and with the analytic model.

The shape of the torque and especially the harmonic contents are very similar. The shape of the air-gap flux density waves at different radii of the motor (producing the torques in figure 4.8) are given in figures 4.10 (3D FEM) and 4.11 (analytic model)

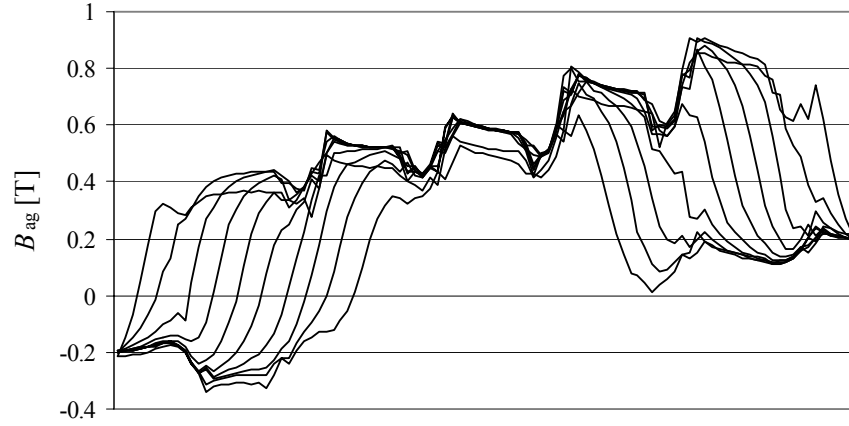


Fig. 4.10. Air-gap flux density shapes in one pole area at different radii in the AFPMSM, with $PM2_0$ corresponding to the load condition of figure 4.7, calculated with 3D FEM.

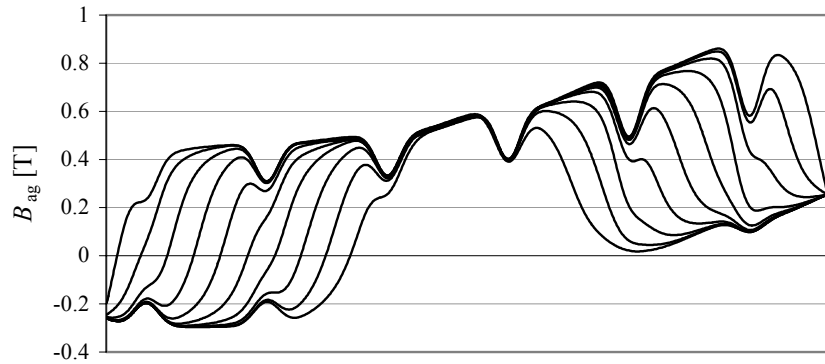


Fig. 4.11. Air-gap flux density shapes in one pole area at different radii in the AFPMSM, with $PM2_0$ corresponding to the load condition of figure 4.7, calculated with analytic equations.

It can be observed some non-uniformity between the two figures 4.10 and 4.11. Although the two flux density forms above are slightly different, it is shown in Figs. 4.8 and 4.9 showed that the torque produced in both cases is quite equivalent.

Difference between 3D FEM and the analytic equations regarding the required calculation resources and calculation time

In addition to the results, also the hardware requirements and required time for the model definition and the problem calculation are essential factors for comparison. To enable verification of both methods the main parameters of the reference calculation and system requirements are listed in table 4.2:

Table 4.2. Model parameters and system requirements in the reference calculation (Figs 4.6 and 4.7).

Parameter	Flux 3D	Analytic calculation
Model size	One pole	One pole pair
Number of 3D nodes	290 300	
Number of 3D elements	213 110	
Elements	2 nd order (Hierarchic) *)	
Air-gap element size	1.25 mm (two layers)	
Iteration criteria		
- Newton-Rhapson (non-lin.)	10 ⁻⁴	
- Stabilisation (linear system)	10 ⁻⁶	8 loops in saturation
Data storage size:		
- Geometry	393 kbytes	< 1 kbyte
- Element network	111 Mbytes	
- Results	8.6 Mbytes / calculation point	< 1 kbyte
Computer requirements:		
- Processor recommendation **)	Min. 1 GHz	100 MHz
- Random Access Memory **)	1 Gbyte	126 Mbytes
Calculation time (Pentium 4, 1.8 GHz / 1 Gbyte) :		
- pre-calculation	~ 58 min	< 10 s
- calculation / point	~ 40 min	< 1.5 s

*) Cubic and pyramide elements

**) values are not definite minimum requirements, but recommended to keep the calculation time reasonable.

In the FEM calculation the main interest is focused and the most dense element network is concentrated in the air-gap region. The software calculates first a static solution as a base for transient calculation. When constant rotor velocity is used the calculation stabilises straight from the beginning. When the exact rotor angle is unknown at the start and when free rotor velocity is used (depends on the torque and inertia) the stabilizing may take dozens of calculation points. Figure 4.12 illustrates the effect of the load inertia on the stabilizing of the torque, when the rotor start angle (pole angle) is 9° below that used with constant velocity.

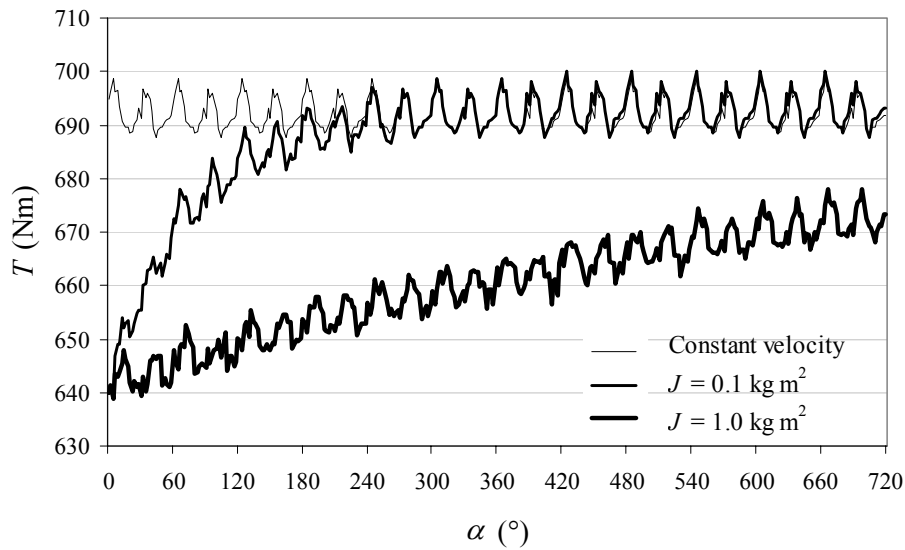


Fig. 4.12. The stabilizing of the torque in the calculation with two different inertias ($J = 0.1 \text{ kg m}^2$ and $J = 1.0 \text{ kg m}^2$) and with constant velocity. It can be noticed that with an inertia of 1.0 kg m^2 the calculation is not stabilized in 720° (el.). The calculation angle at the start was chosen 9° (el.) below the constant velocity angle. The analytical model is used in the calculations.

With the element numbers presented in table 4.2 the calculation with FEM may take several days, even when it is used the fastest personal computers and a large inertia (figure 4.12). After stabilizing has happened the curves (constant velocity and $J = 0.1 \text{ kg m}^2$) are well corresponding. Figure 4.13 shows the behaviour of the angular velocity in the same calculation (the motor was driven with 10 Hz supply frequency).

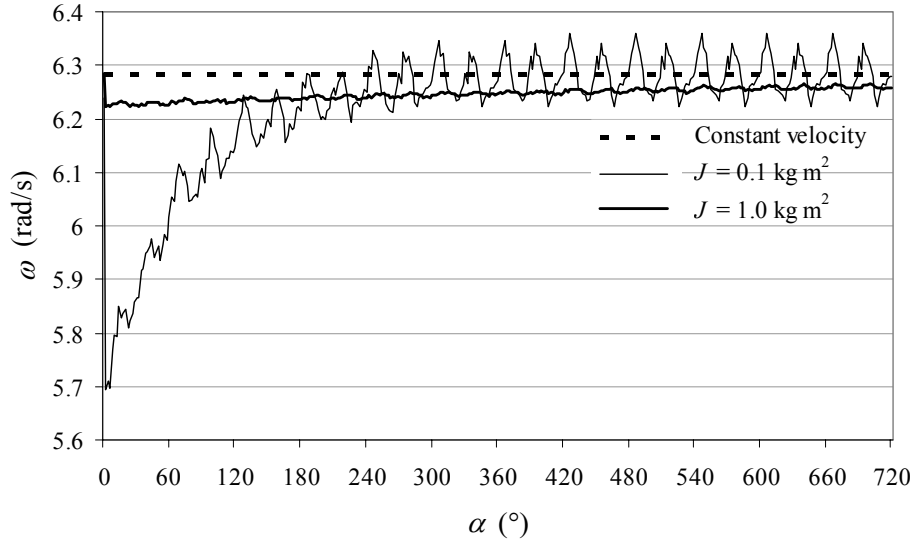


Fig. 4.13. The stabilizing of the angular velocity in the calculation with two different inertias ($J = 0.1 \text{ kg m}^2$ and $J = 1.0 \text{ kg m}^2$) and with 10 Hz ($p = 10$) supply. The calculation angle at the start was chosen 9° (el.) below the constant velocity angle. The analytical model is used in the calculations. α is the electric angle in the calculation.

Figure 4.13 shows that the lower is the inertia, the faster the average speed stabilizes, but also the higher is the amplitude of the ripple. Constant angular velocity corresponds to an infinite inertia with chosen rotor angle.

The method presented in this work is conclusively faster both in the problem definition and in the calculation. Due to the simplicity of the reluctance network the accuracy of the method is not as good as that of 3D FEM when a large number of high order (> 1) elements is used. The high price of the 3D FEM software license and the complexity of the modelling are stimulating factors to use the analytic model in certain cases.

4.3 Test Setup

Different motor versions (AFPMSM) were tested with the test setup presented in fig. 4.14. The motor was driven without any speed or angle feedback with an ABB ACS 600 frequency converter. The load (DC motor fed with ABB DCS 500) was fixed to the test motor with two tangentially stiff clutches. The torque and speed sensors were attached between the machines.

The torque and the speed signals were amplified (VibroMeter) and fed to the computer as analogue signals.

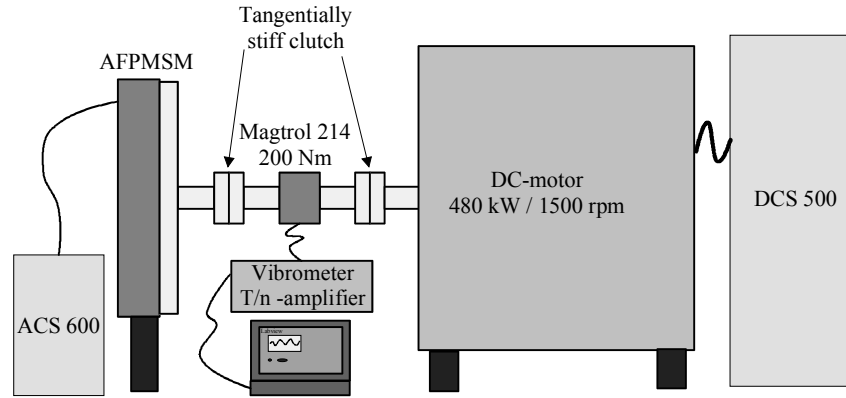


Fig. 4.14. The test set-up for the torque quality measurements.

Due to the test arrangements the harmonic torque excitations were amplified differentially depending on the supply frequency. One of the motor versions was driven with constant torque and current and with six different speeds ($f_s = 1.5, 3, 5, 8, 10$ and 13 Hz) and the harmonic torques were measured. The test set-up had a resonance frequency at about 25 Hz, which can be clearly seen in Figs. 4.15, 4.16 and 4.17.

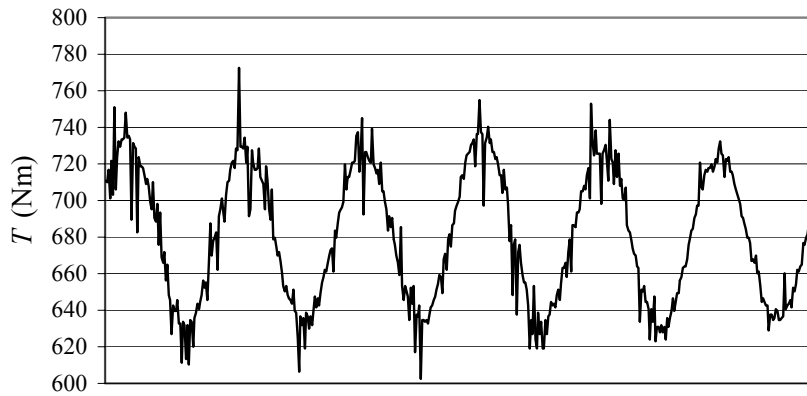


Fig. 4.15. Torque vibration along two pole pitches of the AFPMSM with PM2₀ magnets at 24 Hz (third harmonic).

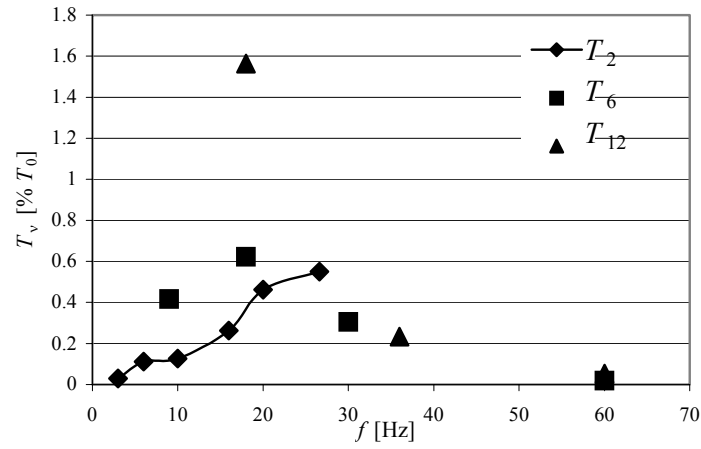


Fig. 4.16. Test arrangement amplification at different frequencies. Harmonic torques (orders two, six and twelve) were measured with the constant average torque and different supply frequencies. Excitations are strongly amplified around 20...25 Hz.

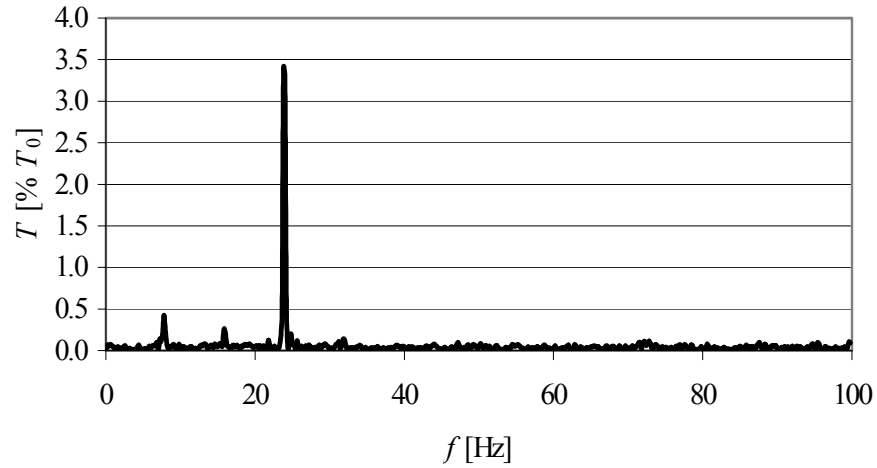


Fig. 4.17. The motor with PM2₀ magnets was driven at 8 Hz. The third harmonic, which in other measurements is a lot smaller than for example the first or the second, is highly amplified.

The natural frequencies of the test system disturbed the measurements remarkably. When any harmonic of the supply frequency occurs near by the resonance frequency, it is amplified causing RMS amplitudes up to 5 % of the average torque. For this reason, special consideration should be paid to test arrangements.

4.4 Comparison between Calculations and Measurements

4.4.1 Standard Stator

In order to get equal amplifications with the 1st and the 2nd and with the 6th and the 12th harmonics they were measured at the same frequencies (3 Hz and 18 Hz), having supply frequencies of 3 Hz (1st and 6th) and of 1.5 Hz (2nd and 12th). As it was shown earlier, torque harmonic excitations might be caused also by other sources, such as current offset and gain errors, which affect the low harmonics (first and second). In the investigations, latter have been eliminated as well as possible. Their influence is studied closer in chapter 4.4.3. As figure 4.18 shows, the first and second harmonic torques are not much dependent on the magnet type or the unequal magnet distribution (asymmetry), contrary to the 6th and 12th, which are given in fig. 4.19.

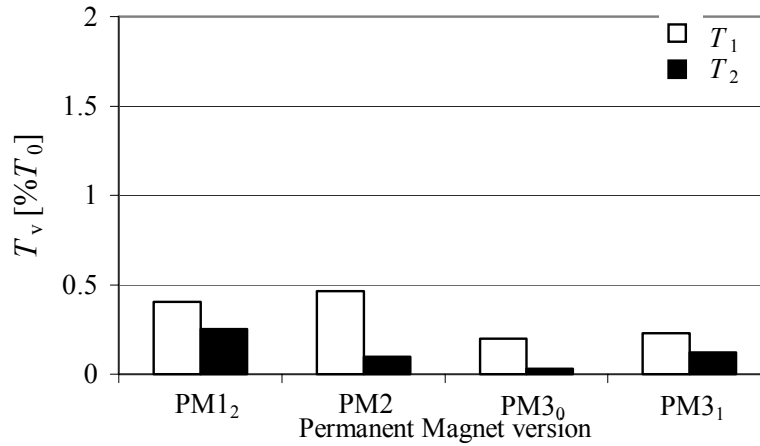


Fig. 4.18. Axial flux motor first and second harmonic torques measured for three different shapes of magnets at the motor rated torque. The magnet PM3 is measured using both symmetric and asymmetric distributions.

When an ideal supply is used in a symmetrical three-phase machine the 6th harmonic is the first to appear in the calculations and thus the first and the second harmonics are zero and not visible in the figures. The results (6th and 12th of harmonic) of the calculations with the same motor versions as given in figure 4.19 are presented in fig. 4.20. Even though the amplitudes between the calculations and measurements differ, the ratios between the harmonic orders and magnet

versions correspond well to each other. The difference between the measurements and calculations can be mainly explained by the frequency dependent amplification of the system.

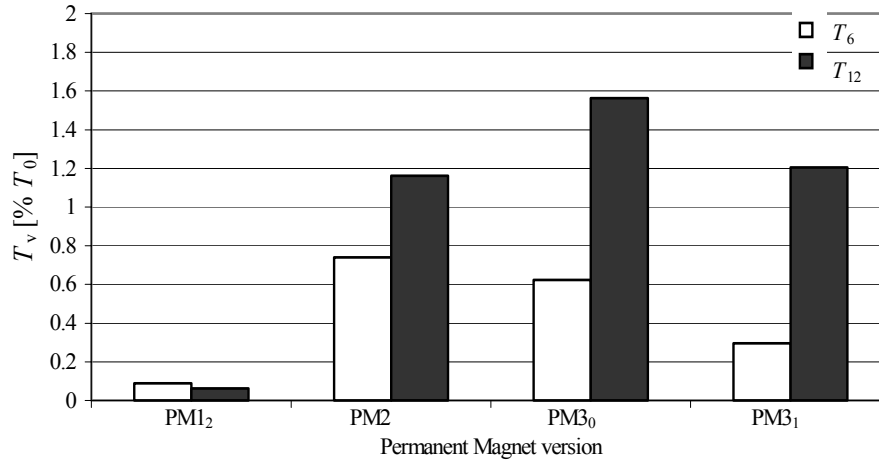


Fig. 4.19. Axial flux motor torque vibration amplitudes of the 6th and the 12th harmonics measured with three different shapes of magnets at motor rated torque. The machine equipped with the magnet PM3 is measured using both symmetric and asymmetric distributions.

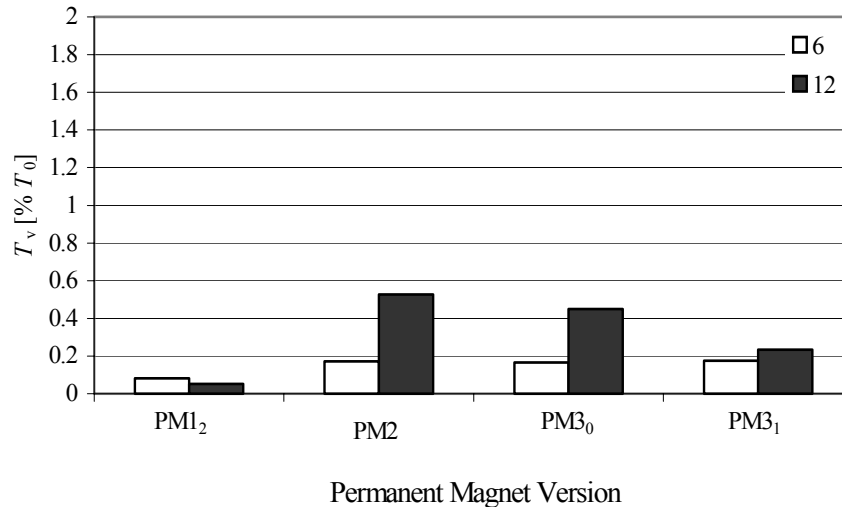


Fig. 4.20. Axial flux motor torque vibration of the 6th and 12th harmonic calculated with three different shapes of magnets at motor rated torque. The machine equipped with the PM3 magnet is calculated using both symmetric and asymmetric magnet distributions.

As vibration is concerned, PM1 with asymmetric magnet distribution appears to be clearly the best solution in the calculation as well as in the measurement. In general, the results obtained with the different magnets are appropriate for most motor applications as the highest amplitudes remain below 2 % of the average torque.

4.4.2 The Influence of the Additional Slot Stator

One 121-slot stator was manufactured to create a suitable asymmetry in order to reduce the cogging torque. This version was measured (fig. 4.21) and calculated (fig. 4.22) with three different rotor versions: PM1₂, PM2 and PM3₀.

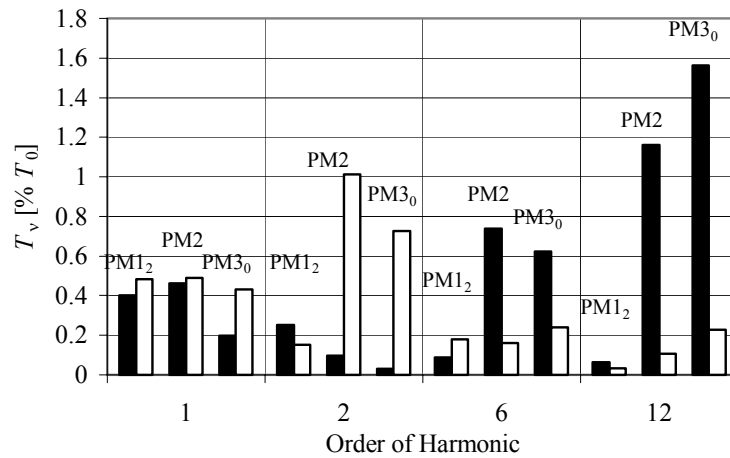


Fig. 4.21. Comparison (measurements) between the torque quality of the standard stator (the first of each bar pair) and the additional-slot-stator.

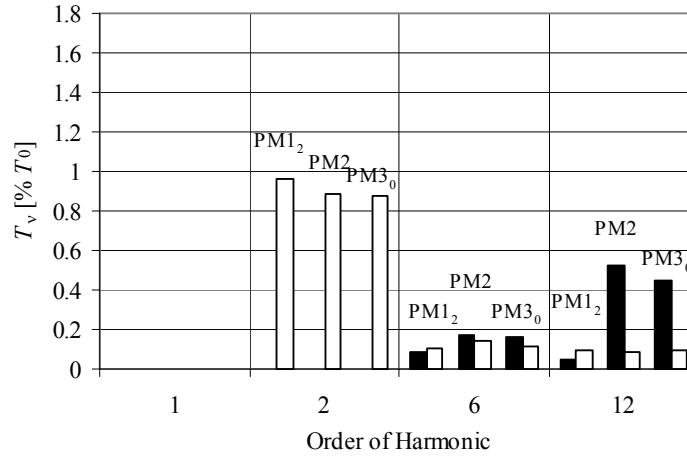


Fig. 4.22. Comparison (Calculation) between the torque quality of the standard stator (the first of each bar pair) and the additional-slot-stator.

Similarly as with standard stator, the test setup amplification affected the amplitude of the harmonics. Nevertheless, a comparison between the different versions could be made. In the asymmetric PM1-case the difference was predictably small, contrary to the symmetric magnet distributions (PM2 and PM3) where the effect is considerably. Asymmetry allows some freedom in the magnet shaping without dramatically affecting the cogging component. The disadvantage is that with the asymmetry low harmonics are produced.

4.4.3 Measured and Calculated Air-gap Permeance Harmonic Torque

The cogging torque of the reference motor with any of the magnet shapes given in fig. 4.1 is so small that it cannot be noticed by rotating the motor by hand. The friction itself is not constant and is much more than the cogging and therefore the effect of cogging was difficult to measure accurately. The measurement was done according to the test set-up illustrated in figure 4.23 and the results of the measurement and the corresponding calculation are given in figure 4.24. A weight was let to fall freely, accelerating the rotor to about 0.16 rad/s constant speed. As it can be seen, the spectrum of the measurement contains a lot of disturbing components, but still the cogging frequency (12th) is the highest peak. The calculation gives approximately corresponding values for the 12th and the 24th, when all the other harmonics below 24th are zero.

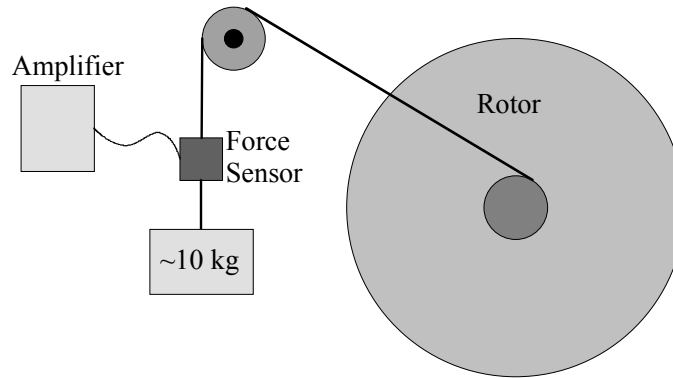


Fig. 4.23. Test set-up for the measuring of the cogging torque. The weight (~10 kg) was chosen to compensate the friction torque so that the velocity was almost constant at the measurement time.

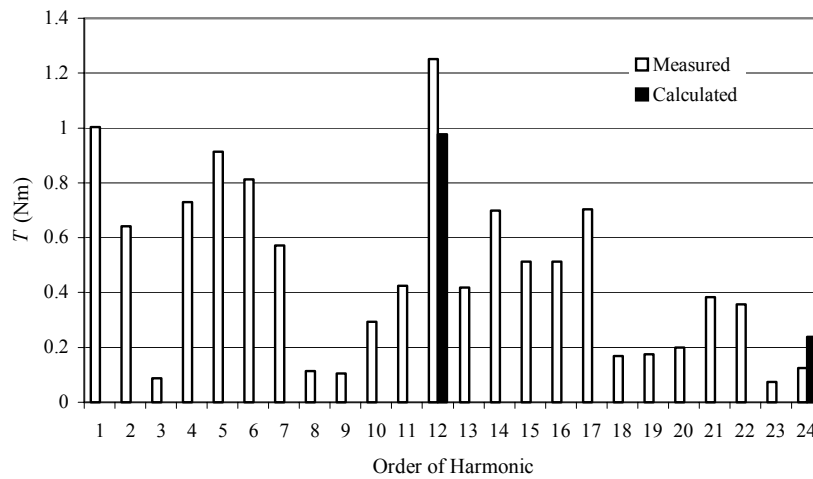


Fig. 4.24. Comparison between measured and calculated cogging torque with PM1

4.4.4 Current Asymmetry Effects

In addition to the motor asymmetries also the supply, in this case the frequency converter, includes non-linearities, such as current measurement offset and gain errors. These effects were already observed in the earlier motor version measurements. In an ABB ASC600 the current

measurement offset and gain values can be adjusted. First, it was sought for the optimum parameter set-up for the gain and the offset by means of torque measurements. Then, the values obtained were varied in one phase using offset errors between 0 ...1.25 % and gain errors between 0 ...4 % (Laurila 2002). The motor model is fed by currents and allows thus current manipulation factors such as the offset or gain.

Offset

An offset error in a phase current causes the first torque harmonic (supply frequency) component in the torque spectrum. Table 4.3 presents the values for the measured and calculated first harmonic with two different offset errors in one phase current.

Table 4.3. Measured and calculated fundamental frequency torque with two different offset errors.

Offset error	Calculated $T_1[\% T_0]$	Measured $T_1[\% T_0]$
0.75 %	0.74	1.24
1.25 %	1.20	2.02

According to the measurements and the calculations the effect is linear and even small errors create undesirable vibrations as it was shown in table 4.3. The measurement was made using 10 Hz supply frequency.

Gain

Error in gain may appear in two different ways; linear error is caused by an incorrect amplification in the measurement and non-linear error is the result of a non-linearity of a measurement system component. Figure 4.25 shows the torque curves of the motor (PM1₂) calculated and measured with 4 % gain and 0.25 % offset errors at about nominal torque. The measurement was made at 5 Hz supply frequency. Table 4.4 gives the calculated and measured results of the gain error.

Table 4.4. Measured and calculated second harmonic torque with two different gain errors.

Gain error	Calculated $T_2[\% T_0]$	Measured $T_2[\% T_0]$
2.0 %	1.31	1.43
4.0 %	2.64	2.89

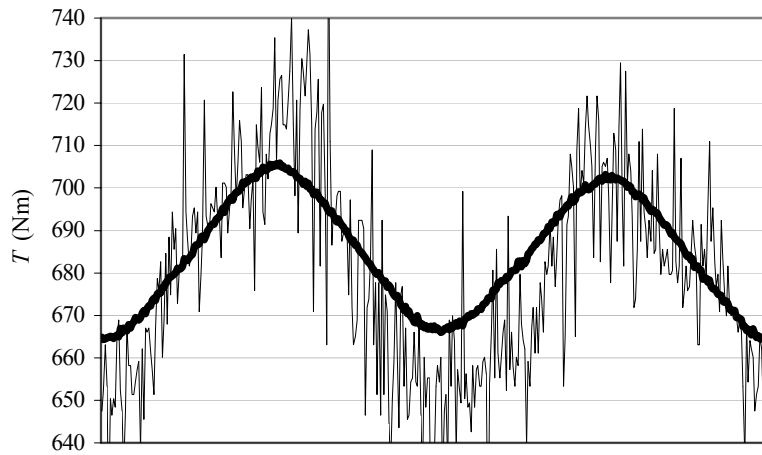


Fig. 4.25. Motor torque (PM1₂) measured and calculated along two pole pitches with an one-phase gain error of 4 % and with offset error 0.25%. The bold line is the calculated torque.

In the calculation only the linear component was considered. Table 4.4 and figure 4.25 show that the calculation results match convincingly well the results obtained with the measurements.

4.5 Conclusions from the Comparison

The calculation procedure functions very reliably within the limits defined in the previous chapters. Comparison with both FEM and the measurements shows that the results obtained with the calculation procedure are promising.

It is shown that PM1 with asymmetric magnet distribution is obviously the most suitable magnet shape. Unfortunately, the symmetric distribution variant of this magnet shape was not available. Also the other magnet shapes (PM2 and PM3) are rather good and their use is acceptable in most motor applications. With PM2 and PM3 the stator asymmetry reduces the

cogging in a considerable way and, for this reason, the results obtained are approaching those of PM1. Due to the fact that the magnets in PM1 are already asymmetrically distributed, the additional asymmetry in the stator does not have a big effect anymore.

The measuring arrangement with its natural frequencies made it difficult to get absolute amplitudes of the harmonics, but the comparison between the magnets could be drawn successfully.

The power supply (ABB ACS600) made it also possible to vary the source phase current amplitude symmetry (gain and offset). The results obtained with the calculation and with the measurements are satisfying.

5 Conclusions

In recent years it could be observed a considerable increase in the studying of permanent magnet motor torque vibrations and especially of the cogging effect. Some of these studies apply analytical methods, but most of them use FEM. The objective for this thesis was to develop a simple but reliable calculation method for testing different factors of the motor and improving the reference motor.

First target

The first goal of this study was to create an analytical calculation method for the purpose of applying it to the surface mounted axial flux permanent magnet motor. The results have proven that analytical equations can be used for PM-motor modelling. These do not compete with FEM, but for certain purposes they may be applied and their application may also be considered as a “pre study” to FEM use in order to reduce the required number of calculations or iterations. As discussed in chapter four, the final result or absolute value is highly depended on the total system and its frequency response and not just on the motor excitation. For this reason, the effect generated by changes is often more interesting to study.

Analytical modelling offers several advantages:

- Easy modelling and parameter variation
- Easy to check the effect of different factors
- Fast calculation compared to FEM
- Can be modified for different accuracy levels (reluctance network)
- Equations easy to adapt for total (larger) systems
- Supply non-linearities can easily be considered
- Possible to use almost arbitrary magnet shape (constant thickness)
- Transients easy to calculate

The method has also some disadvantages and limitations compared to FEM. Of these it should be mentioned:

- Equal magnet height is required
- Magnetic circuit details modelling is limited

- Magnetising direction is assumed to be constant
- Different type of motors require their own models
- Does not include all the options that are available in FEM => many features are lacking
- Does not allow a same accuracy of fine modelling as FEM does

As a further disadvantage it should be noted that the different types of windings require their own model/part. Consequently, this also means that the program can be applied to different kinds of slotted windings by slightly manipulating it or by using separate models for the different windings.

The structure of the reluctance network used appears to be rather simple, even so the calculation results are promising when comparing them with the FEM results and with the measurements of the actual models. This may be mainly explained by the fact that even a simple network is capable of calculating reliably the instant flux in the teeth and thus the winding harmonics and the average torque. The permeance harmonics are calculated using the permeance function, by means of which the air-gap flux density can be accurately determined.

The Matlab-version of the calculation model has already been tested with the DTC –frequency converter model and, in the near future, it will be joined to the electromechanical-system model.

Second target

The second purpose of the study was to apply the developed calculation program. By means of the program the reference motor could be modified, the results achieved with FEM were verified and measurements with actual models were carried out.

The significance of the magnet shape decreases if an additional slot stator is used. However, as cogging is concerned, the results achieved are promising, and these results apply not only to skewed magnets PM1 but also to all the other magnet types.

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CALCULATION PROCEDURE

Calculation starts with the definition of the parameters (table A1.1) and properties of the motor.

Table A1.1 The calculation parameters

The name of the parameter	Symbol	Unit
The number of slots	Q_s	
The number of turns in one slot	N_s	
Slots per pole per phase	q	
Local winding pitch	w	m
Nr of pole pairs	p	
Local pole pitch	τ_p	m
Average air-gap radius	r_{ag}	mm
Air-gap length	δ_{ag}	mm
Magnet thickness	h_{pm}	mm
Stator core length	L_{sc}	mm
Slot opening width	w_{so}	mm
Slot opening height	h_{so}	mm
Slot width	w_{sl}	mm
Tooth height	h_{to}	mm
Permanent magnet remanence flux density	B_{pm}	T
Permanent magnet relative permeability	μ_{pm}	

The magnet is divided into a certain number of ring sectors. The properties of each sector are defined by two parameters: the relative width (α_p) of the sector and the position of the geographical centre of the sector in degrees (el.). An example of the file,

0.8	20
0.7	15
0.6	10
0.5	5

would define a magnet according to figure A1.1 in when stator is in plane.

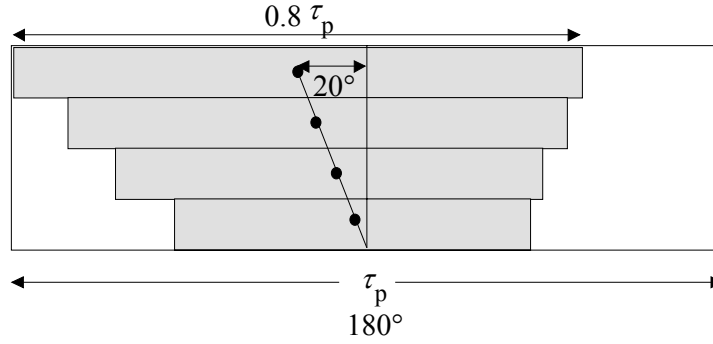


Fig. A1.1. A magnet defined in four sections, when stator pole is put to plane.

The air-gap flux density created by each sector is calculated using eqn. 2.2. Along the calculation these curves are moved according to the rotor angular position. Also an asymmetric positioning of the different poles is made by moving the curves according to the asymmetry level, and the torque created is calculated as an average value of the torque created by each different asymmetric position.

$$B_{pm} = \sum_{n=1,3,5,\dots}^{\infty} \frac{\frac{8B_r}{n\pi} \sin\left(\frac{n\pi\alpha_p}{2}\right)}{\left(e^{\frac{-2n\pi\delta}{\tau_p}} + 1 \right) + \frac{\mu_m \left(-e^{\frac{-2n\pi\delta}{\tau_p}} + 1 \right) \left(e^{\frac{2n\pi h_{pm}}{\tau_p}} + 1 \right)}{\mu_0 \left(e^{\frac{2n\pi h_{pm}}{\tau_p}} - 1 \right)}} e^{\frac{-n\pi\delta}{\tau_s}} \cos\left(\frac{n\pi x}{\tau_p}\right).$$

Reluctance net

The air-gap flux density is transformed to magneto motive force

$$NI_{pm} = \frac{B_{pm} \delta_{ag}}{\mu_0},$$

and updated to reluctance net as well as the total current in each slot. In first the calculation point and during the first iteration the relative permeability of the iron is set to default (2000), but after that updated according to the saturation in each component. The cross section area of each component is taken at the narrowest point, and the reluctance value is calculated with physical dimensions and interpolated BH curve. The reluctance network being used in model is presented in Fig. A1.2

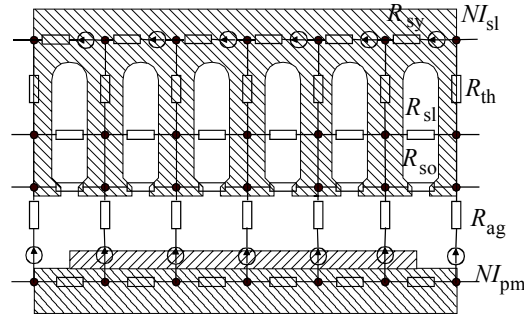


Fig. A1.2. Reluctance network of the calculation model in length of one pole ($q = 2$)

The network is iterated eight times to find the effect of the saturation. The flux in each component is solved by first solving the flux in each loop

$$[\phi] = [R]^{-1} [NI].$$

The calculation of the reluctance network parameters is presented in figure A1.3.

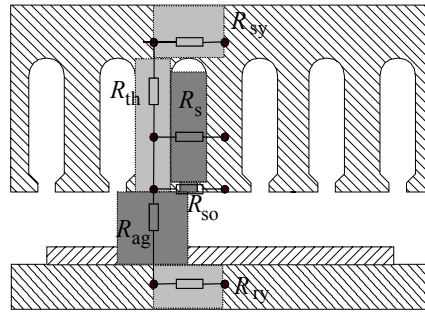


Fig. A1.3. Reluctance network of component definition. The calculation area is represented in grey tones.

Every element in the network presented in figure A1.3 is calculated from cubic form. (?)

The static torque of each calculation point and section is calculated using the total current in each coil multiplied with the total flux in the teeth inside the coil loop (Fig A1.4)

$$T_e(t) = \sum_{n=1}^{n_c} p N i_n(t) \varphi_n(t),$$

The torque in each sector is calculated by multiplying the average radius of the sector with the force. The flux is first divided equally along each slot pitch to constitute a stepwise curve. The slotting effect along one slot pitch is calculated

$$B(\alpha) = \left(1 - 2\beta \sin^{2n} \frac{\pi}{\alpha_d} \alpha \right) B_{\max}.$$

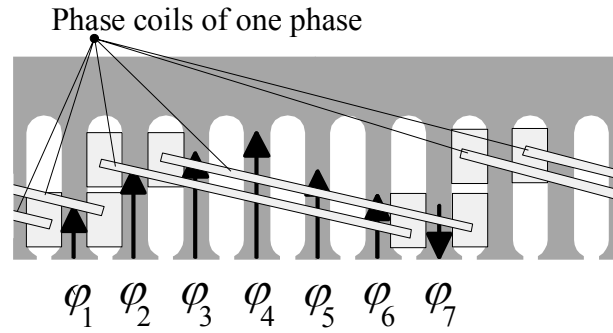


Fig. A1.4. Flux linkage in the stator

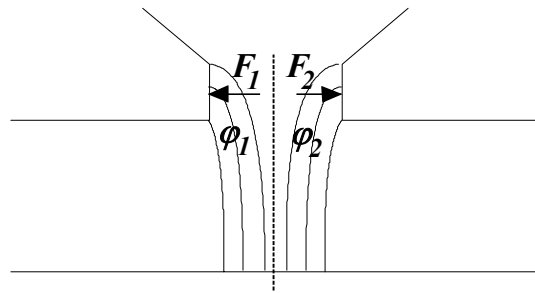


Fig. A1.5. Cogging component of the flux

The cogging torque component in each slot is calculated so that the slot opening is divided in two parts of equal length. The force created by each part is

$$F_{\text{cog},i} = \frac{B_{\text{ag,ave}}^2 A}{2\mu_0},$$

where $B_{\text{ag,ave}}$ is the average flux density of that part and A is the area of half slot opening. The cogging force of one slot is the subtraction of the two opposite components. The force is transformed to torque by multiplying it with the corresponding radius and then adding it to the static torque.

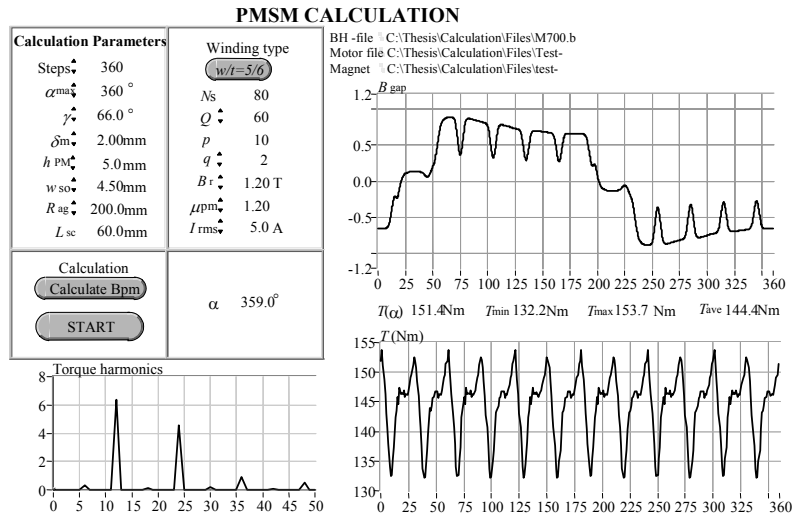
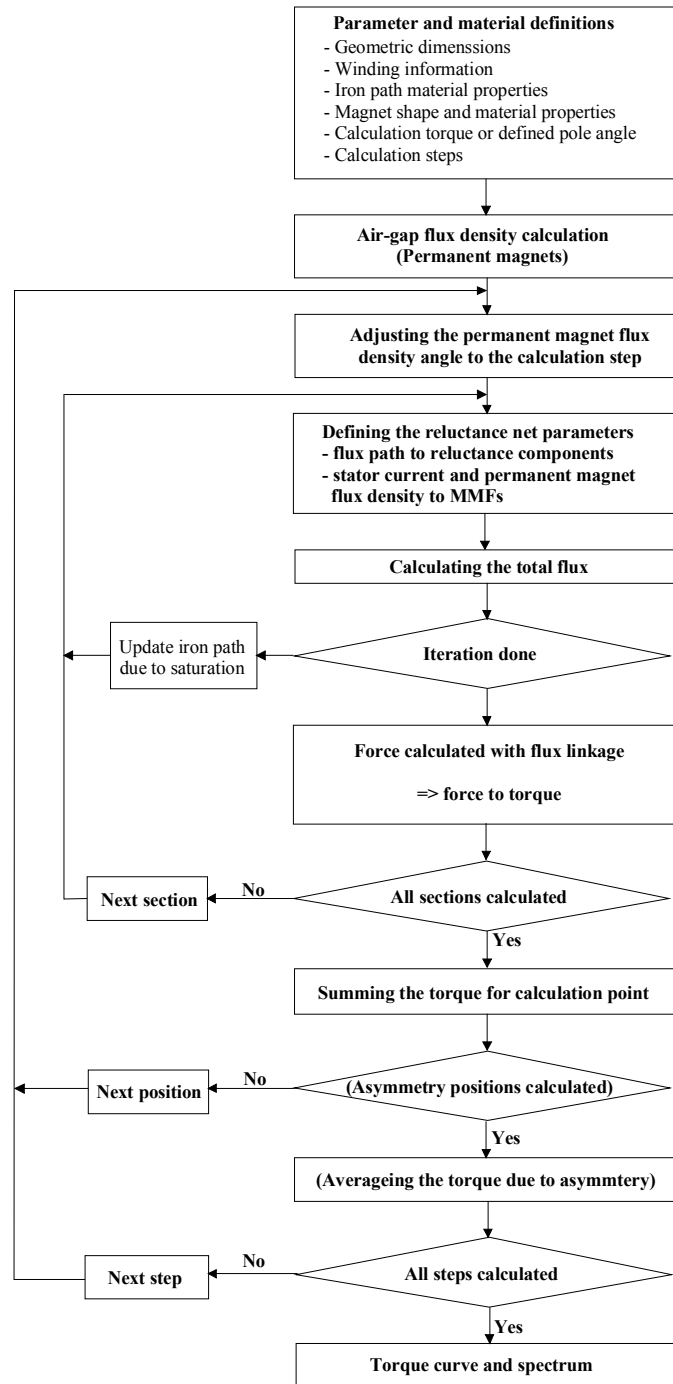


Fig. A1.6. The main view of the calculation program. Calculation parameters are defined in the upper left corner. The calculation results T (Nm) and the torque harmonics are presented in the two figures at the bottom. The upper right figure presents the air gap flux density in a pole pair area during the calculation.

Calculation prpcedure



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